

# Mathematica 11.3 Integration Test Results

Test results for the 700 problems in "4.3.1.2 (d sec)^m (a+b tan)^n.m"

Problem 11: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^7 (a + i a \text{Tan}[c + d x]) dx$$

Optimal (type 3, 98 leaves, 5 steps):

$$\frac{5 a \text{ArcTanh}[\text{Sin}[c + d x]]}{16 d} + \frac{i a \text{Sec}[c + d x]^7}{7 d} + \frac{5 a \text{Sec}[c + d x] \text{Tan}[c + d x]}{16 d} + \frac{5 a \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{24 d} + \frac{a \text{Sec}[c + d x]^5 \text{Tan}[c + d x]}{6 d}$$

Result (type 3, 273 leaves):

$$\begin{aligned} & - \frac{5 a \text{Log}[\text{Cos}[\frac{1}{2}(c + d x)] - \text{Sin}[\frac{1}{2}(c + d x)]]}{16 d} + \\ & \frac{5 a \text{Log}[\text{Cos}[\frac{1}{2}(c + d x)] + \text{Sin}[\frac{1}{2}(c + d x)]]}{16 d} + \frac{i a \text{Sec}[c + d x]^7}{7 d} + \\ & \frac{48 d (\text{Cos}[\frac{1}{2}(c + d x)] - \text{Sin}[\frac{1}{2}(c + d x)])^6}{5 a} + \frac{16 d (\text{Cos}[\frac{1}{2}(c + d x)] - \text{Sin}[\frac{1}{2}(c + d x)])^4}{a} + \\ & \frac{32 d (\text{Cos}[\frac{1}{2}(c + d x)] - \text{Sin}[\frac{1}{2}(c + d x)])^2}{a} - \frac{48 d (\text{Cos}[\frac{1}{2}(c + d x)] + \text{Sin}[\frac{1}{2}(c + d x)])^6}{5 a} - \\ & \frac{16 d (\text{Cos}[\frac{1}{2}(c + d x)] + \text{Sin}[\frac{1}{2}(c + d x)])^4}{32 d (\text{Cos}[\frac{1}{2}(c + d x)] + \text{Sin}[\frac{1}{2}(c + d x)])^2} \end{aligned}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^5 (a + i a \text{Tan}[c + d x]) dx$$

Optimal (type 3, 76 leaves, 4 steps):

$$\frac{3 a \text{ArcTanh}[\text{Sin}[c + d x]]}{8 d} + \frac{i a \text{Sec}[c + d x]^5}{5 d} + \frac{3 a \text{Sec}[c + d x] \text{Tan}[c + d x]}{8 d} + \frac{a \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{4 d}$$

Result (type 3, 209 leaves):

$$\begin{aligned}
 & - \frac{3 a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\
 & \frac{3 a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{i a \operatorname{Sec}[c+d x]^5}{5 d} + \\
 & \frac{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^4}{a} + \frac{3 a}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
 & \frac{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^4}{a} - \frac{3 a}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2}
 \end{aligned}$$

**Problem 13: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^3 (a+i a \operatorname{Tan}[c+d x]) d x$$

Optimal (type 3, 54 leaves, 3 steps):

$$\frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \frac{i a \operatorname{Sec}[c+d x]^3}{3 d} + \frac{a \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 d}$$

Result (type 3, 145 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} + \\
 & \frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} + \frac{i a \operatorname{Sec}[c+d x]^3}{3 d} + \\
 & \frac{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2}{a} - \frac{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2}{a}
 \end{aligned}$$

**Problem 14: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x] (a+i a \operatorname{Tan}[c+d x]) d x$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} + \frac{i a \operatorname{Sec}[c+d x]}{d}$$

Result (type 3, 84 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2}+\frac{d x}{2}\right]-\sin\left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2}+\frac{d x}{2}\right]+\sin\left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d} + \frac{i a \operatorname{Sec}[c+d x]}{d}
 \end{aligned}$$

**Problem 22: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^2 (a+i a \operatorname{Tan}[c+d x])^2 d x$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{1}{3ad} (a + ia \tan[c + dx])^3$$

Result (type 3, 68 leaves):

$$\frac{1}{6d} a^2 \sec[c] \sec[c + dx]^3 \\ (3i \cos[dx] + 3i \cos[2c + dx] + 3 \sin[dx] - 3 \sin[2c + dx] + 2 \sin[2c + 3dx])$$

**Problem 23: Result more than twice size of optimal antiderivative.**

$$\int (a + ia \tan[c + dx])^2 dx$$

Optimal (type 3, 38 leaves, 2 steps):

$$2a^2 x - \frac{2ia^2 \log[\cos[c + dx]]}{d} - \frac{a^2 \tan[c + dx]}{d}$$

Result (type 3, 100 leaves):

$$-\frac{1}{2d} a^2 \sec[c] \sec[c + dx] (4 \operatorname{ArcTan}[\tan[3c + dx]] \cos[c] \cos[c + dx] - 4dx \cos[2c + dx] + \\ \cos[dx] (-4dx + i \log[\cos[c + dx]^2]) + i \cos[2c + dx] \log[\cos[c + dx]^2] + 2 \sin[dx])$$

**Problem 29: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx]^3 (a + ia \tan[c + dx])^2 dx$$

Optimal (type 3, 94 leaves, 4 steps):

$$\frac{5a^2 \operatorname{ArcTanh}[\sin[c + dx]]}{8d} + \frac{5ia^2 \sec[c + dx]^3}{12d} + \\ \frac{5a^2 \sec[c + dx] \tan[c + dx]}{8d} + \frac{i \sec[c + dx]^3 (a^2 + ia^2 \tan[c + dx])}{4d}$$

Result (type 3, 215 leaves):

$$\frac{1}{192d} a^2 \sec[c + dx]^4 \\ \left( 128i \cos[c + dx] - 45 \log\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] - 60 \cos[2(c + dx)] \right. \\ \left. \left( \log\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] - \log\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] \right) - 15 \right. \\ \left. \cos[4(c + dx)] \right. \\ \left. \left( \log\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] - \log\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] \right) \right) + \\ 45 \log\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] - 18 \sin[c + dx] + 30 \sin[3(c + dx)] \Big)$$

**Problem 30: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x] (a + i a \text{Tan}[c + d x])^2 dx$$

Optimal (type 3, 68 leaves, 3 steps):

$$\frac{3 a^2 \text{ArcTanh}[\text{Sin}[c + d x]]}{2 d} + \frac{3 i a^2 \text{Sec}[c + d x]}{2 d} + \frac{i \text{Sec}[c + d x] (a^2 + i a^2 \text{Tan}[c + d x])}{2 d}$$

Result (type 3, 146 leaves):

$$\begin{aligned} &-\frac{1}{4 d} \\ &a^2 \text{Sec}[c + d x]^2 \left( -8 i \text{Cos}[c + d x] + 3 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 3 \text{Cos}[2(c + d x)] \right. \\ &\quad \left. \left( \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) - \right. \\ &\quad \left. 3 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 2 \text{Sin}[c + d x] \right) \end{aligned}$$

**Problem 31: Result more than twice size of optimal antiderivative.**

$$\int \text{Cos}[c + d x] (a + i a \text{Tan}[c + d x])^2 dx$$

Optimal (type 3, 46 leaves, 2 steps):

$$-\frac{a^2 \text{ArcTanh}[\text{Sin}[c + d x]]}{d} - \frac{2 i \text{Cos}[c + d x] (a^2 + i a^2 \text{Tan}[c + d x])}{d}$$

Result (type 3, 180 leaves):

$$\begin{aligned} &\left( a^2 \left( \text{Cos}\left[\frac{1}{2}(c + d x)\right] \left( -2 i + \right. \right. \right. \\ &\quad \left. \left. \left. \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right) + \right. \\ &\quad \left. \left( 2 - i \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + i \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right. \\ &\quad \left. \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \\ &\quad \left( \text{Cos}\left[\frac{1}{2}(c + 5 d x)\right] + i \text{Sin}\left[\frac{1}{2}(c + 5 d x)\right] \right) \Big/ \left( d (\text{Cos}[d x] + i \text{Sin}[d x])^2 \right) \end{aligned}$$

**Problem 39: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^2 (a + i a \text{Tan}[c + d x])^3 dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$-\frac{i(a + ia \tan[c + dx])^4}{4ad}$$

Result (type 3, 84 leaves):

$$\frac{1}{4d} a^3 \sec[c] \sec[c + dx]^4 (3i \cos[c] + 2i \cos[c + 2dx] + 2i \cos[3c + 2dx] - 3 \sin[c] + 2 \sin[c + 2dx] - 2 \sin[3c + 2dx] + \sin[3c + 4dx])$$

**Problem 41: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^2 (a + ia \tan[c + dx])^3 dx$$

Optimal (type 3, 49 leaves, 3 steps):

$$-a^3 x + \frac{ia^3 \log[\cos[c + dx]]}{d} - \frac{2ia^4}{d(a - ia \tan[c + dx])}$$

Result (type 3, 99 leaves):

$$-\left( (a^3 (\cos[c + dx] (2i + 2dx - i \log[\cos[c + dx]^2]) + (-2 - 2i dx - \log[\cos[c + dx]^2]) \sin[c + dx]) (\cos[c + 4dx] + i \sin[c + 4dx])) / (2d (\cos[dx] + i \sin[dx])^3) \right)$$

**Problem 47: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx] (a + ia \tan[c + dx])^3 dx$$

Optimal (type 3, 61 leaves, 3 steps):

$$-\frac{3a^3 \operatorname{ArcTanh}[\sin[c + dx]]}{d} - \frac{3ia^3 \sec[c + dx]}{d} - \frac{2ia \cos[c + dx] (a + ia \tan[c + dx])^2}{d}$$

Result (type 3, 123 leaves):

$$\left( a^3 \cos[c + dx]^2 \left( 6 \operatorname{ArcTanh}[\sin[c] + \cos[c] \tan[\frac{dx}{2}]] \cos[c + dx] (i \cos[3c] + \sin[3c]) + (-\cos[2c - dx] + i \sin[2c - dx]) (5 \cos[c + dx] - i \sin[c + dx]) \right) (-i + \tan[c + dx])^3 \right) / (d (\cos[dx] + i \sin[dx])^3)$$

**Problem 54: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx] (a + ia \tan[c + dx])^4 dx$$

Optimal (type 3, 97 leaves, 4 steps):

$$\frac{15 a^4 \operatorname{ArcTanh}[\sin [c+d x]]}{2 d}-\frac{15 i a^4 \operatorname{Sec}[c+d x]}{2 d} \\ \frac{2 i a \cos [c+d x](a+i a \tan [c+d x])^3}{d}-\frac{5 i \operatorname{Sec}[c+d x]\left(a^4+i a^4 \tan [c+d x]\right)}{2 d}$$

Result (type 3, 906 leaves):

$$\left(15 \cos [4 c] \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right](a+i a \tan [c+d x])^4\right) / \\ \left(2 d(\cos [d x]+i \sin [d x])^4\right)- \\ \left(15 \cos [4 c] \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right](a+i a \tan [c+d x])^4\right) / \\ \left(2 d(\cos [d x]+i \sin [d x])^4\right)+ \\ \left(\cos [d x] \cos [c+d x]^4(-8 i \cos [3 c]-8 \sin [3 c])(a+i a \tan [c+d x])^4\right) / \\ \left(d(\cos [d x]+i \sin [d x])^4\right)+ \\ \left(\cos [c+d x]^4 \operatorname{Sec}[c](-4 i \cos [4 c]-4 \sin [4 c])(a+i a \tan [c+d x])^4\right) / \\ \left(d(\cos [d x]+i \sin [d x])^4\right)- \\ \left(15 i \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sin [4 c](a+i a \tan [c+d x])^4\right) / \\ \left(2 d(\cos [d x]+i \sin [d x])^4\right)+ \\ \left(15 i \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sin [4 c](a+i a \tan [c+d x])^4\right) / \\ \left(2 d(\cos [d x]+i \sin [d x])^4\right)+ \\ \left(\cos [c+d x]^4(8 \cos [3 c]-8 i \sin [3 c]) \sin [d x](a+i a \tan [c+d x])^4\right) / \\ \left(d(\cos [d x]+i \sin [d x])^4\right)+\frac{\cos [c+d x]^4\left(\frac{1}{4} \cos [4 c]-\frac{1}{4} i \sin [4 c]\right)(a+i a \tan [c+d x])^4}{d(\cos [d x]+i \sin [d x])^4\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2}- \\ \left(i \cos [c+d x]^4(4 \cos [4 c]-4 i \sin [4 c]) \sin \left[\frac{d x}{2}\right](a+i a \tan [c+d x])^4\right) / \\ \left(d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)(\cos [d x]+i \sin [d x])^4\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)\right)+ \\ \frac{\cos [c+d x]^4\left(-\frac{1}{4} \cos [4 c]+\frac{1}{4} i \sin [4 c]\right)(a+i a \tan [c+d x])^4}{d(\cos [d x]+i \sin [d x])^4\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2}+ \\ \left(i \cos [c+d x]^4(4 \cos [4 c]-4 i \sin [4 c]) \sin \left[\frac{d x}{2}\right](a+i a \tan [c+d x])^4\right) / \\ \left(d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)(\cos [d x]+i \sin [d x])^4\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)\right)$$

**Problem 55: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^3(a+i a \tan [c+d x])^4 d x$$

Optimal (type 3, 78 leaves, 3 steps):

$$\frac{a^4 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} - \frac{2 i a \operatorname{Cos}[c + d x]^3 (a + i a \operatorname{Tan}[c + d x])^3}{3 d} + \frac{2 i \operatorname{Cos}[c + d x] (a^4 + i a^4 \operatorname{Tan}[c + d x])}{d}$$

Result (type 3, 246 leaves):

$$\frac{1}{3 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4} a^4 \left( -3 \operatorname{Cos}[4 c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) + 3 \operatorname{Cos}[4 c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 2 \operatorname{Cos}[3 d x] \operatorname{Sin}[c] + 6 \operatorname{Cos}[d x] \operatorname{Sin}[3 c] + 3 i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4 c] - 3 i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sin}[4 c] + \operatorname{Cos}[3 c] (6 i \operatorname{Cos}[d x] - 6 \operatorname{Sin}[d x]) + 6 i \operatorname{Sin}[3 c] \operatorname{Sin}[d x] - 2 i \operatorname{Sin}[c] \operatorname{Sin}[3 d x] + 2 \operatorname{Cos}[c] (-i \operatorname{Cos}[3 d x] + \operatorname{Sin}[3 d x]) \right) (\operatorname{Cos}[c + d x] + i \operatorname{Sin}[c + d x])^4$$

**Problem 61: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^4 (a + i a \operatorname{Tan}[c + d x])^5 dx$$

Optimal (type 3, 55 leaves, 3 steps):

$$-\frac{2 i (a + i a \operatorname{Tan}[c + d x])^7}{7 a^2 d} + \frac{i (a + i a \operatorname{Tan}[c + d x])^8}{8 a^3 d}$$

Result (type 3, 143 leaves):

$$\frac{1}{56 d} a^5 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^8 (35 i \operatorname{Cos}[c] + 28 i \operatorname{Cos}[c + 2 d x] + 28 i \operatorname{Cos}[3 c + 2 d x] + 14 i \operatorname{Cos}[3 c + 4 d x] + 14 i \operatorname{Cos}[5 c + 4 d x] - 35 \operatorname{Sin}[c] + 28 \operatorname{Sin}[c + 2 d x] - 28 \operatorname{Sin}[3 c + 2 d x] + 14 \operatorname{Sin}[3 c + 4 d x] - 14 \operatorname{Sin}[5 c + 4 d x] + 8 \operatorname{Sin}[5 c + 6 d x] + \operatorname{Sin}[7 c + 8 d x])$$

**Problem 62: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^2 (a + i a \operatorname{Tan}[c + d x])^5 dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$-\frac{i (a + i a \operatorname{Tan}[c + d x])^6}{6 a d}$$

Result (type 3, 134 leaves):

$$\frac{1}{12 d} a^5 \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^6$$

$$\left( 20 \operatorname{Cos}[c] + 15 \operatorname{Cos}[c+2 d x] + 15 \operatorname{Cos}[3 c+2 d x] + 6 \operatorname{Cos}[3 c+4 d x] + \right.$$

$$\left. 6 \operatorname{Cos}[5 c+4 d x] - 20 \operatorname{Sin}[c] + 15 \operatorname{Sin}[c+2 d x] - 15 \operatorname{Sin}[3 c+2 d x] + \right.$$

$$\left. 6 \operatorname{Sin}[3 c+4 d x] - 6 \operatorname{Sin}[5 c+4 d x] + 2 \operatorname{Sin}[5 c+6 d x] \right)$$

Problem 63: Result more than twice size of optimal antiderivative.

$$\int (a + i a \operatorname{Tan}[c+d x])^5 dx$$

Optimal (type 3, 117 leaves, 5 steps):

$$16 a^5 x - \frac{16 i a^5 \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d} - \frac{8 a^5 \operatorname{Tan}[c+d x]}{d} +$$

$$\frac{2 i a^2 (a + i a \operatorname{Tan}[c+d x])^3}{3 d} + \frac{i a (a + i a \operatorname{Tan}[c+d x])^4}{4 d} + \frac{2 i a (a^2 + i a^2 \operatorname{Tan}[c+d x])^2}{d}$$

Result (type 3, 728 leaves):



$$\begin{aligned}
 & \frac{16 x \cos [5 c] \cos [c+d x]^5 (a+i a \tan [c+d x])^5}{(\cos [d x]+i \sin [d x])^5} - \\
 & \frac{8 i \cos [5 c] \cos [c+d x]^5 \log [\cos [c+d x]^2] (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} + \\
 & \left( \cos [c+d x]^3 (18 \cos [c]+5 i \sin [c]) \left( -\frac{1}{3} i \cos [5 c]-\frac{1}{3} \sin [5 c] \right) (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d \left( \cos \left[ \frac{c}{2} \right]-\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right]+\sin \left[ \frac{c}{2} \right] \right) (\cos [d x]+i \sin [d x])^5 \right) + \\
 & \frac{\cos [c+d x] \left( \frac{1}{4} i \cos [5 c]+\frac{1}{4} \sin [5 c] \right) (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} - \\
 & \frac{16 i x \cos [c+d x]^5 \sin [5 c] (a+i a \tan [c+d x])^5}{(\cos [d x]+i \sin [d x])^5} - \\
 & \frac{8 \cos [c+d x]^5 \log [\cos [c+d x]^2] \sin [5 c] (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} + \\
 & \left( \cos [c+d x]^2 \left( \frac{5}{3} \cos [5 c]-\frac{5}{3} i \sin [5 c] \right) \sin [d x] (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d \left( \cos \left[ \frac{c}{2} \right]-\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right]+\sin \left[ \frac{c}{2} \right] \right) (\cos [d x]+i \sin [d x])^5 \right) + \\
 & \left( \cos [c+d x]^4 \left( -\frac{50}{3} \cos [5 c]+\frac{50}{3} i \sin [5 c] \right) \sin [d x] (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d \left( \cos \left[ \frac{c}{2} \right]-\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right]+\sin \left[ \frac{c}{2} \right] \right) (\cos [d x]+i \sin [d x])^5 \right) + \\
 & \frac{1}{(\cos [d x]+i \sin [d x])^5} x \cos [c+d x]^5 \left( -8 \cos [c]^3+8 \cos [c]^5+32 i \cos [c]^2 \sin [c]- \right. \\
 & \quad \left. 48 i \cos [c]^4 \sin [c]+48 \cos [c] \sin [c]^2-120 \cos [c]^3 \sin [c]^2-32 i \sin [c]^3+ \right. \\
 & \quad \left. 160 i \cos [c]^2 \sin [c]^3+120 \cos [c] \sin [c]^4-48 i \sin [c]^5-8 \sin [c]^3 \tan [c]- \right. \\
 & \quad \left. 8 \sin [c]^5 \tan [c]+i (16 \cos [5 c]-16 i \sin [5 c]) \tan [c] \right) (a+i a \tan [c+d x])^5
 \end{aligned}$$

**Problem 64: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2 (a+i a \tan [c+d x])^5 dx$$

Optimal (type 3, 83 leaves, 3 steps):

$$-12 a^5 x + \frac{12 i a^5 \log [\cos [c+d x]]}{d} + \frac{5 a^5 \tan [c+d x]}{d} + \frac{i a^5 \tan [c+d x]^2}{2 d} - \frac{8 i a^6}{d (a-i a \tan [c+d x])}$$

Result (type 3, 649 leaves):

$$\begin{aligned}
 & - \frac{12 x \cos [5 c] \cos [c+d x]^5 (a+i a \tan [c+d x])^5}{(\cos [d x]+i \sin [d x])^5} + \\
 & \frac{6 i \cos [5 c] \cos [c+d x]^5 \log [\cos [c+d x]^2] (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} + \\
 & \left( \cos [2 d x] \cos [c+d x]^5 (-4 i \cos [3 c]-4 \sin [3 c]) (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^5 \right) + \frac{\cos [c+d x]^3 \left( \frac{1}{2} i \cos [5 c]+\frac{1}{2} \sin [5 c] \right) (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} + \\
 & \frac{12 i x \cos [c+d x]^5 \sin [5 c] (a+i a \tan [c+d x])^5}{(\cos [d x]+i \sin [d x])^5} + \\
 & \frac{6 \cos [c+d x]^5 \log [\cos [c+d x]^2] \sin [5 c] (a+i a \tan [c+d x])^5}{d (\cos [d x]+i \sin [d x])^5} + \\
 & \left( \cos [c+d x]^4 (5 \cos [5 c]-5 i \sin [5 c]) \sin [d x] (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d \left( \cos \left[ \frac{c}{2} \right]-\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right]+\sin \left[ \frac{c}{2} \right] \right) (\cos [d x]+i \sin [d x])^5 \right) + \\
 & \left( \cos [c+d x]^5 (4 \cos [3 c]-4 i \sin [3 c]) \sin [2 d x] (a+i a \tan [c+d x])^5 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^5 \right) + \\
 & \frac{1}{(\cos [d x]+i \sin [d x])^5} x \cos [c+d x]^5 \left( 6 \cos [c]^3-6 \cos [c]^5-24 i \cos [c]^2 \sin [c]+ \right. \\
 & \quad \left. 36 i \cos [c]^4 \sin [c]-36 \cos [c] \sin [c]^2+90 \cos [c]^3 \sin [c]^2+24 i \sin [c]^3- \right. \\
 & \quad \left. 120 i \cos [c]^2 \sin [c]^3-90 \cos [c] \sin [c]^4+36 i \sin [c]^5+6 \sin [c]^3 \tan [c]+ \right. \\
 & \quad \left. 6 \sin [c]^5 \tan [c]-i (12 \cos [5 c]-12 i \sin [5 c]) \tan [c] \right) (a+i a \tan [c+d x])^5
 \end{aligned}$$

**Problem 67: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^8 (a+i a \tan [c+d x])^5 dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$- \frac{i a^9}{4 d (a-i a \tan [c+d x])^4}$$

Result (type 3, 73 leaves):

$$\frac{1}{64 d} a^5 \left( 10 \cos [c+d x]+5 \cos [3(c+d x)]-i (2 \sin [c+d x]+3 \sin [3(c+d x)]) \right) \left( -i \cos [5(c+d x)]+\sin [5(c+d x)] \right)$$

**Problem 77: Result more than twice size of optimal antiderivative.**

$$\int \sec [c+d x]^8 (a+i a \tan [c+d x])^8 dx$$

Optimal (type 3, 109 leaves, 3 steps):

$$\begin{aligned}
 & - \frac{2 i (a + i a \tan [c + d x])^{12}}{3 a^4 d} + \frac{12 i (a + i a \tan [c + d x])^{13}}{13 a^5 d} - \\
 & \frac{3 i (a + i a \tan [c + d x])^{14}}{7 a^6 d} + \frac{i (a + i a \tan [c + d x])^{15}}{15 a^7 d}
 \end{aligned}$$

Result (type 3, 245 leaves):

$$\begin{aligned}
 & \frac{1}{10920 d} a^8 \sec [c] \sec [c + d x]^{15} \\
 & \left( 6435 i \cos [d x] + 6435 i \cos [2 c + d x] + 5005 i \cos [2 c + 3 d x] + 5005 i \cos [4 c + 3 d x] + \right. \\
 & \quad 3003 i \cos [4 c + 5 d x] + 3003 i \cos [6 c + 5 d x] + 1365 i \cos [6 c + 7 d x] + 1365 i \cos [8 c + 7 d x] + \\
 & \quad 6435 \sin [d x] - 6435 \sin [2 c + d x] + 5005 \sin [2 c + 3 d x] - 5005 \sin [4 c + 3 d x] + \\
 & \quad 3003 \sin [4 c + 5 d x] - 3003 \sin [6 c + 5 d x] + 1365 \sin [6 c + 7 d x] - 1365 \sin [8 c + 7 d x] + \\
 & \quad \left. 910 \sin [8 c + 9 d x] + 210 \sin [10 c + 11 d x] + 30 \sin [12 c + 13 d x] + 2 \sin [14 c + 15 d x] \right)
 \end{aligned}$$

**Problem 78: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^6 (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 82 leaves, 3 steps):

$$- \frac{4 i (a + i a \tan [c + d x])^{11}}{11 a^3 d} + \frac{i (a + i a \tan [c + d x])^{12}}{3 a^4 d} - \frac{i (a + i a \tan [c + d x])^{13}}{13 a^5 d}$$

Result (type 3, 234 leaves):

$$\begin{aligned}
 & \frac{1}{1716 d} a^8 \sec [c] \sec [c + d x]^{13} \\
 & \left( 1716 i \cos [d x] + 1716 i \cos [2 c + d x] + 1287 i \cos [2 c + 3 d x] + 1287 i \cos [4 c + 3 d x] + \right. \\
 & \quad 715 i \cos [4 c + 5 d x] + 715 i \cos [6 c + 5 d x] + 286 i \cos [6 c + 7 d x] + \\
 & \quad 286 i \cos [8 c + 7 d x] + 1716 \sin [d x] - 1716 \sin [2 c + d x] + 1287 \sin [2 c + 3 d x] - \\
 & \quad 1287 \sin [4 c + 3 d x] + 715 \sin [4 c + 5 d x] - 715 \sin [6 c + 5 d x] + 286 \sin [6 c + 7 d x] - \\
 & \quad \left. 286 \sin [8 c + 7 d x] + 156 \sin [8 c + 9 d x] + 26 \sin [10 c + 11 d x] + 2 \sin [12 c + 13 d x] \right)
 \end{aligned}$$

**Problem 79: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^4 (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 55 leaves, 3 steps):

$$- \frac{i (a + i a \tan [c + d x])^{10}}{5 a^2 d} + \frac{i (a + i a \tan [c + d x])^{11}}{11 a^3 d}$$

Result (type 3, 223 leaves):

$$\frac{1}{220 d} a^8 \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^{11} \left( 462 \operatorname{Cos}[d x] + 462 \operatorname{Cos}[2 c+d x] + 330 \operatorname{Cos}[2 c+3 d x] + 330 \operatorname{Cos}[4 c+3 d x] + 165 \operatorname{Cos}[4 c+5 d x] + 165 \operatorname{Cos}[6 c+5 d x] + 55 \operatorname{Cos}[6 c+7 d x] + 55 \operatorname{Cos}[8 c+7 d x] + 462 \operatorname{Sin}[d x] - 462 \operatorname{Sin}[2 c+d x] + 330 \operatorname{Sin}[2 c+3 d x] - 330 \operatorname{Sin}[4 c+3 d x] + 165 \operatorname{Sin}[4 c+5 d x] - 165 \operatorname{Sin}[6 c+5 d x] + 55 \operatorname{Sin}[6 c+7 d x] - 55 \operatorname{Sin}[8 c+7 d x] + 22 \operatorname{Sin}[8 c+9 d x] + 2 \operatorname{Sin}[10 c+11 d x] \right)$$

**Problem 80: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^2 (a+i a \operatorname{Tan}[c+d x])^8 dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$-\frac{i (a+i a \operatorname{Tan}[c+d x])^9}{9 a d}$$

Result (type 3, 212 leaves):

$$\frac{1}{18 d} a^8 \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^9 \left( 126 \operatorname{Cos}[d x] + 126 \operatorname{Cos}[2 c+d x] + 84 \operatorname{Cos}[2 c+3 d x] + 84 \operatorname{Cos}[4 c+3 d x] + 36 \operatorname{Cos}[4 c+5 d x] + 36 \operatorname{Cos}[6 c+5 d x] + 9 \operatorname{Cos}[6 c+7 d x] + 9 \operatorname{Cos}[8 c+7 d x] + 126 \operatorname{Sin}[d x] - 126 \operatorname{Sin}[2 c+d x] + 84 \operatorname{Sin}[2 c+3 d x] - 84 \operatorname{Sin}[4 c+3 d x] + 36 \operatorname{Sin}[4 c+5 d x] - 36 \operatorname{Sin}[6 c+5 d x] + 9 \operatorname{Sin}[6 c+7 d x] - 9 \operatorname{Sin}[8 c+7 d x] + 2 \operatorname{Sin}[8 c+9 d x] \right)$$

**Problem 82: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+d x]^2 (a+i a \operatorname{Tan}[c+d x])^8 dx$$

Optimal (type 3, 133 leaves, 3 steps):

$$-192 a^8 x + \frac{192 i a^8 \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d} + \frac{129 a^8 \operatorname{Tan}[c+d x]}{d} + \frac{36 i a^8 \operatorname{Tan}[c+d x]^2}{d} - \frac{10 a^8 \operatorname{Tan}[c+d x]^3}{d} - \frac{2 i a^8 \operatorname{Tan}[c+d x]^4}{d} + \frac{a^8 \operatorname{Tan}[c+d x]^5}{5 d} - \frac{64 i a^9}{d (a-i a \operatorname{Tan}[c+d x])}$$

Result (type 3, 912 leaves):

$$\begin{aligned}
 & - \frac{192 x \cos [8 c] \cos [c+d x]^8 (a+i a \tan [c+d x])^8}{(\cos [d x]+i \sin [d x])^8} + \\
 & \frac{96 i \cos [8 c] \cos [c+d x]^8 \log [\cos [c+d x]^2] (a+i a \tan [c+d x])^8}{d (\cos [d x]+i \sin [d x])^8} + \\
 & \left( \cos [2 d x] \cos [c+d x]^8 (-32 i \cos [6 c]-32 \sin [6 c]) (a+i a \tan [c+d x])^8 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^8 \right) + \left( \cos [c+d x]^4 \sec [c] (10 \cos [c]+i \sin [c]) \right. \\
 & \left. \left( -\frac{1}{5} i \cos [8 c]-\frac{1}{5} \sin [8 c] \right) (a+i a \tan [c+d x])^8 \right) / \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \left( \cos [c+d x]^6 \sec [c] (50 \cos [c]+13 i \sin [c]) \left( \frac{4}{5} i \cos [8 c]+\frac{4}{5} \sin [8 c] \right) \right. \\
 & \left. (a+i a \tan [c+d x])^8 \right) / \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \frac{192 i x \cos [c+d x]^8 \sin [8 c] (a+i a \tan [c+d x])^8}{(\cos [d x]+i \sin [d x])^8} + \\
 & \frac{96 \cos [c+d x]^8 \log [\cos [c+d x]^2] \sin [8 c] (a+i a \tan [c+d x])^8}{d (\cos [d x]+i \sin [d x])^8} + \\
 & \left( \cos [c+d x]^3 \sec [c] \left( \frac{1}{5} \cos [8 c]-\frac{1}{5} i \sin [8 c] \right) \sin [d x] (a+i a \tan [c+d x])^8 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \left( \cos [c+d x]^5 \sec [c] \left( -\frac{52}{5} \cos [8 c]+\frac{52}{5} i \sin [8 c] \right) \sin [d x] (a+i a \tan [c+d x])^8 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \left( \cos [c+d x]^7 \sec [c] \left( \frac{696}{5} \cos [8 c]-\frac{696}{5} i \sin [8 c] \right) \sin [d x] (a+i a \tan [c+d x])^8 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \left( \cos [c+d x]^8 (32 \cos [6 c]-32 i \sin [6 c]) \sin [2 d x] (a+i a \tan [c+d x])^8 \right) / \\
 & \left( d (\cos [d x]+i \sin [d x])^8 \right) + \\
 & \frac{1}{(\cos [d x]+i \sin [d x])^8} x \cos [c+d x]^8 \left( 96 \cos [c]^6-96 \cos [c]^8-672 i \cos [c]^5 \sin [c]+ \right. \\
 & \quad 864 i \cos [c]^7 \sin [c]-2016 \cos [c]^4 \sin [c]^2+3456 \cos [c]^6 \sin [c]^2+ \\
 & \quad 3360 i \cos [c]^3 \sin [c]^3-8064 i \cos [c]^5 \sin [c]^3+3360 \cos [c]^2 \sin [c]^4- \\
 & \quad 12096 \cos [c]^4 \sin [c]^4-2016 i \cos [c] \sin [c]^5+12096 i \cos [c]^3 \sin [c]^5-672 \sin [c]^6+ \\
 & \quad 8064 \cos [c]^2 \sin [c]^6-3456 i \cos [c] \sin [c]^7-864 \sin [c]^8+96 i \sin [c]^6 \tan [c]+ \\
 & \quad \left. 96 i \sin [c]^8 \tan [c]-i (192 \cos [8 c]-192 i \sin [8 c]) \tan [c] \right) (a+i a \tan [c+d x])^8
 \end{aligned}$$

**Problem 83: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 (a+i a \tan [c+d x])^8 dx$$

Optimal (type 3, 124 leaves, 3 steps):

$$80 a^8 x - \frac{80 i a^8 \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{31 a^8 \operatorname{Tan}[c + d x]}{d} - \frac{4 i a^8 \operatorname{Tan}[c + d x]^2}{d} +$$

$$\frac{a^8 \operatorname{Tan}[c + d x]^3}{3 d} - \frac{16 i a^{10}}{d (a - i a \operatorname{Tan}[c + d x])^2} + \frac{80 i a^9}{d (a - i a \operatorname{Tan}[c + d x])}$$

Result (type 3, 566 leaves):

$$\frac{1}{12 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8} a^8 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (\operatorname{Cos}[2 (c + 5 d x)] + i \operatorname{Sin}[2 (c + 5 d x)])$$

$$(-66 i \operatorname{Cos}[2 c + 3 d x] + 180 d x \operatorname{Cos}[2 c + 3 d x] + 75 i \operatorname{Cos}[4 c + 3 d x] +$$

$$180 d x \operatorname{Cos}[4 c + 3 d x] - 50 i \operatorname{Cos}[4 c + 5 d x] + 60 d x \operatorname{Cos}[4 c + 5 d x] - 3 i \operatorname{Cos}[6 c + 5 d x] +$$

$$60 d x \operatorname{Cos}[6 c + 5 d x] + 3 \operatorname{Cos}[2 c + d x] (71 i + 80 d x - 40 i \operatorname{Log}[\operatorname{Cos}[c + d x]^2])) +$$

$$\operatorname{Cos}[d x] (119 i + 240 d x - 120 i \operatorname{Log}[\operatorname{Cos}[c + d x]^2])) -$$

$$90 i \operatorname{Cos}[2 c + 3 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 90 i \operatorname{Cos}[4 c + 3 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] -$$

$$30 i \operatorname{Cos}[4 c + 5 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 30 i \operatorname{Cos}[6 c + 5 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] -$$

$$101 \operatorname{Sin}[d x] - 120 i d x \operatorname{Sin}[d x] - 60 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[d x] +$$

$$87 \operatorname{Sin}[2 c + d x] - 120 i d x \operatorname{Sin}[2 c + d x] - 60 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[2 c + d x] -$$

$$96 \operatorname{Sin}[2 c + 3 d x] - 180 i d x \operatorname{Sin}[2 c + 3 d x] - 90 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[2 c + 3 d x] +$$

$$45 \operatorname{Sin}[4 c + 3 d x] - 180 i d x \operatorname{Sin}[4 c + 3 d x] - 90 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[4 c + 3 d x] -$$

$$44 \operatorname{Sin}[4 c + 5 d x] - 60 i d x \operatorname{Sin}[4 c + 5 d x] - 30 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[4 c + 5 d x] +$$

$$3 \operatorname{Sin}[6 c + 5 d x] - 60 i d x \operatorname{Sin}[6 c + 5 d x] - 30 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[6 c + 5 d x])$$

### Problem 84: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x]^6 (a + i a \operatorname{Tan}[c + d x])^8 dx$$

Optimal (type 3, 114 leaves, 3 steps):

$$-8 a^8 x + \frac{8 i a^8 \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} + \frac{a^8 \operatorname{Tan}[c + d x]}{d} -$$

$$\frac{16 i a^{11}}{3 d (a - i a \operatorname{Tan}[c + d x])^3} + \frac{16 i a^{10}}{d (a - i a \operatorname{Tan}[c + d x])^2} - \frac{24 i a^9}{d (a - i a \operatorname{Tan}[c + d x])}$$

Result (type 3, 414 leaves):

$$-\frac{1}{6 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8}$$

$$a^8 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (12 i \operatorname{Cos}[c] + 10 i \operatorname{Cos}[3 c + 2 d x] + 12 d x \operatorname{Cos}[3 c + 2 d x] -$$

$$2 i \operatorname{Cos}[3 c + 4 d x] + 12 d x \operatorname{Cos}[3 c + 4 d x] + i \operatorname{Cos}[5 c + 4 d x] + 12 d x \operatorname{Cos}[5 c + 4 d x] +$$

$$\operatorname{Cos}[c + 2 d x] (7 i + 12 d x - 6 i \operatorname{Log}[\operatorname{Cos}[c + d x]^2])) - 6 i \operatorname{Cos}[3 c + 2 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] -$$

$$6 i \operatorname{Cos}[3 c + 4 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 6 i \operatorname{Cos}[5 c + 4 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] +$$

$$11 \operatorname{Sin}[c + 2 d x] - 12 i d x \operatorname{Sin}[c + 2 d x] - 6 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[c + 2 d x] +$$

$$14 \operatorname{Sin}[3 c + 2 d x] - 12 i d x \operatorname{Sin}[3 c + 2 d x] - 6 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[3 c + 2 d x] -$$

$$4 \operatorname{Sin}[3 c + 4 d x] - 12 i d x \operatorname{Sin}[3 c + 4 d x] - 6 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[3 c + 4 d x] -$$

$$\operatorname{Sin}[5 c + 4 d x] - 12 i d x \operatorname{Sin}[5 c + 4 d x] - 6 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[5 c + 4 d x])$$

$$(\operatorname{Cos}[3 c + 11 d x] + i \operatorname{Sin}[3 c + 11 d x])$$

### Problem 88: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^{14} (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$-\frac{i a^{15}}{7 d (a - i a \tan [c + d x])^7}$$

Result (type 3, 116 leaves):

$$\begin{aligned} & (a^8 (35 + 56 \cos [2 (c + d x)] + 28 \cos [4 (c + d x)] + 8 \cos [6 (c + d x)] - \\ & \quad 14 i \sin [2 (c + d x)] - 14 i \sin [4 (c + d x)] - 6 i \sin [6 (c + d x)]) \\ & (-i \cos [8 (c + 2 d x)] + \sin [8 (c + 2 d x)]) \Big/ (896 d (\cos [d x] + i \sin [d x])^8) \end{aligned}$$

### Problem 92: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^3 (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 205 leaves, 7 steps):

$$\begin{aligned} & \frac{1155 a^8 \operatorname{ArcTanh}[\sin [c + d x]]}{8 d} + \frac{1155 i a^8 \operatorname{Sec}[c + d x]}{8 d} + \frac{22 i a^3 \cos [c + d x] (a + i a \tan [c + d x])^5}{3 d} \\ & \frac{2 i a \cos [c + d x]^3 (a + i a \tan [c + d x])^7}{3 d} + \frac{33 i a^2 \operatorname{Sec}[c + d x] (a^2 + i a^2 \tan [c + d x])^3}{4 d} + \\ & \frac{77 i \operatorname{Sec}[c + d x] (a^4 + i a^4 \tan [c + d x])^2}{4 d} + \frac{385 i \operatorname{Sec}[c + d x] (a^8 + i a^8 \tan [c + d x])}{8 d} \end{aligned}$$

Result (type 3, 1540 leaves):

$$\begin{aligned} & - \left( \left( 1155 \cos [8 c] \cos [c + d x]^8 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] (a + i a \tan [c + d x])^8 \right) \Big/ \right. \\ & \quad \left. (8 d (\cos [d x] + i \sin [d x])^8) \right) + \\ & \left( 1155 \cos [8 c] \cos [c + d x]^8 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] (a + i a \tan [c + d x])^8 \right) \Big/ \\ & \quad (8 d (\cos [d x] + i \sin [d x])^8) + \\ & \left( \cos [3 d x] \cos [c + d x]^8 \left( -\frac{32}{3} i \cos [5 c] - \frac{32}{3} \sin [5 c] \right) (a + i a \tan [c + d x])^8 \right) \Big/ \\ & \quad (d (\cos [d x] + i \sin [d x])^8) + \\ & \left( \cos [d x] \cos [c + d x]^8 (160 i \cos [7 c] + 160 \sin [7 c]) (a + i a \tan [c + d x])^8 \right) \Big/ \\ & \quad (d (\cos [d x] + i \sin [d x])^8) + \\ & \left( 1155 i \cos [c + d x]^8 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sin [8 c] (a + i a \tan [c + d x])^8 \right) \Big/ \\ & \quad (8 d (\cos [d x] + i \sin [d x])^8) - \end{aligned}$$

$$\begin{aligned}
& \left( 1155 \operatorname{Im} \cos [c+d x]^8 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sin [8 c] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( 8 d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \right) + \\
& \left( \cos [c+d x]^8 \operatorname{Sec} [c] \left( \frac{236}{3} \operatorname{Im} \cos [8 c] + \frac{236}{3} \sin [8 c] \right) (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \right) + \\
& \left( \cos [c+d x]^8 (-160 \cos [7 c] + 160 \operatorname{Im} \sin [7 c]) \sin [d x] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \right) + \\
& \left( \cos [c+d x]^8 \left( \frac{32}{3} \cos [5 c] - \frac{32}{3} \operatorname{Im} \sin [5 c] \right) \sin [3 d x] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \right) + \frac{\cos [c+d x]^8 \left( \frac{1}{16} \cos [8 c] - \frac{1}{16} \operatorname{Im} \sin [8 c] \right) (a + \operatorname{Im} a \tan [c+d x])^8}{d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^4} - \\
& \left( \operatorname{Im} \cos [c+d x]^8 \left( \frac{4}{3} \cos [8 c] - \frac{4}{3} \operatorname{Im} \sin [8 c] \right) \sin \left[ \frac{d x}{2} \right] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^8 \left( (-375 - 32 \operatorname{Im}) \cos \left[ \frac{c}{2} \right] + (375 - 32 \operatorname{Im}) \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \frac{1}{48} \cos [8 c] - \frac{1}{48} \operatorname{Im} \sin [8 c] \right) (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \operatorname{Im} \cos [c+d x]^8 \left( \frac{236}{3} \cos [8 c] - \frac{236}{3} \operatorname{Im} \sin [8 c] \right) \sin \left[ \frac{d x}{2} \right] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
& \frac{\cos [c+d x]^8 \left( -\frac{1}{16} \cos [8 c] + \frac{1}{16} \operatorname{Im} \sin [8 c] \right) (a + \operatorname{Im} a \tan [c+d x])^8}{d (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^4} + \\
& \left( \operatorname{Im} \cos [c+d x]^8 \left( \frac{4}{3} \cos [8 c] - \frac{4}{3} \operatorname{Im} \sin [8 c] \right) \sin \left[ \frac{d x}{2} \right] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^8 \left( (375 - 32 \operatorname{Im}) \cos \left[ \frac{c}{2} \right] + (375 + 32 \operatorname{Im}) \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \frac{1}{48} \cos [8 c] - \frac{1}{48} \operatorname{Im} \sin [8 c] \right) (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) - \\
& \left( \operatorname{Im} \cos [c+d x]^8 \left( \frac{236}{3} \cos [8 c] - \frac{236}{3} \operatorname{Im} \sin [8 c] \right) \sin \left[ \frac{d x}{2} \right] (a + \operatorname{Im} a \tan [c+d x])^8 \right) / \\
& \left( d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) (\cos [d x] + \operatorname{Im} \sin [d x])^8 \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
\end{aligned}$$



Problem 93: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 173 leaves, 6 steps):

$$\begin{aligned} & - \frac{63 a^8 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} - \frac{63 i a^8 \operatorname{Sec}[c + d x]}{2 d} + \\ & \frac{6 i a^3 \cos [c + d x]^3 (a + i a \tan [c + d x])^5}{5 d} - \frac{2 i a \cos [c + d x]^5 (a + i a \tan [c + d x])^7}{5 d} - \\ & \frac{42 i a^2 \cos [c + d x] (a^2 + i a^2 \tan [c + d x])^3}{5 d} - \frac{21 i \operatorname{Sec}[c + d x] (a^8 + i a^8 \tan [c + d x])}{2 d} \end{aligned}$$

Result (type 3, 1162 leaves):

$$\begin{aligned}
 & \left( 63 \operatorname{Cos}[8c] \operatorname{Cos}[c+dx]^8 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( 2d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) - \\
 & \left( 63 \operatorname{Cos}[8c] \operatorname{Cos}[c+dx]^8 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( 2d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[5dx] \operatorname{Cos}[c+dx]^8 \left( -\frac{8}{5} i \operatorname{Cos}[3c] - \frac{8}{5} \operatorname{Sin}[3c] \right) (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[3dx] \operatorname{Cos}[c+dx]^8 (8 i \operatorname{Cos}[5c] + 8 \operatorname{Sin}[5c]) (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[dx] \operatorname{Cos}[c+dx]^8 (-48 i \operatorname{Cos}[7c] - 48 \operatorname{Sin}[7c]) (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[c+dx]^8 \operatorname{Sec}[c] (-8 i \operatorname{Cos}[8c] - 8 \operatorname{Sin}[8c]) (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) - \\
 & \left( 63 i \operatorname{Cos}[c+dx]^8 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sin}[8c] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( 2d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( 63 i \operatorname{Cos}[c+dx]^8 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sin}[8c] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( 2d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[c+dx]^8 (48 \operatorname{Cos}[7c] - 48 i \operatorname{Sin}[7c]) \operatorname{Sin}[dx] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[c+dx]^8 (-8 \operatorname{Cos}[5c] + 8 i \operatorname{Sin}[5c]) \operatorname{Sin}[3dx] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \\
 & \left( \operatorname{Cos}[c+dx]^8 \left( \frac{8}{5} \operatorname{Cos}[3c] - \frac{8}{5} i \operatorname{Sin}[3c] \right) \operatorname{Sin}[5dx] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) + \frac{\operatorname{Cos}[c+dx]^8 \left( \frac{1}{4} \operatorname{Cos}[8c] - \frac{1}{4} i \operatorname{Sin}[8c] \right) (a + i a \operatorname{Tan}[c+dx])^8}{d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2} - \\
 & \left( i \operatorname{Cos}[c+dx]^8 (8 \operatorname{Cos}[8c] - 8 i \operatorname{Sin}[8c]) \operatorname{Sin}\left[\frac{dx}{2}\right] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) + \\
 & \frac{\operatorname{Cos}[c+dx]^8 \left( -\frac{1}{4} \operatorname{Cos}[8c] + \frac{1}{4} i \operatorname{Sin}[8c] \right) (a + i a \operatorname{Tan}[c+dx])^8}{d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2} + \\
 & \left( i \operatorname{Cos}[c+dx]^8 (8 \operatorname{Cos}[8c] - 8 i \operatorname{Sin}[8c]) \operatorname{Sin}\left[\frac{dx}{2}\right] (a + i a \operatorname{Tan}[c+dx])^8 \right) / \\
 & \quad \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right)
 \end{aligned}$$

**Problem 94: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^7 (a + i a \tan [c + d x])^8 dx$$

Optimal (type 3, 152 leaves, 5 steps):

$$\frac{a^8 \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{2 i a^3 \cos [c + d x]^5 (a + i a \tan [c + d x])^5}{5 d} -$$

$$\frac{2 i a \cos [c + d x]^7 (a + i a \tan [c + d x])^7}{7 d} -$$

$$\frac{2 i a^2 \cos [c + d x]^3 (a^2 + i a^2 \tan [c + d x])^3}{3 d} + \frac{2 i \cos [c + d x] (a^8 + i a^8 \tan [c + d x])}{d}$$

Result (type 3, 305 leaves):

$$\frac{1}{105 d (\cos [d x] + i \sin [d x])^8}$$

$$a^8 \left( -70 i \cos \left[ \frac{1}{2} (c + d x) \right] + 42 i \cos \left[ \frac{3}{2} (c + d x) \right] + 210 i \cos \left[ \frac{5}{2} (c + d x) \right] - \right.$$

$$30 i \cos \left[ \frac{7}{2} (c + d x) \right] - 105 \cos \left[ \frac{7}{2} (c + d x) \right] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] +$$

$$105 \cos \left[ \frac{7}{2} (c + d x) \right] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 70 \sin \left[ \frac{1}{2} (c + d x) \right] -$$

$$42 \sin \left[ \frac{3}{2} (c + d x) \right] + 210 \sin \left[ \frac{5}{2} (c + d x) \right] + 30 \sin \left[ \frac{7}{2} (c + d x) \right] +$$

$$105 i \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sin \left[ \frac{7}{2} (c + d x) \right] -$$

$$105 i \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sin \left[ \frac{7}{2} (c + d x) \right] \left. \right)$$

$$\left( \cos \left[ \frac{1}{2} (7 c + 23 d x) \right] + i \sin \left[ \frac{1}{2} (7 c + 23 d x) \right] \right)$$

**Problem 116: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^6}{(a + i a \tan [c + d x])^2} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{i (a - i a \tan [c + d x])^3}{3 a^5 d}$$

Result (type 3, 68 leaves):

$$\frac{1}{6 a^2 d} \sec [c] \sec [c + d x]^3$$

$$(-3 i \cos [d x] - 3 i \cos [2 c + d x] + 3 \sin [d x] - 3 \sin [2 c + d x] + 2 \sin [2 c + 3 d x])$$

### Problem 122: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + d x]^9}{(a + i a \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 124 leaves, 5 steps):

$$\frac{7 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{16 a^2 d} + \frac{7 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{16 a^2 d} + \frac{7 \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{24 a^2 d} + \frac{7 \operatorname{Sec}[c + d x]^5 \operatorname{Tan}[c + d x]}{30 a^2 d} - \frac{2 i \operatorname{Sec}[c + d x]^7}{5 d (a^2 + i a^2 \operatorname{Tan}[c + d x])}$$

Result (type 3, 294 leaves):

$$-\frac{1}{7680 a^2 d} \operatorname{Sec}[c + d x]^6 \left( 3072 i \operatorname{Cos}[c + d x] + 5 \left( 210 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 21 \operatorname{Cos}[6(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 315 \operatorname{Cos}[2(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + 126 \operatorname{Cos}[4(c + d x)] \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + 21 \operatorname{Cos}[6(c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 60 \operatorname{Sin}[c + d x] - 238 \operatorname{Sin}[3(c + d x)] - 42 \operatorname{Sin}[5(c + d x)] \right)$$

### Problem 123: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + d x]^7}{(a + i a \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 100 leaves, 4 steps):

$$\frac{5 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 a^2 d} + \frac{5 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{8 a^2 d} + \frac{5 \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{12 a^2 d} - \frac{2 i \operatorname{Sec}[c + d x]^5}{3 d (a^2 + i a^2 \operatorname{Tan}[c + d x])}$$

Result (type 3, 215 leaves):

$$\begin{aligned}
 & - \frac{1}{192 a^2 d} \operatorname{Sec}[c + d x]^4 \\
 & \left( 128 i \operatorname{Cos}[c + d x] + 45 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 60 \operatorname{Cos}[2(c + d x)] \right. \\
 & \quad \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\
 & \quad 15 \operatorname{Cos}[4(c + d x)] \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \\
 & \quad \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) - \\
 & \quad \left. 45 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 18 \operatorname{Sin}[c + d x] - 30 \operatorname{Sin}[3(c + d x)] \right)
 \end{aligned}$$

**Problem 125: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3}{(a + i a \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 48 leaves, 2 steps):

$$- \frac{\operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{a^2 d} + \frac{2 i \operatorname{Sec}[c + d x]}{d (a^2 + i a^2 \operatorname{Tan}[c + d x])}$$

Result (type 3, 184 leaves):

$$\begin{aligned}
 & - \left( \left( \operatorname{Sec}[c + d x]^2 \right. \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \left( 2 i + \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \left( 2 + i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \\
 & \quad \quad \left. i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{3}{2}(c + d x)\right] + i \operatorname{Sin}\left[\frac{3}{2}(c + d x)\right] \right) \right) / \left( a^2 d (-i + \operatorname{Tan}[c + d x])^2 \right)
 \end{aligned}$$

**Problem 133: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^8}{(a + i a \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{i (a - i a \operatorname{Tan}[c + d x])^4}{4 a^7 d}$$

Result (type 3, 84 leaves):

$$\frac{1}{4 a^3 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \left( -3 \operatorname{Im} \operatorname{Cos}[c] - 2 \operatorname{Im} \operatorname{Cos}[c+2 d x] - 2 \operatorname{Im} \operatorname{Cos}[3 c+2 d x] - 3 \operatorname{Sin}[c] + 2 \operatorname{Sin}[c+2 d x] - 2 \operatorname{Sin}[3 c+2 d x] + \operatorname{Sin}[3 c+4 d x] \right)$$

**Problem 149: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^{12}}{(a+\operatorname{Im} a \operatorname{Tan}[c+d x])^4} dx$$

Optimal (type 3, 55 leaves, 3 steps):

$$\frac{\operatorname{Im} (a-\operatorname{Im} a \operatorname{Tan}[c+d x])^6}{3 a^{10} d} - \frac{\operatorname{Im} (a-\operatorname{Im} a \operatorname{Tan}[c+d x])^7}{7 a^{11} d}$$

Result (type 3, 127 leaves):

$$\frac{1}{84 a^4 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^7 \left( -35 \operatorname{Im} \operatorname{Cos}[d x] - 35 \operatorname{Im} \operatorname{Cos}[2 c+d x] - 21 \operatorname{Im} \operatorname{Cos}[2 c+3 d x] - 21 \operatorname{Im} \operatorname{Cos}[4 c+3 d x] + 35 \operatorname{Sin}[d x] - 35 \operatorname{Sin}[2 c+d x] + 21 \operatorname{Sin}[2 c+3 d x] - 21 \operatorname{Sin}[4 c+3 d x] + 14 \operatorname{Sin}[4 c+5 d x] + 2 \operatorname{Sin}[6 c+7 d x] \right)$$

**Problem 150: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^{10}}{(a+\operatorname{Im} a \operatorname{Tan}[c+d x])^4} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{\operatorname{Im} (a-\operatorname{Im} a \operatorname{Tan}[c+d x])^5}{5 a^9 d}$$

Result (type 3, 116 leaves):

$$\frac{1}{10 a^4 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^5 \left( -10 \operatorname{Im} \operatorname{Cos}[d x] - 10 \operatorname{Im} \operatorname{Cos}[2 c+d x] - 5 \operatorname{Im} \operatorname{Cos}[2 c+3 d x] - 5 \operatorname{Im} \operatorname{Cos}[4 c+3 d x] + 10 \operatorname{Sin}[d x] - 10 \operatorname{Sin}[2 c+d x] + 5 \operatorname{Sin}[2 c+3 d x] - 5 \operatorname{Sin}[4 c+3 d x] + 2 \operatorname{Sin}[4 c+5 d x] \right)$$

**Problem 152: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^6}{(a+\operatorname{Im} a \operatorname{Tan}[c+d x])^4} dx$$

Optimal (type 3, 63 leaves, 3 steps):

$$-\frac{4 x}{a^4} - \frac{4 \operatorname{Im} \operatorname{Log}[\operatorname{Cos}[c+d x]]}{a^4 d} + \frac{\operatorname{Tan}[c+d x]}{a^4 d} + \frac{4 \operatorname{Im}}{d (a^4 + \operatorname{Im} a^4 \operatorname{Tan}[c+d x])}$$

Result (type 3, 214 leaves):

$$\frac{1}{2 a^4 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \left(-\operatorname{Cos}[c+d x]+i \operatorname{Sin}[c+d x]\right) \\ \left(-i \operatorname{Cos}[3 c+2 d x]+2 d x \operatorname{Cos}[3 c+2 d x]+2 \operatorname{Cos}[c+2 d x] \left(d x+i \operatorname{Log}[\operatorname{Cos}[c+d x]]\right)+\right. \\ \left.\operatorname{Cos}[c] \left(-3 i+4 d x+4 i \operatorname{Log}[\operatorname{Cos}[c+d x]]\right)+2 i \operatorname{Cos}[3 c+2 d x] \operatorname{Log}[\operatorname{Cos}[c+d x]]+\right. \\ \left.\operatorname{Sin}[c]-2 \operatorname{Sin}[c+2 d x]+2 i d x \operatorname{Sin}[c+2 d x]-2 \operatorname{Log}[\operatorname{Cos}[c+d x]] \operatorname{Sin}[c+2 d x]-\right. \\ \left.\operatorname{Sin}[3 c+2 d x]+2 i d x \operatorname{Sin}[3 c+2 d x]-2 \operatorname{Log}[\operatorname{Cos}[c+d x]] \operatorname{Sin}[3 c+2 d x]\right)$$

**Problem 154: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^2}{\left(a+i a \operatorname{Tan}[c+d x]\right)^4} d x$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{i}{3 a d \left(a+i a \operatorname{Tan}[c+d x]\right)^3}$$

Result (type 3, 56 leaves):

$$\frac{i \operatorname{Sec}[c+d x]^4 \left(3+4 \operatorname{Cos}\left[2(c+d x)\right]+2 i \operatorname{Sin}\left[2(c+d x)\right]\right)}{24 a^4 d \left(-i+\operatorname{Tan}[c+d x]\right)^4}$$

**Problem 159: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^7}{\left(a+i a \operatorname{Tan}[c+d x]\right)^4} d x$$

Optimal (type 3, 107 leaves, 4 steps):

$$-\frac{15 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 a^4 d}-\frac{15 \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 a^4 d}+ \\ \frac{2 i \operatorname{Sec}[c+d x]^5}{a d \left(a+i a \operatorname{Tan}[c+d x]\right)^3}+\frac{10 i \operatorname{Sec}[c+d x]^3}{d \left(a^4+i a^4 \operatorname{Tan}[c+d x]\right)}$$

Result (type 3, 988 leaves):

$$\begin{aligned}
 & \left( 15 \operatorname{Cos}[4c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c+dx]^4 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c+dx])^4 \right) - \\
 & \left( 15 \operatorname{Cos}[4c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c+dx]^4 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( \operatorname{Cos}[dx] \operatorname{Sec}[c+dx]^4 (8i \operatorname{Cos}[3c] - 8 \operatorname{Sin}[3c]) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 (4i \operatorname{Cos}[4c] - 4 \operatorname{Sin}[4c]) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( 15i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c+dx]^4 \operatorname{Sin}[4c] (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c+dx])^4 \right) - \\
 & \left( 15i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c+dx]^4 \operatorname{Sin}[4c] (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( \operatorname{Sec}[c+dx]^4 (8 \operatorname{Cos}[3c] + 8i \operatorname{Sin}[3c]) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \operatorname{Sin}[dx] \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c+dx])^4 \right) + \frac{\operatorname{Sec}[c+dx]^4 \left( \frac{1}{4} \operatorname{Cos}[4c] + \frac{1}{4}i \operatorname{Sin}[4c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4}{d \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 (a + i a \operatorname{Tan}[c+dx])^4} + \\
 & \frac{\operatorname{Sec}[c+dx]^4 \left( -\frac{1}{4} \operatorname{Cos}[4c] - \frac{1}{4}i \operatorname{Sin}[4c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4}{d \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 (a + i a \operatorname{Tan}[c+dx])^4} + \\
 & \left( 4 \operatorname{Sec}[c+dx]^4 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right. \\
 & \left. \left( \frac{1}{2} \operatorname{Cos}\left[4c - \frac{dx}{2}\right] - \frac{1}{2} \operatorname{Cos}\left[4c + \frac{dx}{2}\right] + \frac{1}{2}i \operatorname{Sin}\left[4c - \frac{dx}{2}\right] - \frac{1}{2}i \operatorname{Sin}\left[4c + \frac{dx}{2}\right] \right) \right) / \\
 & \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right) (a + i a \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( 4 \operatorname{Sec}[c+dx]^4 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right. \\
 & \left. \left( -\frac{1}{2} \operatorname{Cos}\left[4c - \frac{dx}{2}\right] + \frac{1}{2} \operatorname{Cos}\left[4c + \frac{dx}{2}\right] - \frac{1}{2}i \operatorname{Sin}\left[4c - \frac{dx}{2}\right] + \frac{1}{2}i \operatorname{Sin}\left[4c + \frac{dx}{2}\right] \right) \right) / \\
 & \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right) (a + i a \operatorname{Tan}[c+dx])^4 \right)
 \end{aligned}$$

**Problem 160: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^5}{(a + i a \operatorname{Tan}[c+dx])^4} dx$$

Optimal (type 3, 82 leaves, 3 steps):



$$\frac{\text{ArcTanh}[\text{Sin}[c + d x]]}{a^4 d} + \frac{2 i \text{Sec}[c + d x]^3}{3 a d (a + i a \text{Tan}[c + d x])^3} - \frac{2 i \text{Sec}[c + d x]}{d (a^4 + i a^4 \text{Tan}[c + d x])}$$

Result (type 3, 247 leaves):

$$\frac{1}{3 a^4 d (-i + \text{Tan}[c + d x])^4} \text{Sec}[c + d x]^4 (\text{Cos}[d x] + i \text{Sin}[d x])^4 \left( -3 \text{Cos}[4 c] \text{Log} \left[ \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\ \left. 3 \text{Cos}[4 c] \text{Log} \left[ \text{Cos} \left[ \frac{1}{2} (c + d x) \right] + \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - 2 \text{Cos}[3 d x] \text{Sin}[c] + \right. \\ \left. 6 \text{Cos}[d x] \text{Sin}[3 c] - 3 i \text{Log} \left[ \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sin}[4 c] + \right. \\ \left. 3 i \text{Log} \left[ \text{Cos} \left[ \frac{1}{2} (c + d x) \right] + \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sin}[4 c] + \text{Cos}[3 c] (-6 i \text{Cos}[d x] - 6 \text{Sin}[d x]) - \right. \\ \left. 6 i \text{Sin}[3 c] \text{Sin}[d x] + 2 i \text{Sin}[c] \text{Sin}[3 d x] + 2 \text{Cos}[c] (i \text{Cos}[3 d x] + \text{Sin}[3 d x]) \right)$$

**Problem 166: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{14}}{(a + i a \text{Tan}[c + d x])^8} dx$$

Optimal (type 3, 134 leaves, 3 steps):

$$-\frac{192 x}{a^8} - \frac{192 i \text{Log}[\text{Cos}[c + d x]]}{a^8 d} + \frac{129 \text{Tan}[c + d x]}{a^8 d} - \frac{36 i \text{Tan}[c + d x]^2}{a^8 d} - \\ \frac{10 \text{Tan}[c + d x]^3}{a^8 d} + \frac{2 i \text{Tan}[c + d x]^4}{a^8 d} + \frac{\text{Tan}[c + d x]^5}{5 a^8 d} + \frac{64 i}{d (a^8 + i a^8 \text{Tan}[c + d x])}$$

Result (type 3, 599 leaves):

$$\frac{1}{20 a^8 d (-i + \text{Tan}[c + d x])^8} \text{Sec}[c] \text{Sec}[c + d x]^{13} (-\text{Cos}[7(c + d x)] - i \text{Sin}[7(c + d x)]) (-220 i \text{Cos}[3 c + 2 d x] + \\ 900 d x \text{Cos}[3 c + 2 d x] + 238 i \text{Cos}[3 c + 4 d x] + 360 d x \text{Cos}[3 c + 4 d x] - 110 i \text{Cos}[5 c + 4 d x] + \\ 360 d x \text{Cos}[5 c + 4 d x] + 77 i \text{Cos}[5 c + 6 d x] + 60 d x \text{Cos}[5 c + 6 d x] - 10 i \text{Cos}[7 c + 6 d x] + \\ 60 d x \text{Cos}[7 c + 6 d x] + 10 \text{Cos}[c] (-7 i + 120 d x + 120 i \text{Log}[\text{Cos}[c + d x]]) + \\ 5 \text{Cos}[c + 2 d x] (43 i + 180 d x + 180 i \text{Log}[\text{Cos}[c + d x]]) + \\ 900 i \text{Cos}[3 c + 2 d x] \text{Log}[\text{Cos}[c + d x]] + 360 i \text{Cos}[3 c + 4 d x] \text{Log}[\text{Cos}[c + d x]] + \\ 360 i \text{Cos}[5 c + 4 d x] \text{Log}[\text{Cos}[c + d x]] + 60 i \text{Cos}[5 c + 6 d x] \text{Log}[\text{Cos}[c + d x]] + \\ 60 i \text{Cos}[7 c + 6 d x] \text{Log}[\text{Cos}[c + d x]] + 870 \text{Sin}[c] - 985 \text{Sin}[c + 2 d x] + \\ 300 i d x \text{Sin}[c + 2 d x] - 300 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[c + 2 d x] + 320 \text{Sin}[3 c + 2 d x] + \\ 300 i d x \text{Sin}[3 c + 2 d x] - 300 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[3 c + 2 d x] - \\ 512 \text{Sin}[3 c + 4 d x] + 240 i d x \text{Sin}[3 c + 4 d x] - 240 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[3 c + 4 d x] + \\ 10 \text{Sin}[5 c + 4 d x] + 240 i d x \text{Sin}[5 c + 4 d x] - 240 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[5 c + 4 d x] - \\ 97 \text{Sin}[5 c + 6 d x] + 60 i d x \text{Sin}[5 c + 6 d x] - 60 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[5 c + 6 d x] - \\ 10 \text{Sin}[7 c + 6 d x] + 60 i d x \text{Sin}[7 c + 6 d x] - 60 \text{Log}[\text{Cos}[c + d x]] \text{Sin}[7 c + 6 d x])$$

### Problem 167: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{12}}{(a + i a \text{Tan}[c + d x])^8} dx$$

Optimal (type 3, 126 leaves, 3 steps):

$$\frac{80 x}{a^8} + \frac{80 i \text{Log}[\text{Cos}[c + d x]]}{a^8 d} - \frac{31 \text{Tan}[c + d x]}{a^8 d} + \frac{4 i \text{Tan}[c + d x]^2}{a^8 d} + \frac{\text{Tan}[c + d x]^3}{3 a^8 d} + \frac{16 i}{d (a^4 + i a^4 \text{Tan}[c + d x])^2} - \frac{80 i}{d (a^8 + i a^8 \text{Tan}[c + d x])}$$

Result (type 3, 537 leaves):

$$\frac{1}{12 a^8 d (-i + \text{Tan}[c + d x])^8} \text{Sec}[c] \text{Sec}[c + d x]^{11} (\text{Cos}[6(c + d x)] + i \text{Sin}[6(c + d x)])$$

$$\begin{aligned} & (66 i \text{Cos}[2c + 3dx] + 180 dx \text{Cos}[2c + 3dx] - 75 i \text{Cos}[4c + 3dx] + \\ & 180 dx \text{Cos}[4c + 3dx] + 50 i \text{Cos}[4c + 5dx] + 60 dx \text{Cos}[4c + 5dx] + 3 i \text{Cos}[6c + 5dx] + \\ & 60 dx \text{Cos}[6c + 5dx] + 3 \text{Cos}[2c + dx] (-71 i + 80 dx + 80 i \text{Log}[\text{Cos}[c + dx]]) + \\ & \text{Cos}[dx] (-119 i + 240 dx + 240 i \text{Log}[\text{Cos}[c + dx]]) + \\ & 180 i \text{Cos}[2c + 3dx] \text{Log}[\text{Cos}[c + dx]] + 180 i \text{Cos}[4c + 3dx] \text{Log}[\text{Cos}[c + dx]] + \\ & 60 i \text{Cos}[4c + 5dx] \text{Log}[\text{Cos}[c + dx]] + 60 i \text{Cos}[6c + 5dx] \text{Log}[\text{Cos}[c + dx]] - \\ & 101 \text{Sin}[dx] + 120 i dx \text{Sin}[dx] - 120 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[dx] + \\ & 87 \text{Sin}[2c + dx] + 120 i dx \text{Sin}[2c + dx] - 120 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[2c + dx] - \\ & 96 \text{Sin}[2c + 3dx] + 180 i dx \text{Sin}[2c + 3dx] - 180 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[2c + 3dx] + \\ & 45 \text{Sin}[4c + 3dx] + 180 i dx \text{Sin}[4c + 3dx] - 180 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[4c + 3dx] - \\ & 44 \text{Sin}[4c + 5dx] + 60 i dx \text{Sin}[4c + 5dx] - 60 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[4c + 5dx] + \\ & 3 \text{Sin}[6c + 5dx] + 60 i dx \text{Sin}[6c + 5dx] - 60 \text{Log}[\text{Cos}[c + dx]] \text{Sin}[6c + 5dx]) \end{aligned}$$

### Problem 168: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{10}}{(a + i a \text{Tan}[c + d x])^8} dx$$

Optimal (type 3, 116 leaves, 3 steps):

$$-\frac{8 x}{a^8} - \frac{8 i \text{Log}[\text{Cos}[c + d x]]}{a^8 d} + \frac{\text{Tan}[c + d x]}{a^8 d} + \frac{16 i}{3 a^5 d (a + i a \text{Tan}[c + d x])^3} - \frac{16 i}{d (a^4 + i a^4 \text{Tan}[c + d x])^2} + \frac{24 i}{d (a^8 + i a^8 \text{Tan}[c + d x])}$$

Result (type 3, 397 leaves):

$$\frac{1}{6 a^8 d (-i + \tan [c + d x])^8} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^9 \left( -\operatorname{Cos}[5(c + d x)] - i \operatorname{Sin}[5(c + d x)] \right) \\ \left( -12 i \operatorname{Cos}[c] - 10 i \operatorname{Cos}[3 c + 2 d x] + 12 d x \operatorname{Cos}[3 c + 2 d x] + 2 i \operatorname{Cos}[3 c + 4 d x] + \right. \\ \left. 12 d x \operatorname{Cos}[3 c + 4 d x] - i \operatorname{Cos}[5 c + 4 d x] + 12 d x \operatorname{Cos}[5 c + 4 d x] + \right. \\ \left. \operatorname{Cos}[c + 2 d x] (-7 i + 12 d x + 12 i \operatorname{Log}[\operatorname{Cos}[c + d x]]) + 12 i \operatorname{Cos}[3 c + 2 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]] + \right. \\ \left. 12 i \operatorname{Cos}[3 c + 4 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]] + 12 i \operatorname{Cos}[5 c + 4 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]] + \right. \\ \left. 11 \operatorname{Sin}[c + 2 d x] + 12 i d x \operatorname{Sin}[c + 2 d x] - 12 \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sin}[c + 2 d x] + \right. \\ \left. 14 \operatorname{Sin}[3 c + 2 d x] + 12 i d x \operatorname{Sin}[3 c + 2 d x] - 12 \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sin}[3 c + 2 d x] - \right. \\ \left. 4 \operatorname{Sin}[3 c + 4 d x] + 12 i d x \operatorname{Sin}[3 c + 4 d x] - 12 \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sin}[3 c + 4 d x] - \right. \\ \left. \operatorname{Sin}[5 c + 4 d x] + 12 i d x \operatorname{Sin}[5 c + 4 d x] - 12 \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sin}[5 c + 4 d x] \right)$$

**Problem 172: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^2}{(a + i a \tan [c + d x])^8} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{i}{7 a d (a + i a \tan [c + d x])^7}$$

Result (type 3, 100 leaves):

$$(i \operatorname{Sec}[c + d x]^8 \\ (35 + 56 \operatorname{Cos}[2(c + d x)] + 28 \operatorname{Cos}[4(c + d x)] + 8 \operatorname{Cos}[6(c + d x)] + 14 i \operatorname{Sin}[2(c + d x)] + \\ 14 i \operatorname{Sin}[4(c + d x)] + 6 i \operatorname{Sin}[6(c + d x)])) / (896 a^8 d (-i + \tan [c + d x])^8)$$

**Problem 176: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{13}}{(a + i a \tan [c + d x])^8} dx$$

Optimal (type 3, 205 leaves, 7 steps):

$$\frac{1155 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 a^8 d} + \frac{1155 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{8 a^8 d} + \\ \frac{385 \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{4 a^8 d} + \frac{2 i \operatorname{Sec}[c + d x]^{11}}{3 a d (a + i a \tan [c + d x])^7} - \\ \frac{22 i \operatorname{Sec}[c + d x]^9}{3 a^3 d (a + i a \tan [c + d x])^5} - \frac{66 i \operatorname{Sec}[c + d x]^7}{a^2 d (a^2 + i a^2 \tan [c + d x])^3} - \frac{154 i \operatorname{Sec}[c + d x]^5}{d (a^8 + i a^8 \tan [c + d x])}$$

Result (type 3, 1704 leaves):

$$- \left( \left( 1155 \operatorname{Cos}[8 c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^8 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \right. \\ \left. (8 d (a + i a \tan [c + d x])^8) \right) + \\ \left( 1155 \operatorname{Cos}[8 c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^8 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) /$$

$$\begin{aligned}
 & \left( 8 d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( \operatorname{Cos}[3 d x] \operatorname{Sec}[c + d x]^8 \left( \frac{32}{3} i \operatorname{Cos}[5 c] - \frac{32}{3} \operatorname{Sin}[5 c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( \operatorname{Cos}[d x] \operatorname{Sec}[c + d x]^8 (-160 i \operatorname{Cos}[7 c] + 160 \operatorname{Sin}[7 c]) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + d x])^8 \right) - \\
 & \left( 1155 i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^8 \operatorname{Sin}[8 c] (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( 8 d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( 1155 i \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^8 \operatorname{Sin}[8 c] (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( 8 d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^8 \left( -\frac{236}{3} i \operatorname{Cos}[8 c] + \frac{236}{3} \operatorname{Sin}[8 c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( \operatorname{Sec}[c + d x]^8 (-160 \operatorname{Cos}[7 c] - 160 i \operatorname{Sin}[7 c]) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \operatorname{Sin}[d x] \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( \operatorname{Sec}[c + d x]^8 \left( \frac{32}{3} \operatorname{Cos}[5 c] + \frac{32}{3} i \operatorname{Sin}[5 c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \operatorname{Sin}[3 d x] \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + d x])^8 \right) + \frac{\operatorname{Sec}[c + d x]^8 \left( \frac{1}{16} \operatorname{Cos}[8 c] + \frac{1}{16} i \operatorname{Sin}[8 c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8}{d \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^4 (a + i a \operatorname{Tan}[c + d x])^8} \\
 & \left( \left( \frac{1}{96} + \frac{i}{96} \right) \operatorname{Sec}[c + d x]^8 \left( -407 i \operatorname{Cos}\left[\frac{15 c}{2}\right] + 343 \operatorname{Cos}\left[\frac{17 c}{2}\right] + 407 \operatorname{Sin}\left[\frac{15 c}{2}\right] + 343 i \operatorname{Sin}\left[\frac{17 c}{2}\right] \right) \right. \\
 & \quad \left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^2 (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \frac{\operatorname{Sec}[c + d x]^8 \left( -\frac{1}{16} \operatorname{Cos}[8 c] - \frac{1}{16} i \operatorname{Sin}[8 c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8}{d \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^4 (a + i a \operatorname{Tan}[c + d x])^8} + \\
 & \left( \left( \frac{1}{96} + \frac{i}{96} \right) \operatorname{Sec}[c + d x]^8 \left( 407 \operatorname{Cos}\left[\frac{15 c}{2}\right] - 343 i \operatorname{Cos}\left[\frac{17 c}{2}\right] + 407 i \operatorname{Sin}\left[\frac{15 c}{2}\right] + 343 \operatorname{Sin}\left[\frac{17 c}{2}\right] \right) \right. \\
 & \quad \left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right) / \\
 & \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^2 (a + i a \operatorname{Tan}[c + d x])^8 \right) + \\
 & \left( 236 \operatorname{Sec}[c + d x]^8 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^8 \right. \\
 & \quad \left. \left( \frac{1}{2} \operatorname{Cos}\left[8 c - \frac{d x}{2}\right] - \frac{1}{2} \operatorname{Cos}\left[8 c + \frac{d x}{2}\right] + \frac{1}{2} i \operatorname{Sin}\left[8 c - \frac{d x}{2}\right] - \frac{1}{2} i \operatorname{Sin}\left[8 c + \frac{d x}{2}\right] \right) \right) / \\
 & \left( 3 d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right) (a + i a \operatorname{Tan}[c + d x])^8 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \operatorname{Sec}[c + dx]^8 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right. \\
 & \quad \left. \left( \frac{1}{2} \operatorname{Cos}\left[8c - \frac{dx}{2}\right] - \frac{1}{2} \operatorname{Cos}\left[8c + \frac{dx}{2}\right] + \frac{1}{2} i \operatorname{Sin}\left[8c - \frac{dx}{2}\right] - \frac{1}{2} i \operatorname{Sin}\left[8c + \frac{dx}{2}\right] \right) \right) / \\
 & \left( 3d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 (a + i a \operatorname{Tan}[c + dx])^8 \right) + \\
 & \left( 4 \operatorname{Sec}[c + dx]^8 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right. \\
 & \quad \left. \left( -\frac{1}{2} \operatorname{Cos}\left[8c - \frac{dx}{2}\right] + \frac{1}{2} \operatorname{Cos}\left[8c + \frac{dx}{2}\right] - \frac{1}{2} i \operatorname{Sin}\left[8c - \frac{dx}{2}\right] + \frac{1}{2} i \operatorname{Sin}\left[8c + \frac{dx}{2}\right] \right) \right) / \\
 & \left( 3d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 (a + i a \operatorname{Tan}[c + dx])^8 \right) + \\
 & \left( 236 \operatorname{Sec}[c + dx]^8 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right. \\
 & \quad \left. \left( -\frac{1}{2} \operatorname{Cos}\left[8c - \frac{dx}{2}\right] + \frac{1}{2} \operatorname{Cos}\left[8c + \frac{dx}{2}\right] - \frac{1}{2} i \operatorname{Sin}\left[8c - \frac{dx}{2}\right] + \frac{1}{2} i \operatorname{Sin}\left[8c + \frac{dx}{2}\right] \right) \right) / \\
 & \left( 3d \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right] \right) (a + i a \operatorname{Tan}[c + dx])^8 \right)
 \end{aligned}$$

**Problem 177: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx]^{11}}{(a + i a \operatorname{Tan}[c + dx])^8} dx$$

Optimal (type 3, 183 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{63 \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 a^8 d} - \frac{63 \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{2 a^8 d} + \frac{2 i \operatorname{Sec}[c + dx]^9}{5 a d (a + i a \operatorname{Tan}[c + dx])^7} - \\
 & \frac{6 i \operatorname{Sec}[c + dx]^7}{5 a^3 d (a + i a \operatorname{Tan}[c + dx])^5} + \frac{42 i \operatorname{Sec}[c + dx]^5}{5 a^2 d (a^2 + i a^2 \operatorname{Tan}[c + dx])^3} + \frac{42 i \operatorname{Sec}[c + dx]^3}{d (a^8 + i a^8 \operatorname{Tan}[c + dx])}
 \end{aligned}$$

Result (type 3, 1244 leaves):

$$\begin{aligned}
 & \left( 63 \operatorname{Cos}[8c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c + dx]^8 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c + dx])^8 \right) - \\
 & \left( 63 \operatorname{Cos}[8c] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}[c + dx]^8 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) / \\
 & \left( 2d (a + i a \operatorname{Tan}[c + dx])^8 \right) + \\
 & \left( \operatorname{Cos}[5dx] \operatorname{Sec}[c + dx]^8 \left( \frac{8}{5} i \operatorname{Cos}[3c] - \frac{8}{5} \operatorname{Sin}[3c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + dx])^8 \right) + \\
 & \left( \operatorname{Cos}[3dx] \operatorname{Sec}[c + dx]^8 (-8 i \operatorname{Cos}[5c] + 8 \operatorname{Sin}[5c]) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + dx])^8 \right) + \\
 & \left( \operatorname{Cos}[dx] \operatorname{Sec}[c + dx]^8 (48 i \operatorname{Cos}[7c] - 48 \operatorname{Sin}[7c]) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^8 \right) / \\
 & \left( d (a + i a \operatorname{Tan}[c + dx])^8 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{Sec}[c] \text{Sec}[c+dx]^8 \left( 8 \text{Cos}[8c] - 8 \text{Sin}[8c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \right) / \\
 & \left( d \left( a + \text{Tan}[c+dx] \right)^8 \right) + \\
 & \left( 63 \text{Log}\left[ \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] - \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \text{Sec}[c+dx]^8 \text{Sin}[8c] \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \right) / \\
 & \left( 2 d \left( a + \text{Tan}[c+dx] \right)^8 \right) - \\
 & \left( 63 \text{Log}\left[ \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] + \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \text{Sec}[c+dx]^8 \text{Sin}[8c] \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \right) / \\
 & \left( 2 d \left( a + \text{Tan}[c+dx] \right)^8 \right) + \\
 & \left( \text{Sec}[c+dx]^8 \left( 48 \text{Cos}[7c] + 48 \text{Sin}[7c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \text{Sin}[dx] \right) / \\
 & \left( d \left( a + \text{Tan}[c+dx] \right)^8 \right) + \\
 & \left( \text{Sec}[c+dx]^8 \left( -8 \text{Cos}[5c] - 8 \text{Sin}[5c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \text{Sin}[3dx] \right) / \\
 & \left( d \left( a + \text{Tan}[c+dx] \right)^8 \right) + \\
 & \left( \text{Sec}[c+dx]^8 \left( \frac{8}{5} \text{Cos}[3c] + \frac{8}{5} \text{Sin}[3c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \text{Sin}[5dx] \right) / \\
 & \left( d \left( a + \text{Tan}[c+dx] \right)^8 \right) + \frac{\text{Sec}[c+dx]^8 \left( \frac{1}{4} \text{Cos}[8c] + \frac{1}{4} \text{Sin}[8c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8}{d \left( \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] - \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \left( a + \text{Tan}[c+dx] \right)^8} + \\
 & \frac{\text{Sec}[c+dx]^8 \left( -\frac{1}{4} \text{Cos}[8c] - \frac{1}{4} \text{Sin}[8c] \right) \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8}{d \left( \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] + \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \left( a + \text{Tan}[c+dx] \right)^8} + \\
 & \left( 8 \text{Sec}[c+dx]^8 \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \right. \\
 & \left. \left( \frac{1}{2} \text{Cos}\left[ 8c - \frac{dx}{2} \right] - \frac{1}{2} \text{Cos}\left[ 8c + \frac{dx}{2} \right] + \frac{1}{2} \text{Sin}\left[ 8c - \frac{dx}{2} \right] - \frac{1}{2} \text{Sin}\left[ 8c + \frac{dx}{2} \right] \right) \right) / \\
 & \left( d \left( \text{Cos}\left[ \frac{c}{2} \right] + \text{Sin}\left[ \frac{c}{2} \right] \right) \left( \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] + \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \left( a + \text{Tan}[c+dx] \right)^8 \right) + \\
 & \left( 8 \text{Sec}[c+dx]^8 \left( \text{Cos}[dx] + \text{Sin}[dx] \right)^8 \right. \\
 & \left. \left( -\frac{1}{2} \text{Cos}\left[ 8c - \frac{dx}{2} \right] + \frac{1}{2} \text{Cos}\left[ 8c + \frac{dx}{2} \right] - \frac{1}{2} \text{Sin}\left[ 8c - \frac{dx}{2} \right] + \frac{1}{2} \text{Sin}\left[ 8c + \frac{dx}{2} \right] \right) \right) / \\
 & \left( d \left( \text{Cos}\left[ \frac{c}{2} \right] - \text{Sin}\left[ \frac{c}{2} \right] \right) \left( \text{Cos}\left[ \frac{c}{2} + \frac{dx}{2} \right] - \text{Sin}\left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \left( a + \text{Tan}[c+dx] \right)^8 \right)
 \end{aligned}$$

**Problem 185: Result unnecessarily involves higher level functions.**

$$\int \left( e \text{Sec}[c+dx] \right)^{7/2} \left( a + \text{Tan}[c+dx] \right) dx$$

Optimal (type 4, 123 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{6 a e^4 \text{EllipticE}\left[ \frac{1}{2} (c+dx), 2 \right]}{5 d \sqrt{\text{Cos}[c+dx]} \sqrt{e \text{Sec}[c+dx]}} + \frac{2 \text{Tan}[c+dx] \left( e \text{Sec}[c+dx] \right)^{7/2}}{7 d} + \\
 & \frac{6 a e^3 \sqrt{e \text{Sec}[c+dx]} \text{Sin}[c+dx]}{5 d} + \frac{2 a e \left( e \text{Sec}[c+dx] \right)^{5/2} \text{Sin}[c+dx]}{5 d}
 \end{aligned}$$

Result (type 5, 134 leaves):

$$\left( 2 i a e^3 e^{-i(c+dx)} \left( 21 + 77 e^{2i(c+dx)} + 103 e^{4i(c+dx)} + 7 e^{6i(c+dx)} - 21 (1 + e^{2i(c+dx)})^{7/2} \right. \right. \\ \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \sqrt{e \sec[c+dx]} \right) / \left( 35 d (1 + e^{2i(c+dx)})^3 \right)$$

**Problem 187: Result unnecessarily involves higher level functions.**

$$\int (e \sec[c+dx])^{3/2} (a + i a \tan[c+dx]) dx$$

Optimal (type 4, 90 leaves, 4 steps):

$$-\frac{2 a e^2 \text{EllipticE} \left[ \frac{1}{2} (c+dx), 2 \right]}{d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} + \frac{2 i a (e \sec[c+dx])^{3/2}}{3 d} + \frac{2 a e \sqrt{e \sec[c+dx]} \sin[c+dx]}{d}$$

Result (type 5, 98 leaves):

$$\left( 2 a e^2 e^{-2i(c+dx)} \right. \\ \left( -4 + 3 \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] - i \tan[c+dx] \right) \\ \left. (-i + \tan[c+dx]) \right) / \left( 3 d \sqrt{e \sec[c+dx]} \right)$$

**Problem 189: Result unnecessarily involves higher level functions.**

$$\int \frac{a + i a \tan[c+dx]}{\sqrt{e \sec[c+dx]}} dx$$

Optimal (type 4, 60 leaves, 3 steps):

$$-\frac{2 i a}{d \sqrt{e \sec[c+dx]}} + \frac{2 a \text{EllipticE} \left[ \frac{1}{2} (c+dx), 2 \right]}{d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}}$$

Result (type 5, 90 leaves):

$$-\left( \left( 4 i a \left( 1 + e^{2i(c+dx)} - \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right) / \right. \\ \left. \left( d (1 + e^{2i(c+dx)}) \sqrt{e \sec[c+dx]} \right) \right)$$

**Problem 191: Result unnecessarily involves higher level functions.**

$$\int \frac{a + i a \tan[c+dx]}{(e \sec[c+dx])^{5/2}} dx$$

Optimal (type 4, 96 leaves, 4 steps):

$$-\frac{2 i a}{5 d (e \operatorname{Sec}[c+d x])^{5/2}} + \frac{6 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d e^2 \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{2 a \operatorname{Sin}[c+d x]}{5 d e (e \operatorname{Sec}[c+d x])^{3/2}}$$

Result (type 5, 108 leaves):

$$-\left(\left(i a \left(7+8 e^{2 i(c+d x)}+e^{4 i(c+d x)}-12 \sqrt{1+e^{2 i(c+d x)}}\right.\right.\right. \\ \left.\left.\left.\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]\right)\right) / \left(5 d e^2 \left(1+e^{2 i(c+d x)}\right) \sqrt{e \operatorname{Sec}[c+d x]}\right)\right)$$

**Problem 193: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+d x])^{3/2} (a+i a \operatorname{Tan}[c+d x])^2 dx$$

Optimal (type 4, 138 leaves, 5 steps):

$$-\frac{14 a^2 e^2 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{14 i a^2 (e \operatorname{Sec}[c+d x])^{3/2}}{15 d} + \\ \frac{14 a^2 e \sqrt{e \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{5 d} + \frac{2 i (e \operatorname{Sec}[c+d x])^{3/2} (a^2+i a^2 \operatorname{Tan}[c+d x])}{5 d}$$

Result (type 5, 121 leaves):

$$-\left(\left(2 i a^2 e^{-i(c+d x)}\left(-21-56 e^{2 i(c+d x)}-47 e^{4 i(c+d x)}+21\left(1+e^{2 i(c+d x)}\right)^{5/2}\right.\right.\right. \\ \left.\left.\left.\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]\right) \sqrt{e \operatorname{Sec}[c+d x]}\right) / \left(15 d\left(1+e^{2 i(c+d x)}\right)^2\right)\right)$$

**Problem 195: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+i a \operatorname{Tan}[c+d x])^2}{\sqrt{e \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 4, 107 leaves, 4 steps):

$$\frac{6 a^2 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} - \frac{6 a^2 \sqrt{e \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d e} - \frac{4 i (a^2+i a^2 \operatorname{Tan}[c+d x])}{d \sqrt{e \operatorname{Sec}[c+d x]}}$$

Result (type 5, 94 leaves):

$$-\left(\left(4 i a^2\left(3+2 e^{2 i(c+d x)}-3 \sqrt{1+e^{2 i(c+d x)}}\right.\right.\right. \\ \left.\left.\left.\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]\right)\right) / \left(d\left(1+e^{2 i(c+d x)}\right) \sqrt{e \operatorname{Sec}[c+d x]}\right)\right)$$



**Problem 197: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + i a \tan [c + d x])^2}{(e \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 85 leaves, 3 steps):

$$\frac{2 a^2 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d e^2 \sqrt{\cos [c+d x]} \sqrt{e \sec [c+d x]}} - \frac{4 i\left(a^2 + i a^2 \tan [c+d x]\right)}{5 d\left(e \sec [c+d x]\right)^{5/2}}$$

Result (type 5, 110 leaves):

$$-\left(\left(2 i a^2\left(2+3 e^{2 i(c+d x)}+e^{4 i(c+d x)}-2 \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]\right)\right) / \left(5 d e^2\left(1+e^{2 i(c+d x)}\right) \sqrt{e \sec [c+d x]}\right)\right)$$

**Problem 199: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + i a \tan [c + d x])^2}{(e \sec [c + d x])^{9/2}} dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\frac{2 a^2 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{3 d e^4 \sqrt{\cos [c+d x]} \sqrt{e \sec [c+d x]}} + \frac{2 a^2 \sin [c+d x]}{9 d e^3\left(e \sec [c+d x]\right)^{3/2}} - \frac{4 i\left(a^2 + i a^2 \tan [c+d x]\right)}{9 d\left(e \sec [c+d x]\right)^{9/2}}$$

Result (type 5, 123 leaves):

$$-\left(\left(i a^2\left(15+19 e^{2 i(c+d x)}+5 e^{4 i(c+d x)}+e^{6 i(c+d x)}-24 \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]\right)\right) / \left(18 d e^4\left(1+e^{2 i(c+d x)}\right) \sqrt{e \sec [c+d x]}\right)\right)$$

**Problem 201: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (e \sec [c + d x])^{7/2} (a + i a \tan [c + d x])^3 dx$$

Optimal (type 4, 202 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{2 a^3 e^4 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d \sqrt{\text{Cos}[c+d x]} \sqrt{e \text{Sec}[c+d x]}} + \frac{10 i a^3 (e \text{Sec}[c+d x])^{7/2}}{21 d} + \\
 & \frac{2 a^3 e^3 \sqrt{e \text{Sec}[c+d x]} \text{Sin}[c+d x]}{d} + \frac{2 a^3 e (e \text{Sec}[c+d x])^{5/2} \text{Sin}[c+d x]}{3 d} + \\
 & \frac{2 i a (e \text{Sec}[c+d x])^{7/2} (a+i a \text{Tan}[c+d x])^2}{11 d} + \frac{10 i (e \text{Sec}[c+d x])^{7/2} (a^3+i a^3 \text{Tan}[c+d x])}{33 d}
 \end{aligned}$$

Result (type 5, 425 leaves):

$$\begin{aligned}
 & - \left( \left( 2 i \sqrt{2} e^{-i(4 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \right. \right. \\
 & \quad \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] \right) \right. \\
 & \quad \left. (e \text{Sec}[c+d x])^{7/2} (a+i a \text{Tan}[c+d x])^3 \right) / \\
 & \quad \left. \left( d (-1+e^{2 i c}) \text{Sec}[c+d x]^{13/2} (\text{Cos}[d x]+i \text{Sin}[d x])^3 \right) \right) + \\
 & \frac{1}{d (\text{Cos}[d x]+i \text{Sin}[d x])^3} \text{Cos}[c+d x]^6 (e \text{Sec}[c+d x])^{7/2} \\
 & \left( \text{Sec}[c+d x]^5 \left( -\frac{2}{11} i \text{Cos}[3 c] - \frac{2}{11} \text{Sin}[3 c] \right) + \text{Cos}[d x] \text{Csc}[c] (2 \text{Cos}[3 c] - 2 i \text{Sin}[3 c]) + \right. \\
 & \quad \text{Sec}[c] \text{Sec}[c+d x]^3 (12 \text{Cos}[c] + 7 i \text{Sin}[c]) \left( \frac{2}{21} i \text{Cos}[3 c] + \frac{2}{21} \text{Sin}[3 c] \right) + \\
 & \quad \text{Sec}[c] \text{Sec}[c+d x]^2 \left( \frac{2}{3} \text{Cos}[3 c] - \frac{2}{3} i \text{Sin}[3 c] \right) \text{Sin}[d x] + \\
 & \quad \text{Sec}[c] \text{Sec}[c+d x]^4 \left( -\frac{2}{3} \text{Cos}[3 c] + \frac{2}{3} i \text{Sin}[3 c] \right) \text{Sin}[d x] + \\
 & \quad \left. \text{Sec}[c+d x] \left( \frac{2}{3} \text{Cos}[3 c] - \frac{2}{3} i \text{Sin}[3 c] \right) \text{Tan}[c] \right) (a+i a \text{Tan}[c+d x])^3
 \end{aligned}$$

**Problem 203: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (e \text{Sec}[c+d x])^{3/2} (a+i a \text{Tan}[c+d x])^3 dx$$

Optimal (type 4, 175 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{22 a^3 e^2 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 d \sqrt{\text{Cos}[c+dx]} \sqrt{e \text{Sec}[c+dx]}} + \frac{22 i a^3 (e \text{Sec}[c+dx])^{3/2}}{15 d} + \\
 & \frac{22 a^3 e \sqrt{e \text{Sec}[c+dx]} \text{Sin}[c+dx]}{5 d} + \frac{2 i a (e \text{Sec}[c+dx])^{3/2} (a + i a \text{Tan}[c+dx])^2}{7 d} + \\
 & \frac{22 i (e \text{Sec}[c+dx])^{3/2} (a^3 + i a^3 \text{Tan}[c+dx])}{35 d}
 \end{aligned}$$

Result (type 5, 367 leaves):

$$\begin{aligned}
 & - \left( \left( 22 i \sqrt{2} e^{-i(4c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. (e \text{Sec}[c+dx])^{3/2} (a + i a \text{Tan}[c+dx])^3 \right) / \right. \\
 & \quad \left. \left( 5 d (-1 + e^{2ic}) \text{Sec}[c+dx]^{9/2} (\text{Cos}[dx] + i \text{Sin}[dx])^3 \right) \right) + \\
 & \frac{1}{d (\text{Cos}[dx] + i \text{Sin}[dx])^3} \text{Cos}[c+dx]^4 (e \text{Sec}[c+dx])^{3/2} \\
 & \left( \text{Sec}[c+dx]^3 \left( -\frac{2}{7} i \text{Cos}[3c] - \frac{2}{7} \text{Sin}[3c] \right) + \text{Cos}[dx] \text{Csc}[c] \left( \frac{22}{5} \text{Cos}[3c] - \frac{22}{5} i \text{Sin}[3c] \right) + \right. \\
 & \quad \left. \text{Sec}[c] \text{Sec}[c+dx] (20 \text{Cos}[c] + 9 i \text{Sin}[c]) \left( \frac{2}{15} i \text{Cos}[3c] + \frac{2}{15} \text{Sin}[3c] \right) + \right. \\
 & \quad \left. \text{Sec}[c] \text{Sec}[c+dx]^2 \left( -\frac{6}{5} \text{Cos}[3c] + \frac{6}{5} i \text{Sin}[3c] \right) \text{Sin}[dx] \right) (a + i a \text{Tan}[c+dx])^3
 \end{aligned}$$

**Problem 205: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + i a \text{Tan}[c+dx])^3}{\sqrt{e \text{Sec}[c+dx]}} dx$$

Optimal (type 4, 124 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{26 i a^3}{3 d \sqrt{e \text{Sec}[c+dx]}} + \frac{14 a^3 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{d \sqrt{\text{Cos}[c+dx]} \sqrt{e \text{Sec}[c+dx]}} - \frac{6 a^3 \text{Tan}[c+dx]}{d \sqrt{e \text{Sec}[c+dx]}} - \frac{2 i a^3 \text{Tan}[c+dx]^2}{3 d \sqrt{e \text{Sec}[c+dx]}}
 \end{aligned}$$

Result (type 5, 109 leaves):

$$\begin{aligned}
 & \left( i a^3 \text{Sec}[c+dx]^2 \left( -35 - 33 \text{Cos}[2(c+dx)] + 21 e^{-2i(c+dx)} (1 + e^{2i(c+dx)})^{3/2} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 9 i \text{Sin}[2(c+dx)] \right) \right) / \left( 3 d \sqrt{e \text{Sec}[c+dx]} \right)
 \end{aligned}$$

### Problem 207: Result unnecessarily involves higher level functions.

$$\int \frac{(a + i a \tan [c + d x])^3}{(e \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 111 leaves, 4 steps):

$$\frac{6 i a^3}{5 d e^2 \sqrt{e \sec [c + d x]}} - \frac{6 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d e^2 \sqrt{\cos [c + d x]} \sqrt{e \sec [c + d x]}} - \frac{4 i a (a + i a \tan [c + d x])^2}{5 d (e \sec [c + d x])^{5/2}}$$

Result (type 5, 110 leaves):

$$-\left(4 i a^3 \left(-3 - 2 e^{2 i (c+d x)} + e^{4 i (c+d x)} + 3 \sqrt{1 + e^{2 i (c+d x)}}\right) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]\right) / \left(5 d e^2 (1 + e^{2 i (c+d x)}) \sqrt{e \sec [c + d x]}\right)$$

### Problem 209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan [c + d x])^3}{(e \sec [c + d x])^{9/2}} dx$$

Optimal (type 4, 124 leaves, 4 steps):

$$\frac{2 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d e^4 \sqrt{\cos [c + d x]} \sqrt{e \sec [c + d x]}} - \frac{2 i (a + i a \tan [c + d x])^3}{9 d (e \sec [c + d x])^{9/2}} - \frac{4 i (a^3 + i a^3 \tan [c + d x])}{15 d e^2 (e \sec [c + d x])^{5/2}}$$

Result (type 5, 371 leaves):

$$\left( 2 i \sqrt{2} e^{-i(4c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\
 \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 \left. \operatorname{Sec}[c+dx]^{3/2} (a + i a \operatorname{Tan}[c+dx])^3 \right) / \\
 (15 d (-1 + e^{2ic}) (e \operatorname{Sec}[c+dx])^{9/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3) + (\operatorname{Sec}[c+dx])^2 \\
 \left( -\frac{8}{45} i \operatorname{Cos}[3dx] + \operatorname{Cos}[dx] \operatorname{Csc}[c] (12 \operatorname{Cos}[c] + 11 i \operatorname{Sin}[c]) \left( -\frac{1}{90} \operatorname{Cos}[2c] + \frac{1}{90} i \operatorname{Sin}[2c] \right) + \right. \\
 \left. \operatorname{Cos}[5dx] \left( -\frac{1}{18} i \operatorname{Cos}[2c] + \frac{1}{18} \operatorname{Sin}[2c] \right) + \left( \frac{23}{90} \operatorname{Cos}[2c] - \frac{23}{90} i \operatorname{Sin}[2c] \right) \operatorname{Sin}[dx] + \right. \\
 \left. \frac{8}{45} \operatorname{Sin}[3dx] + \left( \frac{1}{18} \operatorname{Cos}[2c] + \frac{1}{18} i \operatorname{Sin}[2c] \right) \operatorname{Sin}[5dx] \right) (a + i a \operatorname{Tan}[c+dx])^3 \Big/ \\
 (d (e \operatorname{Sec}[c+dx])^{9/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3)$$

**Problem 211: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \operatorname{Tan}[c+dx])^3}{(e \operatorname{Sec}[c+dx])^{13/2}} dx$$

Optimal (type 4, 155 leaves, 5 steps):

$$\frac{14 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{39 d e^6 \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Sec}[c+dx]}} + \frac{14 a^3 \operatorname{Sin}[c+dx]}{117 d e^5 (e \operatorname{Sec}[c+dx])^{3/2}} - \\
 \frac{2 i (a + i a \operatorname{Tan}[c+dx])^3}{13 d (e \operatorname{Sec}[c+dx])^{13/2}} - \frac{28 i (a^3 + i a^3 \operatorname{Tan}[c+dx])}{117 d e^2 (e \operatorname{Sec}[c+dx])^{9/2}}$$

Result (type 5, 437 leaves):

$$\left( 14 i \sqrt{2} e^{-i(4c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}[c+dx]^{7/2} (a+i a \operatorname{Tan}[c+dx])^3 \right) / \\ \frac{(39 d (-1+e^{2ic}) (e \operatorname{Sec}[c+dx])^{13/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3) + 1}{d (e \operatorname{Sec}[c+dx])^{13/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3} \\ \operatorname{Sec}[c+dx]^4 \left( -\frac{31}{234} i \operatorname{Cos}[3dx] + \operatorname{Cos}[5dx] \left( -\frac{25}{468} i \operatorname{Cos}[2c] + \frac{25}{468} \operatorname{Sin}[2c] \right) + \right. \\ \left. \operatorname{Cos}[dx] \operatorname{Csc}[c] (253 + 419 \operatorname{Cos}[2c] + 185 i \operatorname{Sin}[2c]) \left( -\frac{\operatorname{Cos}[3c]}{1872} + \frac{i \operatorname{Sin}[3c]}{1872} \right) + \right. \\ \left. \operatorname{Cos}[7dx] \left( -\frac{1}{104} i \operatorname{Cos}[4c] + \frac{1}{104} \operatorname{Sin}[4c] \right) + \right. \\ \left. (419 \operatorname{Cos}[c] + 185 i \operatorname{Sin}[c]) \left( \frac{1}{936} \operatorname{Cos}[3c] - \frac{1}{936} i \operatorname{Sin}[3c] \right) \operatorname{Sin}[dx] + \right. \\ \left. \frac{31}{234} \operatorname{Sin}[3dx] + \left( \frac{25}{468} \operatorname{Cos}[2c] + \frac{25}{468} i \operatorname{Sin}[2c] \right) \operatorname{Sin}[5dx] + \right. \\ \left. \left( \frac{1}{104} \operatorname{Cos}[4c] + \frac{1}{104} i \operatorname{Sin}[4c] \right) \operatorname{Sin}[7dx] \right) (a+i a \operatorname{Tan}[c+dx])^3$$

**Problem 213: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+dx])^{3/2} (a+i a \operatorname{Tan}[c+dx])^4 dx$$

Optimal (type 4, 215 leaves, 7 steps):

$$-\frac{22 a^4 e^2 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{3 d \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Sec}[c+dx]}} + \frac{22 i a^4 (e \operatorname{Sec}[c+dx])^{3/2}}{9 d} + \\ \frac{22 a^4 e \sqrt{e \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3 d} + \frac{2 i a (e \operatorname{Sec}[c+dx])^{3/2} (a+i a \operatorname{Tan}[c+dx])^3}{9 d} + \\ \frac{10 i (e \operatorname{Sec}[c+dx])^{3/2} (a^2+i a^2 \operatorname{Tan}[c+dx])^2}{21 d} + \frac{22 i (e \operatorname{Sec}[c+dx])^{3/2} (a^4+i a^4 \operatorname{Tan}[c+dx])}{21 d}$$

Result (type 5, 414 leaves):

$$\begin{aligned}
 & - \left( \left( 22 i \sqrt{2} e^{-i(5c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \right. \\
 & \quad \left. \left. \left( e \operatorname{Sec}[c+dx] \right)^{3/2} \left( a + i a \operatorname{Tan}[c+dx] \right)^4 \right) \right) / \\
 & \quad \left. \left( 3 d (-1 + e^{2ic}) \operatorname{Sec}[c+dx]^{11/2} \left( \operatorname{Cos}[dx] + i \operatorname{Sin}[dx] \right)^4 \right) \right) + \\
 & \quad \frac{1}{d \left( \operatorname{Cos}[dx] + i \operatorname{Sin}[dx] \right)^4} \operatorname{Cos}[c+dx]^5 \left( e \operatorname{Sec}[c+dx] \right)^{3/2} \\
 & \quad \left( \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \left( 36 \operatorname{Cos}[c] + 7 i \operatorname{Sin}[c] \right) \left( -\frac{2}{63} i \operatorname{Cos}[4c] - \frac{2}{63} \operatorname{Sin}[4c] \right) + \right. \\
 & \quad \operatorname{Cos}[dx] \operatorname{Csc}[c] \left( \frac{22}{3} \operatorname{Cos}[4c] - \frac{22}{3} i \operatorname{Sin}[4c] \right) + \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \left( 24 \operatorname{Cos}[c] + 13 i \operatorname{Sin}[c] \right) \\
 & \quad \left. \left( \frac{2}{9} i \operatorname{Cos}[4c] + \frac{2}{9} \operatorname{Sin}[4c] \right) + \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 \left( \frac{2}{9} \operatorname{Cos}[4c] - \frac{2}{9} i \operatorname{Sin}[4c] \right) \operatorname{Sin}[dx] + \right. \\
 & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 \left( -\frac{26}{9} \operatorname{Cos}[4c] + \frac{26}{9} i \operatorname{Sin}[4c] \right) \operatorname{Sin}[dx] \right) \left( a + i a \operatorname{Tan}[c+dx] \right)^4
 \end{aligned}$$

**Problem 215: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \operatorname{Tan}[c + dx])^4}{\sqrt{e \operatorname{Sec}[c + dx]}} dx$$

Optimal (type 4, 178 leaves, 6 steps):

$$\begin{aligned}
 & \frac{154 a^4 \operatorname{EllipticE} \left[ \frac{1}{2} (c + dx), 2 \right]}{5 d \sqrt{\operatorname{Cos}[c + dx]} \sqrt{e \operatorname{Sec}[c + dx]}} - \\
 & \frac{154 i a^4 \left( e \operatorname{Sec}[c + dx] \right)^{3/2}}{15 d e^2} - \frac{154 a^4 \sqrt{e \operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{5 d e} - \\
 & \frac{4 i a \left( a + i a \operatorname{Tan}[c + dx] \right)^3}{d \sqrt{e \operatorname{Sec}[c + dx]}} - \frac{22 i \left( e \operatorname{Sec}[c + dx] \right)^{3/2} \left( a^4 + i a^4 \operatorname{Tan}[c + dx] \right)}{5 d e^2}
 \end{aligned}$$

Result (type 5, 370 leaves):

$$\left( 154 i \sqrt{2} e^{-i(5c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. (a+i a \operatorname{Tan}[c+dx])^4 \right) / \\ \left( 5 d (-1+e^{2ic}) \operatorname{Sec}[c+dx]^{7/2} \sqrt{e \operatorname{Sec}[c+dx]} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) + \\ \frac{1}{d \sqrt{e \operatorname{Sec}[c+dx]} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4} \\ \operatorname{Cos}[c+dx]^3 \left( \operatorname{Cos}[dx] \operatorname{Csc}[c] (77 \operatorname{Cos}[c] - 37 i \operatorname{Sin}[c]) \left( -\frac{2}{5} \operatorname{Cos}[3c] + \frac{2}{5} i \operatorname{Sin}[3c] \right) + \right. \\ \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (20 \operatorname{Cos}[c] + 3 i \operatorname{Sin}[c]) \left( -\frac{2}{15} i \operatorname{Cos}[4c] - \frac{2}{15} \operatorname{Sin}[4c] \right) + \\ \left. (16 \operatorname{Cos}[3c] - 16 i \operatorname{Sin}[3c]) \operatorname{Sin}[dx] + \right. \\ \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 \left( \frac{2}{5} \operatorname{Cos}[4c] - \frac{2}{5} i \operatorname{Sin}[4c] \right) \operatorname{Sin}[dx] \right) (a+i a \operatorname{Tan}[c+dx])^4$$

**Problem 217: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+dx])^4}{(e \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 156 leaves, 5 steps):

$$-\frac{42 a^4 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 d e^2 \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Sec}[c+dx]}} + \frac{42 a^4 \sqrt{e \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{5 d e^3} - \\ \frac{4 i a (a+i a \operatorname{Tan}[c+dx])^3}{5 d (e \operatorname{Sec}[c+dx])^{5/2}} + \frac{28 i (a^4 + i a^4 \operatorname{Tan}[c+dx])}{5 d e^2 \sqrt{e \operatorname{Sec}[c+dx]}}$$

Result (type 5, 341 leaves):



$$\begin{aligned}
 & - \left( \left( 42 i \sqrt{2} e^{-i(5c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \right. \\
 & \quad \left. \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \right. \\
 & \quad \left. \left. (a+i a \operatorname{Tan}[c+dx])^4 \right) / \right. \\
 & \quad \left. \left( 5d(-1+e^{2ic}) \operatorname{Sec}[c+dx]^{3/2} (e \operatorname{Sec}[c+dx])^{5/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) \right) + \\
 & \left( \operatorname{Cos}[c+dx] \left( \operatorname{Cos}[3dx] \left( -\frac{4}{5} i \operatorname{Cos}[c] - \frac{4 \operatorname{Sin}[c]}{5} \right) + \right. \right. \\
 & \quad \left. \left. \operatorname{Cos}[dx] \operatorname{Csc}[c] (3 \operatorname{Cos}[c] - i \operatorname{Sin}[c]) \left( \frac{14}{5} \operatorname{Cos}[3c] - \frac{14}{5} i \operatorname{Sin}[3c] \right) + \right. \right. \\
 & \quad \left. \left. \left( -\frac{28}{5} \operatorname{Cos}[3c] + \frac{28}{5} i \operatorname{Sin}[3c] \right) \operatorname{Sin}[dx] + \left( \frac{4 \operatorname{Cos}[c]}{5} - \frac{4}{5} i \operatorname{Sin}[c] \right) \operatorname{Sin}[3dx] \right) \right. \\
 & \quad \left. (a+i a \operatorname{Tan}[c+dx])^4 \right) / \left( d (e \operatorname{Sec}[c+dx])^{5/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right)
 \end{aligned}$$

**Problem 219: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+dx])^4}{(e \operatorname{Sec}[c+dx])^{9/2}} dx$$

Optimal (type 4, 125 leaves, 4 steps):

$$-\frac{2 a^4 \operatorname{EllipticE} \left[ \frac{1}{2} (c+dx), 2 \right]}{15 d e^4 \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Sec}[c+dx]}} - \frac{4 i a (a+i a \operatorname{Tan}[c+dx])^3}{9 d (e \operatorname{Sec}[c+dx])^{9/2}} + \frac{4 i (a^4+i a^4 \operatorname{Tan}[c+dx])}{15 d e^2 (e \operatorname{Sec}[c+dx])^{5/2}}$$

Result (type 5, 383 leaves):

$$\begin{aligned}
 & - \left( \left( 2 \, i \, \sqrt{2} \, e^{-i (5 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \right. \right. \\
 & \quad \left. \left. \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \right. \right. \\
 & \quad \left. \left. \sqrt{\operatorname{Sec}[c+d x]} (a+i a \operatorname{Tan}[c+d x])^4 \right) \right) / \\
 & \quad \left. \left( 15 d (-1+e^{2 i c}) (e \operatorname{Sec}[c+d x])^{9/2} (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^4 \right) \right) + \\
 & \quad \frac{1}{d (e \operatorname{Sec}[c+d x])^{9/2} (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^4} \\
 & \quad \operatorname{Sec}[c+d x] \left( \operatorname{Cos}[3 d x] \left( -\frac{7}{45} i \operatorname{Cos}[c] - \frac{7 \operatorname{Sin}[c]}{45} \right) + \operatorname{Cos}[5 d x] \left( -\frac{1}{9} i \operatorname{Cos}[c] + \frac{\operatorname{Sin}[c]}{9} \right) + \right. \\
 & \quad \operatorname{Cos}[d x] \operatorname{Csc}[c] (3 \operatorname{Cos}[c] - i \operatorname{Sin}[c]) \left( \frac{2}{45} \operatorname{Cos}[3 c] - \frac{2}{45} i \operatorname{Sin}[3 c] \right) + \\
 & \quad \left. \left( -\frac{4}{45} \operatorname{Cos}[3 c] + \frac{4}{45} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[d x] + \left( \frac{7 \operatorname{Cos}[c]}{45} - \frac{7}{45} i \operatorname{Sin}[c] \right) \operatorname{Sin}[3 d x] + \right. \\
 & \quad \left. \left( \frac{\operatorname{Cos}[c]}{9} + \frac{1}{9} i \operatorname{Sin}[c] \right) \operatorname{Sin}[5 d x] \right) (a+i a \operatorname{Tan}[c+d x])^4
 \end{aligned}$$

**Problem 221: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+d x])^4}{(e \operatorname{Sec}[c+d x])^{13/2}} dx$$

Optimal (type 4, 156 leaves, 5 steps):

$$\begin{aligned}
 & \frac{2 a^4 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{39 d e^6 \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{2 a^4 \operatorname{Sin}[c+d x]}{117 d e^5 (e \operatorname{Sec}[c+d x])^{3/2}} - \\
 & \frac{4 i a (a+i a \operatorname{Tan}[c+d x])^3}{13 d (e \operatorname{Sec}[c+d x])^{13/2}} - \frac{4 i (a^4+i a^4 \operatorname{Tan}[c+d x])}{117 d e^2 (e \operatorname{Sec}[c+d x])^{9/2}}
 \end{aligned}$$

Result (type 5, 435 leaves):

$$\left( 2 i \sqrt{2} e^{-i(5c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\
 \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 \left. \operatorname{Sec}[c+dx]^{5/2} (a+i a \operatorname{Tan}[c+dx])^4 \right) / \\
 \left( 39 d (-1+e^{2ic}) (e \operatorname{Sec}[c+dx])^{13/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4 \right) + \\
 \frac{1}{d (e \operatorname{Sec}[c+dx])^{13/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^4} \operatorname{Sec}[c+dx]^3 \\
 \left( \operatorname{Cos}[3dx] \left( -\frac{59}{468} i \operatorname{Cos}[c] - \frac{59 \operatorname{Sin}[c]}{468} \right) + \operatorname{Cos}[5dx] \left( -\frac{37}{468} i \operatorname{Cos}[c] + \frac{37 \operatorname{Sin}[c]}{468} \right) \right) + \\
 \operatorname{Cos}[dx] \operatorname{Csc}[c] (24 \operatorname{Cos}[c] + 31 i \operatorname{Sin}[c]) \left( -\frac{1}{468} \operatorname{Cos}[3c] + \frac{1}{468} i \operatorname{Sin}[3c] \right) + \\
 \operatorname{Cos}[7dx] \left( -\frac{1}{52} i \operatorname{Cos}[3c] + \frac{1}{52} \operatorname{Sin}[3c] \right) + \left( \frac{55}{468} \operatorname{Cos}[3c] - \frac{55}{468} i \operatorname{Sin}[3c] \right) \operatorname{Sin}[dx] + \\
 \left( \frac{59 \operatorname{Cos}[c]}{468} - \frac{59}{468} i \operatorname{Sin}[c] \right) \operatorname{Sin}[3dx] + \left( \frac{37 \operatorname{Cos}[c]}{468} + \frac{37}{468} i \operatorname{Sin}[c] \right) \operatorname{Sin}[5dx] + \\
 \left( \frac{1}{52} \operatorname{Cos}[3c] + \frac{1}{52} i \operatorname{Sin}[3c] \right) \operatorname{Sin}[7dx] \right) (a+i a \operatorname{Tan}[c+dx])^4$$

**Problem 223: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+dx])^{11/2}}{a+i a \operatorname{Tan}[c+dx]} dx$$

Optimal (type 4, 136 leaves, 5 steps):

$$-\frac{6 e^6 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 a d \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Sec}[c+dx]}} - \frac{2 i e^2 (e \operatorname{Sec}[c+dx])^{7/2}}{7 a d} + \\
 \frac{6 e^5 \sqrt{e \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{5 a d} + \frac{2 e^3 (e \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{5 a d}$$

Result (type 5, 128 leaves):

$$-\frac{1}{70 a d} e^4 (e \operatorname{Sec}[c+dx])^{3/2} \left( -36 - 28 \operatorname{Cos}[2(c+dx)] \right) + \\
 21 e^{-2i(c+dx)} (1+e^{2i(c+dx)})^{5/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\
 7 i \operatorname{Sec}[c+dx] \operatorname{Sin}[3(c+dx)] + 27 i \operatorname{Tan}[c+dx] \right) (i + \operatorname{Tan}[c+dx])$$

**Problem 225: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c + d x])^{7/2}}{a + i a \operatorname{Tan}[c + d x]} dx$$

Optimal (type 4, 101 leaves, 4 steps):

$$-\frac{2 e^4 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{a d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} - \frac{2 i e^2 (e \operatorname{Sec}[c + d x])^{3/2}}{3 a d} + \frac{2 e^3 \sqrt{e \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{a d}$$

Result (type 5, 101 leaves):

$$\frac{1}{3 a d} 2 e^3 \sqrt{e \operatorname{Sec}[c + d x]} (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) (\operatorname{Cos}[d x] - i \operatorname{Sin}[d x]) \\ \left(2 i - 3 i \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + \operatorname{Tan}[c + d x]\right)$$

**Problem 227: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c + d x])^{3/2}}{a + i a \operatorname{Tan}[c + d x]} dx$$

Optimal (type 4, 70 leaves, 3 steps):

$$\frac{2 i e^2}{a d \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{2 e^2 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{a d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}}$$

Result (type 5, 74 leaves):

$$\frac{1}{a d} 2 i e e^{-i (c + d x)} \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] \sqrt{e \operatorname{Sec}[c + d x]}$$

**Problem 229: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])} dx$$

Optimal (type 4, 80 leaves, 3 steps):

$$\frac{6 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 a d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{2 i}{5 d \sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])}$$

Result (type 5, 98 leaves):

$$-\left(\left(\left(2 + 2 \operatorname{Cos}[2(c + d x)] - 6 \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + 3 i \operatorname{Sin}[2(c + d x)]\right) (i + \operatorname{Tan}[c + d x])\right) / \left(5 a d \sqrt{e \operatorname{Sec}[c + d x]}\right)\right)$$

**Problem 231: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{(e \operatorname{Sec}[c + d x])^{5/2} (a + i a \operatorname{Tan}[c + d x])} dx$$

Optimal (type 4, 114 leaves, 4 steps):

$$\frac{14 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 a d e^2 \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{14 \operatorname{Sin}[c + d x]}{45 a d e (e \operatorname{Sec}[c + d x])^{3/2}} + \frac{2 i}{9 d (e \operatorname{Sec}[c + d x])^{5/2} (a + i a \operatorname{Tan}[c + d x])}$$

Result (type 5, 123 leaves):

$$-\left(\left(\left(62 + 64 \operatorname{Cos}[2(c + d x)] + 2 \operatorname{Cos}[4(c + d x)] - 168 \sqrt{1 + e^{2i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+d x)}\right] + 98 i \operatorname{Sin}[2(c + d x)] + 7 i \operatorname{Sin}[4(c + d x)]\right) (i + \operatorname{Tan}[c + d x])\right) / \left(180 a d e^2 \sqrt{e \operatorname{Sec}[c + d x]}\right)\right)$$

**Problem 233: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c + d x])^{15/2}}{(a + i a \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 4, 183 leaves, 6 steps):

$$\frac{22 e^8 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 a^2 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{22 e^7 \sqrt{e \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a^2 d} + \frac{22 e^5 (e \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{45 a^2 d} + \frac{22 e^3 (e \operatorname{Sec}[c + d x])^{9/2} \operatorname{Sin}[c + d x]}{63 a^2 d} - \frac{4 i e^2 (e \operatorname{Sec}[c + d x])^{11/2}}{7 d (a^2 + i a^2 \operatorname{Tan}[c + d x])}$$

Result (type 5, 285 leaves):

$$\frac{1}{15 d \operatorname{Sec}[c+d x]^{11/2} (a+i a \operatorname{Tan}[c+d x])^2} \left( (e \operatorname{Sec}[c+d x])^{15/2} (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^2 \left( -\frac{1}{-1+e^{2 i c}} 22 i \sqrt{2} e^{i(c-d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}}} \right. \right. \\ \left. \left. \left( 1+e^{2 i(c+d x)}+(-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]\right) \right) + \right. \\ \left. \frac{1}{168} \operatorname{Csc}[c] \operatorname{Sec}[c+d x]^{9/2} (\operatorname{Cos}[2 c]+i \operatorname{Sin}[2 c]) \right. \\ \left. (1260 \operatorname{Cos}[d x]+1050 \operatorname{Cos}[2 c+d x]+1078 \operatorname{Cos}[2 c+3 d x]+77 \operatorname{Cos}[4 c+3 d x]+ \right. \\ \left. \left. 231 \operatorname{Cos}[4 c+5 d x]+720 i \operatorname{Sin}[d x]-720 i \operatorname{Sin}[2 c+d x]\right) \right)$$

**Problem 235: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+d x])^{11/2}}{(a+i a \operatorname{Tan}[c+d x])^2} dx$$

Optimal (type 4, 152 leaves, 5 steps):

$$-\frac{14 e^6 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^2 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{14 e^5 \sqrt{e \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{5 a^2 d} + \\ \frac{14 e^3 (e \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{15 a^2 d} - \frac{4 i e^2 (e \operatorname{Sec}[c+d x])^{7/2}}{3 d (a^2+i a^2 \operatorname{Tan}[c+d x])}$$

Result (type 5, 263 leaves):

$$\left( (e \operatorname{Sec}[c+d x])^{11/2} (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^2 \left( -\frac{1}{-1+e^{2 i c}} 14 i \sqrt{2} e^{i(c-d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}}} \right. \right. \\ \left. \left. \left( 1+e^{2 i(c+d x)}+(-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]\right) \right) + \right. \\ \left. \frac{1}{6} \operatorname{Csc}[c] \operatorname{Sec}[c+d x]^{5/2} (\operatorname{Cos}[2 c]+i \operatorname{Sin}[2 c]) \right. \\ \left. (36 \operatorname{Cos}[d x]+27 \operatorname{Cos}[2 c+d x]+21 \operatorname{Cos}[2 c+3 d x]+20 i \operatorname{Sin}[d x]-20 i \operatorname{Sin}[2 c+d x]) \right) \Bigg) / \\ (5 d \operatorname{Sec}[c+d x]^{7/2} (a+i a \operatorname{Tan}[c+d x])^2)$$

**Problem 237: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+d x])^{7/2}}{(a+i a \operatorname{Tan}[c+d x])^2} dx$$

Optimal (type 4, 115 leaves, 4 steps):

$$\frac{6 e^4 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} - \frac{6 e^3 \sqrt{e \sec[c+dx]} \sin[c+dx]}{a^2 d} + \frac{4 i e^2 (e \sec[c+dx])^{3/2}}{d (a^2 + i a^2 \tan[c+dx])}$$

Result (type 5, 80 leaves):

$$\frac{1}{a^2 d} 2 i e^3 e^{-i(c+dx)} \left( -1 + 3 \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \sqrt{e \sec[c+dx]}$$

**Problem 239: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \sec[c+dx])^{3/2}}{(a + i a \tan[c+dx])^2} dx$$

Optimal (type 4, 90 leaves, 3 steps):

$$\frac{2 e^2 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 a^2 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} + \frac{4 i e^2}{5 d \sqrt{e \sec[c+dx]} (a^2 + i a^2 \tan[c+dx])}$$

Result (type 5, 102 leaves):

$$\frac{1}{5 a^2 d} i e^{-3i(c+dx)} \left( 1 + e^{2i(c+dx)} + 2 e^{2i(c+dx)} \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \sqrt{e \sec[c+dx]}$$

**Problem 241: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\sqrt{e \sec[c+dx]} (a + i a \tan[c+dx])^2} dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\frac{2 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{3 a^2 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} + \frac{2 e \sin[c+dx]}{9 a^2 d (e \sec[c+dx])^{3/2}} + \frac{4 i e^2}{9 d (e \sec[c+dx])^{5/2} (a^2 + i a^2 \tan[c+dx])}$$

Result (type 5, 124 leaves):

$$\left( \left( \cos [2 (c+d x)] - i \sin [2 (c+d x)] \right) \left( 4 i - 8 i \cos [2 (c+d x)] + \frac{24 i e^{2 i (c+d x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} + 10 \sin [2 (c+d x)] \right) \right) / \left( 18 a^2 d \sqrt{e \operatorname{Sec}[c+d x]} \right)$$

**Problem 243: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{(e \operatorname{Sec}[c+d x])^{5/2} (a+i a \operatorname{Tan}[c+d x])^2} dx$$

Optimal (type 4, 150 leaves, 5 steps):

$$\frac{42 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{65 a^2 d e^2 \sqrt{\cos [c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{2 e \sin [c+d x]}{13 a^2 d (e \operatorname{Sec}[c+d x])^{7/2}} + \frac{14 \sin [c+d x]}{65 a^2 d e (e \operatorname{Sec}[c+d x])^{3/2}} + \frac{4 i e^2}{13 d (e \operatorname{Sec}[c+d x])^{9/2} (a^2+i a^2 \operatorname{Tan}[c+d x])}$$

Result (type 5, 149 leaves):

$$\left( \left( \cos [2 (c+d x)] - i \sin [2 (c+d x)] \right) \left( 88 i - 256 i \cos [2 (c+d x)] - 8 i \cos [4 (c+d x)] + \frac{672 i e^{2 i (c+d x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} + 316 \sin [2 (c+d x)] + 18 \sin [4 (c+d x)] \right) \right) / \left( 520 a^2 d e^2 \sqrt{e \operatorname{Sec}[c+d x]} \right)$$

**Problem 245: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+d x])^{15/2}}{(a+i a \operatorname{Tan}[c+d x])^3} dx$$

Optimal (type 4, 178 leaves, 6 steps):

$$-\frac{22 e^8 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^3 d \sqrt{\cos [c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} - \frac{22 i e^4 (e \operatorname{Sec}[c+d x])^{7/2}}{21 a^3 d} + \frac{22 e^7 \sqrt{e \operatorname{Sec}[c+d x]} \sin [c+d x]}{5 a^3 d} + \frac{22 e^5 (e \operatorname{Sec}[c+d x])^{5/2} \sin [c+d x]}{15 a^3 d} - \frac{4 i e^2 (e \operatorname{Sec}[c+d x])^{11/2}}{3 a d (a+i a \operatorname{Tan}[c+d x])^2}$$



Result (type 5, 128 leaves):

$$\begin{aligned}
 & -\frac{1}{210 a^3 d} e^6 (e \operatorname{Sec}[c+d x])^{3/2} \left( -116 - 308 \operatorname{Cos}[2(c+d x)] + \right. \\
 & \quad 231 e^{-2 i(c+d x)} (1 + e^{2 i(c+d x)})^{5/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \\
 & \quad \left. 77 i \operatorname{Sec}[c+d x] \operatorname{Sin}[3(c+d x)] + 17 i \operatorname{Tan}[c+d x] \right) (i + \operatorname{Tan}[c+d x])
 \end{aligned}$$

**Problem 247: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+d x])^{11/2}}{(a+i a \operatorname{Tan}[c+d x])^3} dx$$

Optimal (type 4, 141 leaves, 5 steps):

$$\begin{aligned}
 & \frac{14 e^6 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a^3 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{14 i e^4 (e \operatorname{Sec}[c+d x])^{3/2}}{3 a^3 d} - \\
 & \frac{14 e^5 \sqrt{e \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{a^3 d} + \frac{4 i e^2 (e \operatorname{Sec}[c+d x])^{7/2}}{a d (a+i a \operatorname{Tan}[c+d x])^2}
 \end{aligned}$$

Result (type 5, 101 leaves):

$$\begin{aligned}
 & \frac{1}{3 a^3 d} 2 e^5 \sqrt{e \operatorname{Sec}[c+d x]} (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) (i \operatorname{Cos}[d x] + \operatorname{Sin}[d x]) \\
 & \left( -8 + 21 \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + i \operatorname{Tan}[c+d x] \right)
 \end{aligned}$$

**Problem 249: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c+d x])^{7/2}}{(a+i a \operatorname{Tan}[c+d x])^3} dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{6 i e^4}{5 a^3 d \sqrt{e \operatorname{Sec}[c+d x]}} - \frac{6 e^4 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^3 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{e \operatorname{Sec}[c+d x]}} + \frac{4 i e^2 (e \operatorname{Sec}[c+d x])^{3/2}}{5 a d (a+i a \operatorname{Tan}[c+d x])^2}
 \end{aligned}$$

Result (type 5, 117 leaves):

$$\begin{aligned}
 & \left( 2 e e^{-i d x} \left( -2 + \frac{6 e^{2 i(c+d x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]}{\sqrt{1 + e^{2 i(c+d x)}}} \right) \right. \\
 & \quad \left. (e \operatorname{Sec}[c+d x])^{5/2} (\operatorname{Cos}[c+2 d x] + i \operatorname{Sin}[c+2 d x]) \right) / (5 a^3 d (-i + \operatorname{Tan}[c+d x])^3)
 \end{aligned}$$

### Problem 251: Result unnecessarily involves higher level functions.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{3/2}}{(a + i a \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$\frac{2 e^2 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 a^3 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{4 i e^2}{9 a d \sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^2} + \frac{2 i e^2}{45 d \sqrt{e \operatorname{Sec}[c + d x]} (a^3 + i a^3 \operatorname{Tan}[c + d x])}$$

Result (type 5, 140 leaves):

$$-\left( \left( e^{-i d x} \operatorname{Sec}[c + d x]^2 (e \operatorname{Sec}[c + d x])^{3/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \right. \right. \\ \left. \left. \left( 8 + 8 \operatorname{Cos}[2(c + d x)] + 6 e^{2 i (c + d x)} \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + 3 i \operatorname{Sin}[2(c + d x)] \right) \right) \right) / \left( 45 a^3 d (-i + \operatorname{Tan}[c + d x])^3 \right)$$

### Problem 253: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 4, 152 leaves, 5 steps):

$$\frac{14 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{39 a^3 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{14 e \operatorname{Sin}[c + d x]}{117 a^3 d (e \operatorname{Sec}[c + d x])^{3/2}} + \frac{2 i}{13 d \sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^3} + \frac{28 i e^2}{117 d (e \operatorname{Sec}[c + d x])^{5/2} (a^3 + i a^3 \operatorname{Tan}[c + d x])}$$

Result (type 5, 145 leaves):

$$\frac{1}{468 a^3 d e} \sqrt{e \operatorname{Sec}[c + d x]} (i \operatorname{Cos}[3(c + d x)] + \operatorname{Sin}[3(c + d x)]) \\ \left( 62 + 8 \operatorname{Cos}[2(c + d x)] - 54 \operatorname{Cos}[4(c + d x)] + 168 e^{2 i (c + d x)} \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] - 42 i \operatorname{Sin}[2(c + d x)] - 63 i \operatorname{Sin}[4(c + d x)] \right)$$

### Problem 255: Result unnecessarily involves higher level functions.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{15/2}}{(a + i a \operatorname{Tan}[c + d x])^4} dx$$

Optimal (type 4, 192 leaves, 6 steps):

$$\frac{154 e^8 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 a^4 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} - \frac{154 e^7 \sqrt{e \sec[c+dx]} \sin[c+dx]}{5 a^4 d} - \frac{154 e^5 (e \sec[c+dx])^{5/2} \sin[c+dx]}{15 a^4 d} + \frac{4 i e^2 (e \sec[c+dx])^{11/2}}{a d (a + i a \tan[c+dx])^3} + \frac{44 i e^4 (e \sec[c+dx])^{7/2}}{3 d (a^4 + i a^4 \tan[c+dx])}$$

Result (type 5, 135 leaves):

$$\left( 32 i e^7 e^{7 i (c+dx)} \left( -111 - 176 e^{2 i (c+dx)} - 77 e^{4 i (c+dx)} + 231 (1 + e^{2 i (c+dx)})^{5/2} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+dx)}\right] \right) \sqrt{e \sec[c+dx]} \right) / \left( 15 a^4 d (1 + e^{2 i (c+dx)})^6 (-i + \tan[c+dx])^4 \right)$$

**Problem 257: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \sec[c+dx])^{11/2}}{(a + i a \tan[c+dx])^4} dx$$

Optimal (type 4, 163 leaves, 5 steps):

$$-\frac{42 e^6 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 a^4 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} + \frac{42 e^5 \sqrt{e \sec[c+dx]} \sin[c+dx]}{5 a^4 d} + \frac{4 i e^2 (e \sec[c+dx])^{7/2}}{5 a d (a + i a \tan[c+dx])^3} - \frac{28 i e^4 (e \sec[c+dx])^{3/2}}{5 d (a^4 + i a^4 \tan[c+dx])}$$

Result (type 5, 106 leaves):

$$-\frac{1}{5 a^4 d} 2 i e^5 e^{-3 i (c+dx)} \left( -2 - 7 e^{2 i (c+dx)} + 21 e^{2 i (c+dx)} \sqrt{1 + e^{2 i (c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+dx)}\right] \right) \sqrt{e \sec[c+dx]}$$

**Problem 259: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \sec[c+dx])^{7/2}}{(a + i a \tan[c+dx])^4} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$-\frac{2 e^4 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{15 a^4 d \sqrt{\cos[c+dx]} \sqrt{e \sec[c+dx]}} + \frac{4 i e^2 (e \sec[c+dx])^{3/2}}{9 a d (a + i a \tan[c+dx])^3} - \frac{4 i e^4}{15 d \sqrt{e \sec[c+dx]} (a^4 + i a^4 \tan[c+dx])}$$

Result (type 5, 149 leaves):

$$\left( e^3 e^{-i d x} \operatorname{Sec}[c + d x]^4 \sqrt{e \operatorname{Sec}[c + d x]} \left( -7 - 7 \operatorname{Cos}[2(c + d x)] + 6 e^{2 i (c + d x)} \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + 3 i \operatorname{Sin}[2(c + d x)] \right) \right. \\ \left. (-i \operatorname{Cos}[c + 2 d x] + \operatorname{Sin}[c + 2 d x]) \right) / \left( 45 a^4 d (-i + \operatorname{Tan}[c + d x])^4 \right)$$

**Problem 261: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \operatorname{Sec}[c + d x])^{3/2}}{(a + i a \operatorname{Tan}[c + d x])^4} dx$$

Optimal (type 4, 163 leaves, 5 steps):

$$\frac{2 e^2 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{39 a^4 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{2 e^3 \operatorname{Sin}[c + d x]}{117 a^4 d (e \operatorname{Sec}[c + d x])^{3/2}} + \\ \frac{4 i e^2}{13 a d \sqrt{e \operatorname{Sec}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^3} + \frac{4 i e^4}{117 d (e \operatorname{Sec}[c + d x])^{5/2} (a^4 + i a^4 \operatorname{Tan}[c + d x])}$$

Result (type 5, 142 leaves):

$$\left( i e^{-i d x} \operatorname{Sec}[c + d x]^2 (e \operatorname{Sec}[c + d x])^{3/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \right. \\ \left( 28 + 40 \operatorname{Cos}[2(c + d x)] + \frac{24 e^{4 i (c + d x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right]}{\sqrt{1 + e^{2 i (c + d x)}}} + 22 i \operatorname{Sin}[2(c + d x)] \right) \left. \right) / \left( 234 a^4 d (-i + \operatorname{Tan}[c + d x])^4 \right)$$

**Problem 267: Result more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e + f x])^{5/3} (a + i a \operatorname{Tan}[e + f x])^2 dx$$

Optimal (type 5, 71 leaves, 4 steps):

$$\left( 12 i 2^{5/6} a^2 \operatorname{Hypergeometric2F1}\left[-\frac{11}{6}, \frac{5}{6}, \frac{11}{6}, \frac{1}{2} (1 - i \operatorname{Tan}[e + f x])\right] (d \operatorname{Sec}[e + f x])^{5/3} \right) / \\ (5 f (1 + i \operatorname{Tan}[e + f x])^{5/6})$$

Result (type 5, 264 leaves):

$$\frac{1}{16 f \operatorname{Sec}[e+f x]^{11/3} (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^2} \\ (d \operatorname{Sec}[e+f x])^{5/3} \left( -\frac{1}{-1+e^{2 i e}} 33 i 2^{2/3} e^{-i(3 e+f x)} \left( \frac{e^{i(e+f x)}}{1+e^{2 i(e+f x)}} \right)^{2/3} \right. \\ \left. \left( 1+e^{2 i(e+f x)} + (-1+e^{2 i e}) (1+e^{2 i(e+f x)})^{2/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i(e+f x)}\right] \right) + \right. \\ \left. \frac{3}{20} \operatorname{Csc}[e] \operatorname{Sec}[e+f x]^{8/3} (\operatorname{Cos}[2 e] - i \operatorname{Sin}[2 e]) (90 \operatorname{Cos}[f x] + 75 \operatorname{Cos}[2 e+f x] + \right. \\ \left. 55 \operatorname{Cos}[2 e+3 f x] - 64 i \operatorname{Sin}[f x] + 64 i \operatorname{Sin}[2 e+f x]) \right) \left. \right) (a+i a \operatorname{Tan}[e+f x])^2$$

**Problem 278: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e+f x])^{5/3} (a+i a \operatorname{Tan}[e+f x])^2} dx$$

Optimal (type 5, 71 leaves, 4 steps):

$$-\left( \left( 3 i \operatorname{Hypergeometric2F1}\left[-\frac{5}{6}, \frac{23}{6}, \frac{1}{6}, \frac{1}{2} (1-i \operatorname{Tan}[e+f x])\right] \right) (1+i \operatorname{Tan}[e+f x])^{5/6} \right) / \\ \left( 20 \times 2^{5/6} a^2 f (d \operatorname{Sec}[e+f x])^{5/3} \right)$$

Result (type 5, 143 leaves):

$$\left( 3 i \operatorname{Sec}[e+f x]^4 \left( -46 - 40 \operatorname{Cos}[2(e+f x)] + 6 \operatorname{Cos}[4(e+f x)] + 128 e^{2 i(e+f x)} (1+e^{2 i(e+f x)})^{1/3} \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i(e+f x)}\right] - 10 i \operatorname{Sin}[2(e+f x)] + 11 i \operatorname{Sin}[4(e+f x)] \right) \right) / \\ \left( 680 a^2 f (d \operatorname{Sec}[e+f x])^{5/3} (-i + \operatorname{Tan}[e+f x])^2 \right)$$

**Problem 296: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^2 (a+i a \operatorname{Tan}[c+d x])^{3/2} dx$$

Optimal (type 3, 29 leaves, 2 steps):

$$\frac{2 i (a+i a \operatorname{Tan}[c+d x])^{5/2}}{5 a d}$$

Result (type 3, 69 leaves):

$$\frac{1}{5 d} 2 a \operatorname{Sec}[c+d x]^2 (\operatorname{Cos}[d x] - i \operatorname{Sin}[d x]) \\ (-i \operatorname{Cos}[2 c+3 d x] + \operatorname{Sin}[2 c+3 d x]) \sqrt{a+i a \operatorname{Tan}[c+d x]}$$

**Problem 309: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^2 (a + i a \tan [c + d x])^{5/2} dx$$

Optimal (type 3, 29 leaves, 2 steps):

$$\frac{2 i (a + i a \tan [c + d x])^{7/2}}{7 a d}$$

Result (type 3, 73 leaves):

$$\left( 2 a^2 \sec [c + d x]^3 (-i \cos [3 c + 5 d x] + \sin [3 c + 5 d x]) \sqrt{a + i a \tan [c + d x]} \right) / \left( 7 d (\cos [d x] + i \sin [d x])^2 \right)$$

**Problem 322: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^2 (a + i a \tan [c + d x])^{7/2} dx$$

Optimal (type 3, 29 leaves, 2 steps):

$$\frac{2 i (a + i a \tan [c + d x])^{9/2}}{9 a d}$$

Result (type 3, 73 leaves):

$$\left( 2 a^3 \sec [c + d x]^4 (-i \cos [4 c + 7 d x] + \sin [4 c + 7 d x]) \sqrt{a + i a \tan [c + d x]} \right) / \left( 9 d (\cos [d x] + i \sin [d x])^3 \right)$$

**Problem 329: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^5 (a + i a \tan [c + d x])^{7/2} dx$$

Optimal (type 3, 35 leaves, 1 step):

$$\frac{2 i a \cos [c + d x]^5 (a + i a \tan [c + d x])^{5/2}}{5 d}$$

Result (type 3, 73 leaves):

$$\left( 2 a^3 \cos [c + d x]^3 (-i \cos [2 c + 5 d x] + \sin [2 c + 5 d x]) \sqrt{a + i a \tan [c + d x]} \right) / \left( 5 d (\cos [d x] + i \sin [d x])^3 \right)$$

**Problem 394: Result more than twice size of optimal antiderivative.**

$$\int (e \sec [c + d x])^{3/2} \sqrt{a + i a \tan [c + d x]} dx$$

Optimal (type 3, 524 leaves, 12 steps):

$$\begin{aligned}
 & \frac{i a (e \operatorname{Sec}[c+d x])^{3/2}}{d \sqrt{a+i a \operatorname{Tan}[c+d x]}} - \frac{i a^{3/2} e^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a-i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right] \operatorname{Sec}[c+d x]}{\sqrt{2} d \sqrt{a-i a \operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}} + \\
 & \frac{i a^{3/2} e^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a-i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right] \operatorname{Sec}[c+d x]}{\sqrt{2} d \sqrt{a-i a \operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}} + \\
 & \left( i a^{3/2} e^{3/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a-i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a-i a \operatorname{Tan}[c+d x])\right] \right) \\
 & \operatorname{Sec}[c+d x] \Big/ \left( 2 \sqrt{2} d \sqrt{a-i a \operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]} \right) - \\
 & \left( i a^{3/2} e^{3/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a-i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a-i a \operatorname{Tan}[c+d x])\right] \right) \\
 & \operatorname{Sec}[c+d x] \Big/ \left( 2 \sqrt{2} d \sqrt{a-i a \operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]} \right)
 \end{aligned}$$

Result (type 3, 1530 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c+d x] (e \operatorname{Sec}[c+d x])^{3/2} \right. \\
 & \left. \left( i \operatorname{Cos}[c+d x] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} + \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \operatorname{Sin}[c+d x] \right) \right. \\
 & \left. \sqrt{a+i a \operatorname{Tan}[c+d x]} \right) \Big/ \left( d \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \right) + \\
 & \left( (1+i) \left[ \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right] + \right. \right. \\
 & \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right] \right] \operatorname{Cos}[c+d x]^2 (e \operatorname{Sec}[c+d x])^{3/2} \right. \\
 & \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) (i \operatorname{Cos}[c] + \operatorname{Sin}[c]) \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{a+i a \operatorname{Tan}[c+d x]} \right. \\
 & \left. \left. \left( \frac{1}{2} \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} - \frac{1}{2} i \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \operatorname{Tan}[c+d x] \right) \right] \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( d \sqrt{2i - 2 \operatorname{Tan}\left[\frac{dx}{2}\right]} \left( \left( \frac{1}{4} + \frac{i}{4} \right) \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{\sqrt{i - \operatorname{Tan}\left[\frac{dx}{2}\right]}} \right] + \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \operatorname{Tan}\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( i \operatorname{Cos}[c] + \operatorname{Sin}[c] \right) \sqrt{\operatorname{Cos}[dx] + i \operatorname{Sin}[dx]} \right) / \\
 & \left( \sqrt{2i - 2 \operatorname{Tan}\left[\frac{dx}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]} \right) + \\
 & \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{\sqrt{i - \operatorname{Tan}\left[\frac{dx}{2}\right]}} \right] + \right. \\
 & \quad \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \operatorname{Tan}\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \\
 & \quad \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( i \operatorname{Cos}[c] + \operatorname{Sin}[c] \right) \sqrt{\operatorname{Cos}[dx] + i \operatorname{Sin}[dx]} \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]} \right) / \\
 & \left( 2i - 2 \operatorname{Tan}\left[\frac{dx}{2}\right] \right)^{3/2} + \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{\sqrt{i - \operatorname{Tan}\left[\frac{dx}{2}\right]}} \right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right) \\
 & \left. \left( i \cos[c] + \sin[c] \right) \left( i \cos[dx] - \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \\
 & \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( (1+i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( i \cos[c] + \sin[c] \right) \sqrt{\cos[dx] + i \sin[dx]} \right. \\
 & \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \left( i \left( \frac{\sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \right. \right. \right. \right. \\
 & \left. \left. \left( \sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) + \\
 & \left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /
 \end{aligned}$$

$$\left( \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left( i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \left/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \right)$$

**Problem 395: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{e \sec[c + dx]} \sqrt{a + i a \tan[c + dx]} dx$$

Optimal (type 3, 323 leaves, 10 steps):

$$\frac{i \sqrt{2} \sqrt{a} \sqrt{e} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{d} - \frac{i \sqrt{2} \sqrt{a} \sqrt{e} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{d} - \frac{1}{\sqrt{2} d} + \frac{i \sqrt{a} \sqrt{e} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right]}{\sqrt{2} d} + \frac{1}{\sqrt{2} d} i \sqrt{a} \sqrt{e} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right]$$

Result (type 3, 1344 leaves):

$$\left( (1 + i) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - i \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1 - i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sqrt{e \sec[c + dx]} \right) \left/ \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \sqrt{a + i a \tan[c + dx]} \right) \right)$$

$$\begin{aligned}
 & \left( d \sqrt{i - \tan\left[\frac{dx}{2}\right]} \left( \left( \frac{1}{4} + \frac{i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right. \\
 & \quad \left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{2 \cos[dx] + 2i \sin[dx]} \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \right. \\
 & \quad \left( \frac{1}{4} + \frac{i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right. \\
 & \quad \left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} + \right. \\
 & \quad \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right. \right.
 \end{aligned}$$

$$\left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( 2i \cos[dx] - 2 \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) /$$

$$\left( \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) + \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}$$

$$(1 + i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}$$

$$\left( - \left( \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) \right) /$$

$$\left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} +$$

$$\frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2}} \right) /$$

$$\left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right)$$

### Problem 400: Result more than twice size of optimal antiderivative.

$$\int (e \sec [c + d x])^{5/2} (a + i a \tan [c + d x])^{3/2} dx$$

Optimal (type 3, 453 leaves, 13 steps):

$$\frac{7 i a^{3/2} e^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \sec [c+d x]}}\right]}{8 \sqrt{2} d} - \frac{7 i a^{3/2} e^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \sec [c+d x]}}\right]}{8 \sqrt{2} d} - \frac{1}{16 \sqrt{2} d} 7 i a^{3/2} e^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{e \sec [c+d x]}} + \cos [c+d x] (a+i a \tan [c+d x])\right] + \frac{1}{16 \sqrt{2} d} 7 i a^{3/2} e^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{e \sec [c+d x]}} + \cos [c+d x] (a+i a \tan [c+d x])\right] + \frac{7 i a^2 (e \sec [c+d x])^{5/2}}{12 d \sqrt{a+i a \tan [c+d x]}} - \frac{7 i a e^2 \sqrt{e \sec [c+d x]} \sqrt{a+i a \tan [c+d x]}}{8 d} + \frac{i a (e \sec [c+d x])^{5/2} \sqrt{a+i a \tan [c+d x]}}{3 d}$$

Result (type 3, 1537 leaves):

$$\left(\cos [c+d x]^4 (e \sec [c+d x])^{5/2} \left(\sec [c+d x] \left(-\frac{7}{8} i \cos [c] - \frac{7 \sin [c]}{8}\right) + \sec [c+d x]^3 \left(\frac{1}{3} i \cos [c] + \frac{\sin [c]}{3}\right) + \sec [c+d x]^2 \left(\frac{7}{12} i \cos [2 c+d x] + \frac{7}{12} \sin [2 c+d x]\right)\right) (a+i a \tan [c+d x])^{3/2}\right) / (d (\cos [d x] + i \sin [d x])) + \left(\left(\frac{7}{8} + \frac{7 i}{8}\right) \left(\operatorname{ArcTan}\left[\frac{(-1)^{1/4} (\cos [\frac{c}{2}] - i \sin [\frac{c}{2}]) \sqrt{i + \tan [\frac{d x}{2}]}}{\sqrt{i - \tan [\frac{d x}{2}]}}\right] - i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} (\cos [\frac{c}{2}] - i \sin [\frac{c}{2}]) \sqrt{i + \tan [\frac{d x}{2}]}}{\sqrt{-1-i} \sqrt{i - \tan [\frac{d x}{2}]}}\right]\right) \cos [c+d x]^3 (e \sec [c+d x])^{5/2} \left(\cos \left[\frac{3 c}{2}\right] - i \sin \left[\frac{3 c}{2}\right]\right) \left(\frac{7}{16} \cos [c] \sqrt{\cos [d x] + i \sin [d x]} - \frac{7}{16} i \sin [c] \sqrt{\cos [d x] + i \sin [d x]}\right)$$

$$\left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} (a + i a \tan[c + dx])^{3/2} \right/$$

$$\left( d (\cos[dx] + i \sin[dx]) \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right.$$

$$\left. \left( \left( \frac{7}{32} + \frac{7i}{32} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{3c}{2}\right] - \right. \right. \right.$$

$$\left. \left. \left. i \sin\left[\frac{3c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \right) \right/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( \left( \frac{7}{16} + \frac{7i}{16} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - i \operatorname{ArcTan}\left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{-1+i} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{3c}{2}\right] - i \sin\left[\frac{3c}{2}\right] \right) \right.$$

$$\left. \left. \left. \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right/ \left( 2i - 2 \tan\left[\frac{dx}{2}\right] \right)^{3/2} +$$

$$\begin{aligned}
 & \left( \left( \frac{7}{16} + \frac{7i}{16} \right) \left( \text{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] - \right. \right. \\
 & \quad \left. \left. i \text{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right) \right. \\
 & \quad \left. \left( \cos \left[ \frac{3c}{2} \right] - i \sin \left[ \frac{3c}{2} \right] \right) \left( i \cos [dx] - \sin [dx] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) / \\
 & \quad \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{2i - 2 \tan \left[ \frac{dx}{2} \right]} \right) + \\
 & \quad \left( \left( \frac{7}{8} + \frac{7i}{8} \right) \left( \cos \left[ \frac{3c}{2} \right] - i \sin \left[ \frac{3c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \right. \\
 & \quad \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \left( \left( \left( \left( \frac{\sqrt{-1+i} \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left( \sqrt{-1+i} \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)^2 \left( i + \tan \left[ \frac{dx}{2} \right] \right)}{i - \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) + \\
 & \quad \left( \frac{(-1)^{1/4} \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{4 \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]}} + \left( (-1)^{1/4} \sec \left[ \frac{dx}{2} \right]^2 \right. \right.
 \end{aligned}$$

$$\left( \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \Bigg/ \left( \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \Bigg/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \Bigg)$$

**Problem 401: Result more than twice size of optimal antiderivative.**

$$\int (e \sec [c + d x])^{3/2} (a + i a \tan [c + d x])^{3/2} dx$$

Optimal (type 3, 571 leaves, 13 steps):

$$\frac{5 i a^2 (e \sec [c + d x])^{3/2}}{4 d \sqrt{a + i a \tan [c + d x]}} - \frac{5 i a^{5/2} e^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan [c + d x]}}{\sqrt{a} \sqrt{e \sec [c + d x]}}\right] \sec [c + d x]}{4 \sqrt{2} d \sqrt{a - i a \tan [c + d x]} \sqrt{a + i a \tan [c + d x]}} +$$

$$\frac{5 i a^{5/2} e^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan [c + d x]}}{\sqrt{a} \sqrt{e \sec [c + d x]}}\right] \sec [c + d x]}{4 \sqrt{2} d \sqrt{a - i a \tan [c + d x]} \sqrt{a + i a \tan [c + d x]}} +$$

$$\left( 5 i a^{5/2} e^{3/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan [c + d x]}}{\sqrt{e \sec [c + d x]}} + \cos [c + d x] (a - i a \tan [c + d x])\right] \right) \sec [c + d x] \Bigg/ \left( 8 \sqrt{2} d \sqrt{a - i a \tan [c + d x]} \sqrt{a + i a \tan [c + d x]} \right) -$$

$$\left( 5 i a^{5/2} e^{3/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan [c + d x]}}{\sqrt{e \sec [c + d x]}} + \cos [c + d x] (a - i a \tan [c + d x])\right] \right) \sec [c + d x] \Bigg/ \left( 8 \sqrt{2} d \sqrt{a - i a \tan [c + d x]} \sqrt{a + i a \tan [c + d x]} \right) +$$

$$\frac{i a (e \sec [c + d x])^{3/2} \sqrt{a + i a \tan [c + d x]}}{2 d}$$

Result (type 3, 5861 leaves):

$$\left( \cos [c + d x]^3 (e \sec [c + d x])^{3/2} \left( \sec [c + d x]^2 \left( \frac{1}{2} i \cos [c] + \frac{\sin [c]}{2} \right) + \sec [c + d x] \left( \frac{5}{4} i \cos [2 c + d x] + \frac{5}{4} \sin [2 c + d x] \right) \right) (a + i a \tan [c + d x])^{3/2} \right) \Bigg/ \left( d (\cos [d x] + i \sin [d x]) \right) +$$



$$\frac{1}{8 d (\cos [d x] + i \sin [d x])^{3/2}} 5 \cos [c + d x]^3 (e \sec [c + d x])^{3/2}$$

$$\left( \frac{1}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} (1 + i) \cos [c] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [c] \sqrt{\frac{i - \tan \left[ \frac{d x}{2} \right]}{i + \tan \left[ \frac{d x}{2} \right]}} \right.$$

$$\left( \cos \left[ \frac{c}{2} \right] \left( (2 - 2 i) \sqrt{i - \tan \left[ \frac{d x}{2} \right]} - \sqrt{2} \log \left[ \left( (1 + i) \left( 2 - 2 i \cot \left[ \frac{c}{2} \right] \right) \sin \left[ \frac{c}{2} \right]^2 \right. \right. \right.$$

$$\left. \left. \left( \sqrt{2} \sqrt{-1 + \sin [c]} + \sqrt{2} \sqrt{-1 + \sin [c]} \tan \left[ \frac{d x}{2} \right] - 2 \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \right. \right. \right.$$

$$\left. \left. \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \cot \left[ \frac{c}{2} \right] \left( -\sqrt{2} \sqrt{-1 + \sin [c]} + \sqrt{2} \sqrt{-1 + \sin [c]} \tan \left[ \frac{d x}{2} \right] + 2 \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) \right) \right) / \left( \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right.$$

$$\left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( -\sin \left[ \frac{c}{2} \right] \left( -1 + \tan \left[ \frac{d x}{2} \right] \right) + \cos \left[ \frac{c}{2} \right] \left( 1 + \tan \left[ \frac{d x}{2} \right] \right) \right) \right) \right]$$

$$\sqrt{-1 + \sin [c]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \sqrt{2} \log \left[ - \left( (2 - 2 i) \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \right. \right.$$

$$\left. \left( \sin \left[ \frac{c}{2} \right] \left( \sqrt{2} \sqrt{1 + \sin [c]} - \sqrt{2} \sqrt{1 + \sin [c]} \tan \left[ \frac{d x}{2} \right] + \right. \right. \right.$$

$$\left. \left. 2 i \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \cos \left[ \frac{c}{2} \right] \left( \sqrt{2} \sqrt{1 + \sin [c]} + \right. \right. \right.$$

$$\left. \left. \sqrt{2} \sqrt{1 + \sin [c]} \tan \left[ \frac{d x}{2} \right] + 2 i \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) \right) \right) / \left( \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] \left( -1 + \tan \left[ \frac{d x}{2} \right] \right) + \right. \right.$$

$$\left. \left. \sin \left[ \frac{c}{2} \right] \left( 1 + \tan \left[ \frac{d x}{2} \right] \right) \right) \right) \right] \sqrt{1 + \sin [c]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} -$$

$$\begin{aligned}
 & \sin\left[\frac{c}{2}\right] \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ \left(1+i\right) \left(2-2i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \\
 & \left. \left. \left( \sqrt{2} \sqrt{-1+\sin[c]} + \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1+\sin[c]} + \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right] \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \\
 & \sqrt{-1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ - \left( \left(2-2i\right) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} - \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \\
 & \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} + \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right] \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \sqrt{1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1+i) \cos[2c]^2 \cos[dx] \sec[c+dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \left( \cos[dx] + i \sin[dx] \right) \right)
 \end{aligned}$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)$$

$$\left. \left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right)$$

$$\left( \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos[2c] \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right. \right. \right. \right. \right. \right.$$

$$\left( \left( \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} -$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos[2c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( i \cos[dx] - \sin[dx] \right) \right.$$

$$\left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right.$$

$$\left. \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right.$$

$$\left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)$$

$$\left( \left( \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) -$$

$$\frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} (1+i) \cos[2c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]}$$

$$\left( -\frac{\left(\frac{1}{4} + \frac{i}{4}\right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \left( \operatorname{ArcTan}\left[ \right. \right. \right.$$

$$\left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right/ \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right/ \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right/ \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) \right/ \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right)$$

$$(a + i a \operatorname{Tan}[c + d x])^{3/2} - \frac{1}{8 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{3/2}}$$

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$$i \operatorname{Cos}\left[\frac{c + d x}{2}\right]^3$$

$$(e \operatorname{Sec}[c + d x])^{3/2} \left( \frac{1}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right)$$

$$\left(\frac{1}{2} + \frac{i}{2}\right)$$

$$\operatorname{Cos}\left[\frac{c}{2}\right]$$

$$\left(\operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]}$$

$$\left(\operatorname{Cos}\left[\frac{c}{2}\right] \left( (-2 + 2 i) \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} + \right.$$

$$\left. \sqrt{2} \operatorname{Log}\left[\left( (2 + 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left(1 - i \operatorname{Cot}\left[\frac{c}{2}\right]\right) \operatorname{Sin}\left[\frac{c}{2}\right]^2 \left(\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \right.$$

$$\left. \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] - 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} + \operatorname{Cot}\left[\frac{c}{2}\right] \right.$$

$$\left. \left(-\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \right.$$

$$\left. \left. \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right) \right) / \left( \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right) \right)$$

$$\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right) \sqrt{-1 + \operatorname{Sin}[c]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} -$$

$$\sqrt{2} \operatorname{Log}\left[\left( (2 - 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left(\operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Sin}\left[\frac{c}{2}\right] \left(\sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} - \right.$$

$$\left. \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 i \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) +$$

$$\begin{aligned}
 & \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} + \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \quad \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \\
 & \sin\left[\frac{c}{2}\right] \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ (2+2i) \cos\left[\frac{dx}{2}\right] \left(1 - i \cot\left[\frac{c}{2}\right]\right) \right] \right. \\
 & \quad \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1+\sin[c]} + \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] - \right. \\
 & \quad \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1+\sin[c]} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \Bigg/ \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg] \\
 & \sqrt{-1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right] \\
 & \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} - \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \\
 & \quad \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \Bigg/ \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \Bigg) -
 \end{aligned}$$

$$\left( (1+i) \cos [d x] \sec [c+d x] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [2 c]^2 \right.$$

$$\left. (\cos [d x] + i \sin [d x]) \right.$$

$$\left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{d x}{2} \right]} + \right.$$

$$\left. \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \right.$$

$$\left. i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \right.$$

$$\left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) \right) / \left( \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \right.$$

$$\left. \left. \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \sec \left[ \frac{d x}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [2 c] \sqrt{\cos [d x] + i \sin [d x]} \right. \right. \right.$$

$$\left. \left. \left. \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{d x}{2} \right]} + \sqrt{2} \operatorname{ArcTan} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \right. \right.$$



$$\begin{aligned}
 & i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} \right) - \\
 & \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [2c] \left( i \cos [dx] - \sin [dx] \right) \right. \\
 & \left. \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \sqrt{2} \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \right. \right. \\
 & \left. \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right) \right) \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) - \\
 & \frac{1}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [2c] \sqrt{\cos [dx] + i \sin [dx]}
 \end{aligned}$$

$$\left( -\frac{\left(\frac{1}{4} + \frac{i}{4}\right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] / \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i\sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4\sqrt{-1-i} \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2} \right) \right) / \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right) \right)$$

$$\left( \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \left( a + i a \tan[c + dx] \right)^{3/2}$$

### Problem 402: Result more than twice size of optimal antiderivative.

$$\int \sqrt{e \sec[c + dx]} (a + i a \tan[c + dx])^{3/2} dx$$

Optimal (type 3, 364 leaves, 11 steps):

$$\frac{3 i a^{3/2} \sqrt{e} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{\sqrt{2} d} - \frac{3 i a^{3/2} \sqrt{e} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{\sqrt{2} d} - \frac{1}{2 \sqrt{2} d} 3 i a^{3/2} \sqrt{e} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] + \frac{1}{2 \sqrt{2} d} 3 i a^{3/2} \sqrt{e} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] + \frac{i a \sqrt{e \sec[c + dx]} \sqrt{a + i a \tan[c + dx]}}{d}$$

Result (type 3, 1488 leaves):

$$\left( \cos[c + dx] \sqrt{e \sec[c + dx]} \left( i \cos[c] \sqrt{\cos[dx] + i \sin[dx]} + \sin[c] \sqrt{\cos[dx] + i \sin[dx]} \right) (a + i a \tan[c + dx])^{3/2} \right) / \left( d (\cos[dx] + i \sin[dx])^{3/2} \right) + \left( (3 + 3 i) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - i \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1 - i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \cos[c + dx] \sqrt{e \sec[c + dx]} \left( \cos\left[\frac{3c}{2}\right] - i \sin\left[\frac{3c}{2}\right] \right)$$

$$\begin{aligned}
 & \left( \frac{3}{2} \cos[c] \sqrt{\cos[dx] + i \sin[dx]} - \frac{3}{2} i \sin[c] \sqrt{\cos[dx] + i \sin[dx]} \right) \\
 & \sqrt{i + \tan\left[\frac{dx}{2}\right]} (a + i a \tan[c + dx])^{3/2} \Bigg/ \left( d (\cos[dx] + i \sin[dx]) \right) \\
 & \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \left( \left( \frac{3}{4} + \frac{3i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \\
 & \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{3c}{2}\right] - \right. \right. \\
 & \left. \left. i \sin\left[\frac{3c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \right) \Bigg/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( \left( \frac{3}{2} + \frac{3i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \\
 & \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \\
 & \left. \left( \cos\left[\frac{3c}{2}\right] - i \sin\left[\frac{3c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \\
 & \left( 2i - 2 \tan\left[\frac{dx}{2}\right] \right)^{3/2} + \left( \left( \frac{3}{2} + \frac{3i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\cos[\frac{c}{2}] - i \sin[\frac{c}{2}]) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right.
 \end{aligned}$$

$$\left. \begin{aligned} & \left( \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right) \\ & i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \end{aligned} \right)$$

$$\left( \cos\left[\frac{3c}{2}\right] - i \sin\left[\frac{3c}{2}\right] \right) \left( i \cos[dx] - \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) /$$

$$\left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( (3 + 3i) \left( \cos\left[\frac{3c}{2}\right] - i \sin\left[\frac{3c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right)$$

$$\left( - \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} \right) + \right.$$

$$\left. \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{4 \sqrt{-1-i}} \right) \right) /$$

$$\left( \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) +$$

$$\left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right) \right)$$

$$\left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /$$

$$\left( \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left( i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \Bigg/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right)$$

**Problem 403: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[c + dx])^{3/2}}{\sqrt{e \sec[c + dx]}} dx$$

Optimal (type 3, 520 leaves, 12 steps):

$$\frac{i \sqrt{2} a^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx]}{d \sqrt{e} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}} - \frac{i \sqrt{2} a^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx]}{d \sqrt{e} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}} - \left( i a^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right] \sec[c + dx] \right) \Bigg/ \left( \sqrt{2} d \sqrt{e} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) + \left( i a^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right] \sec[c + dx] \right) \Bigg/ \left( \sqrt{2} d \sqrt{e} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) - \frac{4 i a \sqrt{a + i a \tan[c + dx]}}{d \sqrt{e \sec[c + dx]}}$$

Result (type 3, 5881 leaves):

$$\frac{4 i \cos[c] \cos[c + dx] (a + i a \tan[c + dx])^{3/2}}{d \sqrt{e \sec[c + dx]} (\cos[dx] + i \sin[dx])} - \frac{4 \cos[c + dx] \sin[c] (a + i a \tan[c + dx])^{3/2}}{d \sqrt{e \sec[c + dx]} (\cos[dx] + i \sin[dx])} - \frac{1}{d \sqrt{e \sec[c + dx]} (\cos[dx] + i \sin[dx])^{3/2} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left( (1 + i) \cos[c] \cos[c + dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[c] \sqrt{\frac{i - \tan\left[\frac{dx}{2}\right]}{i + \tan\left[\frac{dx}{2}\right]}} \right) \left( \cos\left[\frac{c}{2}\right] \left( (2 - 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \sqrt{2} \operatorname{Log}\left[ (1 + i) \left( 2 - 2i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right.$$

$$\begin{aligned}
 & \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \quad \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \\
 & \quad \left. \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ - \left( \left( 2 - 2i \right) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \\
 & \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. \sqrt{2} \log \left[ \left( (1 + i) \left( 2 - 2i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \cos\left[\frac{c}{2}\right] \left(1 + \tan\left[\frac{dx}{2}\right]\right)\right)\right)\right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{Log}\left[ \right. \\
 & - \left( \left( (2 - 2i) \left(\cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right]\right) \left(\sin\left[\frac{c}{2}\right] \left(\sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}\right) + \cos\left[\frac{c}{2}\right] \left(\sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}\right)\right)\right)\right) \right) / \\
 & \left. \left. \left. \left. \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2}\right] \left(-1 + \tan\left[\frac{dx}{2}\right]\right) + \sin\left[\frac{c}{2}\right] \left(1 + \tan\left[\frac{dx}{2}\right]\right)\right)\right)\right)\right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \\
 & (a + i a \tan[c + dx])^{3/2} + \left( (1 + i) \cos[2c]^2 \cos[dx] \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \right) \\
 & \left( (1 + i) \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \right) \\
 & \left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \\
 & \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \\
 & \left. \left. \left. (a + i a \tan [c + dx])^{3/2} \right) / d \right) \right. \\
 & \frac{\sqrt{e \operatorname{Sec} [c + dx]}}{\sqrt{\cos [dx] + i \sin [dx]}} \\
 & \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \\
 & \left( - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos [2c] \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \right. \right. \\
 & \left. \left. \sqrt{\cos [dx] + i \sin [dx]} \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + \right. \right. \right.
 \end{aligned}$$

$$i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right]$$

$$\left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} \right) -$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos [2c] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( i \cos [dx] - \sin [dx] \right) \right)$$

$$\left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \sqrt{2} \right)$$

$$\operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + i \sqrt{2}$$

$$\left. \left. \left. \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) /$$

$$\left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) - \frac{1}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}}$$

$$(1+i) \cos [2c] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]}$$

$$\left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} + \right)$$

$$\begin{aligned}
 & \frac{\text{ArcTan}\left[\frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \text{Sec}\left[\frac{dx}{2}\right]^2 \sin[c]}{2 \sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \\
 & \left( i \text{ArcTan}\left[\frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \text{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( i \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \text{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left. \left( \sqrt{-1+i} \text{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right. \\
 & \left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) / \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) + \\
 & \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \text{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left. \left( (-1)^{1/4} \text{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \right. \right. \\
 & \left. \left. \left. \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) \right) / \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) +
 \end{aligned}$$

$$\frac{1}{d \sqrt{e \operatorname{Sec}[c + d x]} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{3/2}}$$

$$i \operatorname{Cos}\left[\frac{c + d x}{2}\right]$$

$$\left( \frac{1}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Cos}[2 c] \left(\operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \right.$$

$$\left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] \left( (-2 + 2 i) \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} + \sqrt{2} \operatorname{Log}\left[\left( (2 + 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left(1 - i \operatorname{Cot}\left[\frac{c}{2}\right]\right)\right.\right.\right.\right.\right.$$

$$\left. \left. \operatorname{Sin}\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] - \right.\right.\right.$$

$$\left. \left. 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} + \operatorname{Cot}\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \right.\right.\right.$$

$$\left. \left. \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right) \right) \Bigg/$$

$$\left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \Bigg]$$

$$\sqrt{-1 + \operatorname{Sin}[c]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} - \sqrt{2} \operatorname{Log}\left[\left( (2 - 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left(\operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right]\right)\right)\right]$$

$$\left( \operatorname{Sin}\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} - \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + \right.\right.$$

$$\left. \left. 2 i \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} + \operatorname{Cos}\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} + \right.\right.\right.$$

$$\left. \left. \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 i \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right) \Bigg/$$

$$\left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \Bigg]$$

$$\begin{aligned}
 & \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \sqrt{2} \log \left[ \left( (2 + 2i) \cos\left[\frac{dx}{2}\right] \left( 1 - i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \right. \right. \right. \\
 & \left. \left. \left. \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right] / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \\
 & \sqrt{2} \log \left[ \left( (2 - 2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right] + \\
 & \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right] / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1 + i) \cos[dx] \sec[c + dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c]^2 (\cos[dx] + i \sin[dx]) \right)
 \end{aligned}$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} +$$

$$i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right]$$

$$\left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \left/ \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \right.$$

$$\left. - \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c] \sqrt{\cos[dx] + i \sin[dx]} \right) \right) \right) \right)$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \right. \right.$$

$$\left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right)$$

$$\left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} - \right.$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c] (i \cos[dx] - \sin[dx]) \right.$$

$$\left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right. \right.$$

$$\left. \left. \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right. \right.$$

$$\left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right. \right.$$

$$\left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) -$$

$$\frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c] \sqrt{\cos[dx] + i \sin[dx]}$$

$$\left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[ \right. \right.$$

$$\left( \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \right.$$

$$\left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \left( i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \left( i\sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right.$$

$$\left. \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - \right. \right. \right.$$

$$\left. \left. i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4\sqrt{-1-i} \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /$$

$$\left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right.$$

$$\left. \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right) \right.$$

$$\left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /$$



$$\left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left( i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \left( a + i a \tan[c + dx] \right)^{3/2}$$

**Problem 408: Result more than twice size of optimal antiderivative.**

$$\int (e \sec[c + dx])^{3/2} (a + i a \tan[c + dx])^{5/2} dx$$

Optimal (type 3, 612 leaves, 14 steps):

$$\begin{aligned} & \frac{15 i a^3 (e \sec[c + dx])^{3/2}}{8 d \sqrt{a + i a \tan[c + dx]}} - \frac{15 i a^{7/2} e^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx]}{8 \sqrt{2} d \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}} + \\ & \frac{15 i a^{7/2} e^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx]}{8 \sqrt{2} d \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}} + \\ & \left( \frac{15 i a^{7/2} e^{3/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right]}{\sec[c + dx]} \right) / \left( \frac{16 \sqrt{2} d \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}}{\sec[c + dx]} \right) - \\ & \left( \frac{15 i a^{7/2} e^{3/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right]}{\sec[c + dx]} \right) / \left( \frac{16 \sqrt{2} d \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]}}{\sec[c + dx]} \right) + \\ & \frac{3 i a^2 (e \sec[c + dx])^{3/2} \sqrt{a + i a \tan[c + dx]}}{4 d} + \frac{i a (e \sec[c + dx])^{3/2} (a + i a \tan[c + dx])^{3/2}}{3 d} \end{aligned}$$

Result (type 3, 5917 leaves):

$$\begin{aligned} & \left( \cos[c + dx]^4 (e \sec[c + dx])^{3/2} \left( \sec[c + dx]^2 \left( \frac{17}{12} i \cos[2c] + \frac{17}{12} \sin[2c] \right) + \right. \right. \\ & \quad \sec[c + dx]^3 \left( -\frac{1}{3} i \cos[3c + dx] - \frac{1}{3} \sin[3c + dx] \right) + \\ & \quad \left. \left. \sec[c + dx] \left( \frac{15}{8} i \cos[3c + dx] + \frac{15}{8} \sin[3c + dx] \right) \right) (a + i a \tan[c + dx])^{5/2} \right) / \\ & \left( d (\cos[dx] + i \sin[dx])^2 \right) + \frac{1}{16 d (\cos[dx] + i \sin[dx])^{5/2}} \\ & 15 \cos[c + dx]^4 (e \sec[c + dx])^{3/2} \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left(\frac{1}{2} + \frac{i}{2}\right) (1 + 2 \cos[2c]) \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sin[c] \sqrt{\frac{i - \tan\left[\frac{dx}{2}\right]}{i + \tan\left[\frac{dx}{2}\right]}} \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] \left( (2 - 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \sqrt{2} \log\left[\left(1 + i\right) \left(2 - 2i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right. \right. \\
 & \left. \left. \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[-\left( (2 - 2i) \left(\cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right]\right) \right. \right. \right. \\
 & \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \\
 & \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \\
 & \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[\left(1 + i\right) \left(2 - 2i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right. \\
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \quad \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] \right. \right. \\
 & \quad \left. \left. + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \\
 & \quad \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ - \left( (2 - 2i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1 + i) \cos[3c]^2 \cos[dx] \sec[c + dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. \left( (1 + i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + \\
 & i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right. \\
 & \left. \left. \left. \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos [3c] \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \right. \right. \right. \\
 & \left. \left. \left. \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \sqrt{2} \operatorname{ArcTan} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + \right. \right. \right. \\
 & \left. \left. \left. \left. i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) \right) / \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} \right) -
 \end{aligned}$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos[3c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( i \cos[dx] - \sin[dx] \right) \right.$$

$$\left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right.$$

$$\left. \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right.$$

$$\left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)$$

$$\left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) -$$

$$\frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} (1+i) \cos[3c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]}$$

$$\left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[ \right.$$

$$\left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \right)$$

$$\sqrt{i + \tan\left[\frac{dx}{2}\right]} + \left( i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \right)$$

$$\operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \Bigg/ \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( i\sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right.$$

$$\left. \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( 4\sqrt{-1-i} \right.$$

$$\left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \Bigg/ \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right.$$

$$\left. \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( 4 \right.$$

$$\left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \Bigg/ \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \Bigg) \Bigg) \Bigg) \Bigg)$$

$$(a + i a \tan[c + dx])^{5/2} - \frac{1}{16 d (\cos[dx] + i \sin[dx])^{5/2}}$$

15  
i  
Cos [  
c +  
d

$$\begin{aligned}
 & x]^4 \\
 & (e \operatorname{Sec}[c + d x])^{3/2} \left( \frac{1}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right. \\
 & \left. \left( \frac{1}{2} + \frac{i}{2} \right) \right. \\
 & \operatorname{Cos}[c] \\
 & (-1 + 2 \operatorname{Cos}[2 c]) \\
 & \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \right. \\
 & \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] \left( (-2 + 2 i) \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} + \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \operatorname{Log}\left[ \left( (2 + 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left( 1 - i \operatorname{Cot}\left[\frac{c}{2}\right] \right) \operatorname{Sin}\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] - 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} + \operatorname{Cot}\left[\frac{c}{2}\right] \right. \right. \right. \right. \\
 & \left. \left. \left. \left( -\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right] \right) \right) \right) / \left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right) \\
 & \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \sqrt{-1 + \operatorname{Sin}[c]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} - \\
 & \left. \sqrt{2} \operatorname{Log}\left[ \left( (2 - 2 i) \operatorname{Cos}\left[\frac{d x}{2}\right] \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Sin}\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} - \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 i \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right) \right] + \right. \\
 & \left. \operatorname{Cos}\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 i \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right]
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \\
 \sin\left[\frac{c}{2}\right] & \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ \left( (2+2i) \cos\left[\frac{dx}{2}\right] \left( 1 - i \cot\left[\frac{c}{2}\right] \right) \right. \right. \right. \right. \\
 & \left. \left. \left. \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - \right. \right. \right. \right. \\
 & \left. \left. \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 \sqrt{-1 + \sin[c]} & \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ \left( (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \right. \\
 & \left. \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \right. \\
 & \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \right. \right. \right. \\
 & \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) -
 \end{aligned}$$



$$\left( (1+i) \cos[dx] \sec[c+dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[3c]^2 \right.$$

$$\left. (\cos[dx] + i \sin[dx]) \right.$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right.$$

$$\left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right)$$

$$\left( - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[3c] \sqrt{\cos[dx] + i \sin[dx]} \right) \right.$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \right. \right.$$

$$\left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\begin{aligned}
 & i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} \right) - \\
 & \left( \left( \frac{1+i}{2} \right) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [3c] (i \cos [dx] - \sin [dx]) \right. \\
 & \left. \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \sqrt{2} \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \right. \right. \right. \\
 & \left. \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right) \right) - \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) - \\
 & \frac{1}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [3c] \sqrt{\cos [dx] + i \sin [dx]}
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{\left(\frac{1}{4} + \frac{i}{4}\right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \right. \\
 & \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i\sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right. \\
 & \left. \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - \right. \right. \right. \\
 & \left. \left. \left. i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4\sqrt{-1-i} \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2} \right) \right) / \\
 & \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right. \\
 & \left. \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right.
 \end{aligned}$$

$$\left( \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \left( a + i a \tan[c + dx] \right)^{5/2}$$

**Problem 409: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{e \operatorname{Sec}[c + dx]} (a + i a \tan[c + dx])^{5/2} dx$$

Optimal (type 3, 411 leaves, 12 steps):

$$\frac{21 i a^{5/2} \sqrt{e} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + dx]}}\right]}{4 \sqrt{2} d} - \frac{21 i a^{5/2} \sqrt{e} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + dx]}}\right]}{4 \sqrt{2} d} - \frac{1}{8 \sqrt{2} d} 21 i a^{5/2} \sqrt{e} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \operatorname{Sec}[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] + \frac{1}{8 \sqrt{2} d} 21 i a^{5/2} \sqrt{e} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \operatorname{Sec}[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] + \frac{7 i a^2 \sqrt{e \operatorname{Sec}[c + dx]} \sqrt{a + i a \tan[c + dx]}}{4 d} + \frac{i a \sqrt{e \operatorname{Sec}[c + dx]} (a + i a \tan[c + dx])^{3/2}}{2 d}$$

Result (type 3, 1521 leaves):

$$\left( \cos[c + dx]^3 \sqrt{e \operatorname{Sec}[c + dx]} \left( \operatorname{Sec}[c + dx] \left( \frac{11}{4} i \cos[2c] + \frac{11}{4} \sin[2c] \right) + \operatorname{Sec}[c + dx]^2 \left( -\frac{1}{2} i \cos[3c + dx] - \frac{1}{2} \sin[3c + dx] \right) \right) \right) / \left( d (\cos[dx] + i \sin[dx])^2 \right) + \left( \left( \frac{21}{4} + \frac{21 i}{4} \right) \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) -$$

$$\begin{aligned}
 & \left. i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right) \\
 & \cos [c + dx]^2 \sqrt{e \operatorname{Sec} [c + dx]} \left( \cos \left[ \frac{5c}{2} \right] - i \sin \left[ \frac{5c}{2} \right] \right) \\
 & \left( \frac{21}{8} \cos [2c] \sqrt{\cos [dx] + i \sin [dx]} - \frac{21}{8} i \sin [2c] \sqrt{\cos [dx] + i \sin [dx]} \right) \\
 & \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} (a + i a \tan [c + dx])^{5/2} \right) / \\
 & \left( d (\cos [dx] + i \sin [dx])^2 \sqrt{2i - 2 \tan \left[ \frac{dx}{2} \right]} \right. \\
 & \left. \left( \left( \frac{21}{16} + \frac{21i}{16} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] - \right. \right. \right. \\
 & \left. \left. i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right) \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{5c}{2} \right] - \right. \right. \\
 & \left. \left. i \sin \left[ \frac{5c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \right) / \left( \sqrt{2i - 2 \tan \left[ \frac{dx}{2} \right]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) + \\
 & \left( \left( \frac{21}{8} + \frac{21i}{8} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] - i \operatorname{ArcTan} \left[ \right. \right. \right.
 \end{aligned}$$

$$\left. \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{5c}{2}\right] - i \sin\left[\frac{5c}{2}\right] \right)$$

$$\sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \Big/ \left( 2i - 2 \tan\left[\frac{dx}{2}\right] \right)^{3/2} +$$

$$\left( \frac{21}{8} + \frac{21i}{8} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right.$$

$$\left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)$$

$$\left( \cos\left[\frac{5c}{2}\right] - i \sin\left[\frac{5c}{2}\right] \right) \left( i \cos[dx] - \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \Big/$$

$$\left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( \frac{21}{4} + \frac{21i}{4} \right) \left( \cos\left[\frac{5c}{2}\right] - i \sin\left[\frac{5c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]}$$

$$\sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \left( \left( \left( \frac{\sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \right. \right. \right.$$

$$\left. \left. \left. \left( \sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Big/ \left( 4 \sqrt{-1-i} \right) \right. \right. \right.$$

$$\left( \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \left/ \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right. +$$

$$\left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \right.$$

$$\left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \left/ \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right. \left/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \right)$$

$$\left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \left/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \right)$$

**Problem 410: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[c + dx])^{5/2}}{\sqrt{e \sec[c + dx]}} dx$$

Optimal (type 3, 563 leaves, 13 steps):

$$\frac{5 i a^{7/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{\sqrt{2} d \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} -$$

$$\frac{5 i a^{7/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{\sqrt{2} d \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} -$$

$$\left(5 i a^{7/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x])\right]\right)$$

$$\operatorname{Sec}[c + d x] \Big/ \left(2 \sqrt{2} d \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}\right) +$$

$$\left(5 i a^{7/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x])\right]\right)$$

$$\operatorname{Sec}[c + d x] \Big/ \left(2 \sqrt{2} d \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}\right) -$$

$$\frac{10 i a^2 \sqrt{a + i a \operatorname{Tan}[c + d x]}}{d \sqrt{e \operatorname{Sec}[c + d x]}} + \frac{i a (a + i a \operatorname{Tan}[c + d x])^{3/2}}{d \sqrt{e \operatorname{Sec}[c + d x]}}$$

Result (type 3, 5863 leaves):

$$\frac{\left(\operatorname{Cos}[c + d x]^2 (-8 i \operatorname{Cos}[2 c] - 8 \operatorname{Sin}[2 c] + \operatorname{Sec}[c + d x] (-i \operatorname{Cos}[3 c + d x] - \operatorname{Sin}[3 c + d x]))\right)}{\left(a + i a \operatorname{Tan}[c + d x]\right)^{5/2}} \Big/ \left(d \sqrt{e \operatorname{Sec}[c + d x]} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^2\right) -$$

$$\frac{1}{2 d \sqrt{e \operatorname{Sec}[c + d x]} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2}} 5 \operatorname{Cos}[c + d x]^2$$

$$\left(\frac{1}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \left(\frac{1}{2} + \frac{i}{2}\right) (1 + 2 \operatorname{Cos}[2 c]) \left(\operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \operatorname{Sin}[c] \sqrt{\frac{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}\right)$$

$$\left(\operatorname{Cos}\left[\frac{c}{2}\right] \left((2 - 2 i) \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} - \sqrt{2} \operatorname{Log}\left[\left(1 + i\right) \left(2 - 2 i \operatorname{Cot}\left[\frac{c}{2}\right]\right) \operatorname{Sin}\left[\frac{c}{2}\right]^2\right.\right.\right)$$

$$\left.\left.\left(\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] - 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}\right.\right.\right)$$

$$\left.\left.\left.\sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} + \operatorname{Cot}\left[\frac{c}{2}\right] \left(-\sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] + 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}\right)\right)\right) \Big/ \left(\left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)\right)$$



$$\begin{aligned}
 & \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ - \left( (2 - 2i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \\
 & \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right] \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \\
 & \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ \left( (1 + i) \left( 2 - 2i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right. \right. \\
 & \left. \left. \left. \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right] \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right) \\
 & \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ - \left( (2 - 2i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \\
 & \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left(-1 + \tan\left[\frac{dx}{2}\right]\right) + \right. \right. \\
 & \left. \left. \sin\left[\frac{c}{2}\right] \left(1 + \tan\left[\frac{dx}{2}\right]\right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \Bigg) - \\
 & \left( (1 + i) \cos[3c]^2 \cos[dx] \sec[c + dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. (\cos[dx] + i \sin[dx]) \right. \\
 & \left. \left( (1 + i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \right. \\
 & \left. \left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \\
 & \left. \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1 - i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \right) / \\
 & \left( \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \\
 & - \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos[3c] \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \right) \right)
 \end{aligned}$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \Bigg) -$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos[3c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) (i \cos[dx] - \sin[dx]) \right.$$

$$\left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right. \right.$$

$$\left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \sin [c] \sqrt{i + \tan \left[\frac{dx}{2}\right]} \right) \right) \right) / \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[\frac{dx}{2}\right]} \right) - \\
 & \frac{1}{\sqrt{i - \tan \left[\frac{dx}{2}\right]}} (1 + i) \cos [3c] \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right) \sqrt{\cos [dx] + i \sin [dx]} \\
 & \left( -\frac{\left(\frac{1}{4} + \frac{i}{4}\right) \sec \left[\frac{dx}{2}\right]^2 \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan \left[\frac{dx}{2}\right]}} + \operatorname{ArcTan} \left[ \right. \right. \\
 & \left. \left. \frac{(-1)^{1/4} \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right) \sqrt{i + \tan \left[\frac{dx}{2}\right]}}{\sqrt{i - \tan \left[\frac{dx}{2}\right]}} \right] \sec \left[\frac{dx}{2}\right]^2 \sin [c] \right) / \left( 2\sqrt{2} \right. \\
 & \left. \left. \sqrt{i + \tan \left[\frac{dx}{2}\right]} \right) + \left( i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right) \sqrt{i + \tan \left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[\frac{dx}{2}\right]}} \right] \right. \right. \\
 & \left. \left. \sec \left[\frac{dx}{2}\right]^2 \sin [c] \right) / \left( 2\sqrt{2} \sqrt{i + \tan \left[\frac{dx}{2}\right]} \right) + \right. \\
 & \left( i \sqrt{2} \sin [c] \sqrt{i + \tan \left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \sec \left[\frac{dx}{2}\right]^2 \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan \left[\frac{dx}{2}\right]}} \sqrt{i + \tan \left[\frac{dx}{2}\right]} \right) \right. \\
 & \left. \left. \left( \sqrt{-1+i} \sec \left[\frac{dx}{2}\right]^2 \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right) \sqrt{i + \tan \left[\frac{dx}{2}\right]} \right) \right) / \left( 4 \sqrt{-1-i} \right. \right. \\
 & \left. \left. \left( i - \tan \left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos \left[\frac{c}{2}\right] - i \sin \left[\frac{c}{2}\right] \right)^2 \left( i + \tan \left[\frac{dx}{2}\right] \right)}{i - \tan \left[\frac{dx}{2}\right]} \right) \right) +
 \end{aligned}$$

$$\left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\ \left. \left. \left( (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \right. \right. \right. \\ \left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right)$$

$$(a + i a \tan[c + dx])^{5/2} + \frac{1}{2 d \sqrt{e} \sec[c + dx] (\cos[dx] + i \sin[dx])^{5/2}}$$

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$$i \cos\left[\frac{c + dx}{x^2}\right]$$

$$\left( \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left( \frac{1}{2} + \frac{i}{2} \right) \cos[c] (-1 + 2 \cos[2c]) \right)$$

$$\frac{\left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{\sqrt{\cos[dx] + i \sin[dx]}}$$

$$\left( \cos\left[\frac{c}{2}\right] \left( (-2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \right)$$

$$\left. \sqrt{2} \log\left[ \left( (2 + 2i) \cos\left[\frac{dx}{2}\right] \left( 1 - i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \right)$$

$$\left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \right) \right) \right)$$

$$\left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \\
 & \sqrt{2} \operatorname{Log}\left[ \left( (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right. \right. \\
 & \left. \left. \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) \right) / \\
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \\
 & \sin\left[\frac{c}{2}\right] \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{Log}\left[ \left( (2+2i) \cos\left[\frac{dx}{2}\right] \left( 1 - i \cot\left[\frac{c}{2}\right] \right) \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{Log}\left[ \left( (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right) \right]
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} - \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \\
 & \quad \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} + \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1+i) \cos[dx] \sec[c+dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[3c]^2 \right. \\
 & \quad \left. (\cos[dx] + i \sin[dx]) \right) \\
 & \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \quad \left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \quad \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \\
 & \quad \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \operatorname{Sin} [3c] \sqrt{\operatorname{Cos} [dx] + i \operatorname{Sin} [dx]} \right. \right. \\
 & \left. \left( (1+i) \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \sqrt{i - \operatorname{Tan} \left[ \frac{dx}{2} \right]} + \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \sqrt{i + \operatorname{Tan} \left[ \frac{dx}{2} \right]}}{\sqrt{i - \operatorname{Tan} \left[ \frac{dx}{2} \right]}} \right] \operatorname{Sin} [c] \sqrt{i + \operatorname{Tan} \left[ \frac{dx}{2} \right]} + \right. \right. \\
 & \left. \left. i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \sqrt{i + \operatorname{Tan} \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \operatorname{Tan} \left[ \frac{dx}{2} \right]}} \right] \right) \right) \left. \right) / \left( i - \operatorname{Tan} \left[ \frac{dx}{2} \right] \right)^{3/2} - \\
 & \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \operatorname{Sin} [3c] (i \operatorname{Cos} [dx] - \operatorname{Sin} [dx]) \right. \\
 & \left. \left( (1+i) \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \sqrt{i - \operatorname{Tan} \left[ \frac{dx}{2} \right]} + \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - i \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \sqrt{i + \operatorname{Tan} \left[ \frac{dx}{2} \right]}}{\sqrt{i - \operatorname{Tan} \left[ \frac{dx}{2} \right]}} \right] \operatorname{Sin} [c] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]} + \mathbf{i} \sqrt{2} \operatorname{ArcTan}\left[\frac{\sqrt{-1+\mathbf{i}} \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right) \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-\mathbf{i}} \sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]}}\right] \\
 & \left. \sin[c] \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( \sqrt{\cos[dx] + \mathbf{i} \sin[dx]} \sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \frac{1}{\sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]}} (1 + \mathbf{i}) \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right) \sin[3c] \sqrt{\cos[dx] + \mathbf{i} \sin[dx]} \\
 & \left( -\frac{\left(\frac{1}{4} + \frac{\mathbf{i}}{4}\right) \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right)}{\sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right) \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]}}{\sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]}} \right] \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) \Bigg/ \left( 2\sqrt{2} \right. \\
 & \left. \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]} \right) + \left( \mathbf{i} \operatorname{ArcTan}\left[\frac{\sqrt{-1+\mathbf{i}} \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right) \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-\mathbf{i}} \sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]}}\right] \right. \\
 & \left. \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) \Bigg/ \left( 2\sqrt{2} \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]} \right) + \left( \mathbf{i} \sqrt{2} \sin[c] \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]} \right. \\
 & \left. \frac{\sqrt{-1+\mathbf{i}} \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - \mathbf{i} \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-\mathbf{i}} \sqrt{\mathbf{i} - \tan\left[\frac{dx}{2}\right]} \sqrt{\mathbf{i} + \tan\left[\frac{dx}{2}\right]}} + \left( \sqrt{-1+\mathbf{i}} \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \frac{i \sin\left[\frac{c}{2}\right] \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\left(4\sqrt{-1-i} \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2}\right)} \right) \right) \right) \right) \right) /$$

$$\left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right.$$

$$\left. \left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} \right) + \left( (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \right.$$

$$\left. \left. \left. \left. \left. \frac{\left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\left(4 \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2}\right)} \right) \right) \right) \right) \right) /$$

$$\left. \left. \left. \left. \left. \left. \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) \right) \left( a + i a \tan[c + dx] \right)^{5/2}$$

Problem 411: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[c + dx])^{5/2}}{(e \sec[c + dx])^{3/2}} dx$$

Optimal (type 3, 362 leaves, 11 steps):

$$\frac{i \sqrt{2} a^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{d e^{3/2}} + \frac{i \sqrt{2} a^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right]}{d e^{3/2}} +$$

$$\frac{1}{\sqrt{2} d e^{3/2}} i a^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] -$$

$$\frac{1}{\sqrt{2} d e^{3/2}} i a^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a + i a \tan[c + dx])\right] -$$

$$\frac{4 i a (a + i a \tan[c + dx])^{3/2}}{3 d (e \sec[c + dx])^{3/2}}$$

Result (type 3, 1571 leaves):

$$\left( \cos [c+d x] \left( \cos [d x] \left( -\frac{4}{3} i \cos [c] - \frac{4 \sin [c]}{3} \right) + \left( \frac{4 \cos [c]}{3} - \frac{4}{3} i \sin [c] \right) \sin [d x] \right) \right. \\ \left. (a+i a \tan [c+d x])^{5/2} \right) / \left( d \left( e \sec [c+d x] \right)^{3/2} (\cos [d x]+i \sin [d x])^2 \right) -$$

$$\left( (1+i) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i+\tan \left[ \frac{d x}{2} \right]}}{\sqrt{i-\tan \left[ \frac{d x}{2} \right]}} \right] - \right.$$

$$\left. i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i+\tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1-i} \sqrt{i-\tan \left[ \frac{d x}{2} \right]}} \right] \right)$$

$$\left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) (\cos [2 c] - i \sin [2 c]) \\ \left( -\cos [2 c] \sqrt{\cos [d x]+i \sin [d x]} + i \sin [2 c] \sqrt{\cos [d x]+i \sin [d x]} \right)$$

$$\left. \sqrt{2 \cos [d x]+2 i \sin [d x]} \sqrt{i+\tan \left[ \frac{d x}{2} \right]} (a+i a \tan [c+d x])^{5/2} \right) /$$

$$\left( d \left( e \sec [c+d x] \right)^{3/2} (\cos [d x]+i \sin [d x])^{5/2} \sqrt{i-\tan \left[ \frac{d x}{2} \right]} \right)$$

$$\left( - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i+\tan \left[ \frac{d x}{2} \right]}}{\sqrt{i-\tan \left[ \frac{d x}{2} \right]}} \right] - \right.$$

$$\left. i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i+\tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1-i} \sqrt{i-\tan \left[ \frac{d x}{2} \right]}} \right] \right)$$

$$\sec \left[ \frac{d x}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) (\cos [2 c] - i \sin [2 c])$$

$$\left. \sqrt{2 \cos [d x] + 2 i \sin [d x]} \right) / \left( \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) -$$

$$\left( \frac{1}{4} + \frac{i}{4} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] - i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \right) \operatorname{Sec} \left[ \frac{d x}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)$$

$$\left( \cos [2 c] - i \sin [2 c] \right) \sqrt{2 \cos [d x] + 2 i \sin [d x]} \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) /$$

$$\left( i - \tan \left[ \frac{d x}{2} \right] \right)^{3/2} - \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] - i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \right) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)$$

$$\left( \cos [2 c] - i \sin [2 c] \right) \left( 2 i \cos [d x] - 2 \sin [d x] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) /$$

$$\left( \sqrt{2 \cos [d x] + 2 i \sin [d x]} \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \right) - \frac{1}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}}$$

$$(1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( \cos [2 c] - i \sin [2 c] \right) \sqrt{2 \cos [d x] + 2 i \sin [d x]}$$

$$\begin{aligned}
 & \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( - \left( \left( \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right)}{4 \sqrt{-1-i}} \right) \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left( \frac{\left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2}}{1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]}} \right) \right) \right) \right) \right) + \\
 & \left( \frac{\left(-1\right)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \\
 & \left. \frac{\left(-1\right)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{4 \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2}} \right) / \\
 & \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 416: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(e \operatorname{Sec}[c + dx]\right)^{5/2}}{\sqrt{a + i a \tan[c + dx]}} dx$$

Optimal (type 3, 369 leaves, 11 steps):

$$\frac{i e^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} \sqrt{a} d} - \frac{i e^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} \sqrt{a} d} - \frac{1}{2 \sqrt{2} \sqrt{a} d}$$

$$+ i e^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right] +$$

$$\frac{1}{2 \sqrt{2} \sqrt{a} d} i e^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right] -$$

$$\frac{i e^2 \sqrt{e \operatorname{Sec}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{a d}$$

Result (type 3, 1531 leaves):

$$\left(\operatorname{Cos}[c+d x] (e \operatorname{Sec}[c+d x])^{5/2} \left(-i \operatorname{Cos}[c] \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]} + \operatorname{Sin}[c] \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]}\right) \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]}\right) / \left(d \sqrt{a+i a \operatorname{Tan}[c+d x]}\right) +$$

$$\left((1+i) \left(\operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\operatorname{Cos}\left[\frac{c}{2}\right]-i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i+\operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{i-\operatorname{Tan}\left[\frac{d x}{2}\right]}}\right] - i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\operatorname{Cos}\left[\frac{c}{2}\right]-i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i+\operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{-1-i} \sqrt{i-\operatorname{Tan}\left[\frac{d x}{2}\right]}}\right]\right)$$

$$\operatorname{Cos}[c+d x] (e \operatorname{Sec}[c+d x])^{5/2} \left(\operatorname{Cos}\left[\frac{c}{2}\right]-i \operatorname{Sin}\left[\frac{c}{2}\right]\right) (\operatorname{Cos}[c]+i \operatorname{Sin}[c]) \left(\frac{1}{2} \operatorname{Cos}[c] \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]} + \frac{1}{2} i \operatorname{Sin}[c] \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]}\right) \sqrt{\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]}\right) / \left(d \sqrt{2 i-2 \operatorname{Tan}\left[\frac{d x}{2}\right]}\right)$$

$$\left(\left(\frac{1}{4} + \frac{i}{4}\right) \left(\operatorname{ArcTan}\left[\frac{(-1)^{1/4} \left(\operatorname{Cos}\left[\frac{c}{2}\right]-i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i+\operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{i-\operatorname{Tan}\left[\frac{d x}{2}\right]}}\right] - i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\operatorname{Cos}\left[\frac{c}{2}\right]-i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i+\operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{-1-i} \sqrt{i-\operatorname{Tan}\left[\frac{d x}{2}\right]}}\right]\right)$$

$$\left. \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)$$

$$\left( \cos[c] + i \sin[c] \right) \sqrt{\cos[dx] + i \sin[dx]} \left/ \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \right.$$

$$\left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right.$$

$$\left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \sec\left[\frac{dx}{2}\right]^2$$

$$\left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( \cos[c] + i \sin[c] \right) \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left/ \right.$$

$$\left( 2i - 2 \tan\left[\frac{dx}{2}\right] \right)^{3/2} + \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right.$$

$$\left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)$$

$$\left( \cos[c] + i \sin[c] \right) \left( i \cos[dx] - \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left/ \right.$$

$$\left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) (\cos[c] + i \sin[c]) \sqrt{\cos[dx] + i \sin[dx]} \right.$$

$$\sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right.$$

$$\left. \left. \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right.$$

$$\left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) +$$

$$\left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right.$$

$$\left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /$$

$$\left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) /$$

$$\left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \sqrt{a + i a \tan[c + dx]}$$



### Problem 417: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{3/2}}{\sqrt{a + i a \operatorname{Tan}[c + d x]}} dx$$

Optimal (type 3, 483 leaves, 11 steps):

$$\begin{aligned} & \frac{i \sqrt{2} \sqrt{a} e^{3/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} + \\ & \frac{i \sqrt{2} \sqrt{a} e^{3/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} + \\ & \left( i \sqrt{a} e^{3/2} \operatorname{Log}\left[ a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x]) \right] \right. \\ & \quad \left. \operatorname{Sec}[c + d x] \right) / \left( \sqrt{2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) - \\ & \left( i \sqrt{a} e^{3/2} \operatorname{Log}\left[ a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x]) \right] \right. \\ & \quad \left. \operatorname{Sec}[c + d x] \right) / \left( \sqrt{2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) \end{aligned}$$

Result (type 3, 1683 leaves):

$$\begin{aligned} & \left( (1 + i) \left( -i \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right] + \right. \right. \\ & \quad \left. \left. \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}{\sqrt{-1 - i} \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}} \right] \right) \right) \\ & \operatorname{Cos}[c + d x] (e \operatorname{Sec}[c + d x])^{3/2} \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \\ & \left( \operatorname{Cos}[d x] \operatorname{Sec}[c + d x] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} - i \operatorname{Sec}[c + d x] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \operatorname{Sin}[d x] \right) \\ & \left. \sqrt{2 i - 2 \operatorname{Tan}\left[\frac{d x}{2}\right]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) / \end{aligned}$$

$$\left( d \left( -i + \tan\left[\frac{dx}{2}\right] \right) \left( \left( \frac{1}{4} + \frac{i}{4} \right) \left( -i \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] + \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right.$$

$$\left. \left. \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) / \left( \left( -i + \tan\left[\frac{dx}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \right.$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( -i \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] + \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right.$$

$$\left. \left. \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( -i + \tan\left[\frac{dx}{2}\right] \right)^2 - \right.$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( -i \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] + \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right.$$

$$\begin{aligned}
 & \left. \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \left(-i + \tan\left[\frac{dx}{2}\right]\right) \right) + \\
 & \left( \left(\frac{1}{2} + \frac{i}{2}\right) \left( -i \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] + \right. \right. \\
 & \left. \left. \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \\
 & \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( i \cos[dx] - \sin[dx] \right) \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \\
 & \left( \sqrt{\cos[dx] + i \sin[dx]} \left(-i + \tan\left[\frac{dx}{2}\right]\right) \right) + \frac{1}{-i + \tan\left[\frac{dx}{2}\right]} \\
 & (1+i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \\
 & \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left. \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{4 \sqrt{-1-i} \left(i - \tan\left[\frac{dx}{2}\right]\right)^{3/2}} \right) \right) / \left( 1 - \right. \\
 & \left. \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) - \left( i \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right.
 \end{aligned}$$

$$\left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{i + \operatorname{Tan}\left[\frac{dx}{2}\right]}}{4 \left(i - \operatorname{Tan}\left[\frac{dx}{2}\right]\right)^{3/2}} \right) \left/ \left( \left( 1 + \frac{i \left(\operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right]\right)^2 \left(i + \operatorname{Tan}\left[\frac{dx}{2}\right]\right)}{i - \operatorname{Tan}\left[\frac{dx}{2}\right]} \right) \sqrt{a + i a \operatorname{Tan}[c + dx]} \right) \right.$$

**Problem 423: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \operatorname{Sec}[c + dx])^{7/2}}{(a + i a \operatorname{Tan}[c + dx])^{3/2}} dx$$

Optimal (type 3, 529 leaves, 13 steps):

$$\begin{aligned} & - \frac{i e^2 (e \operatorname{Sec}[c + dx])^{3/2}}{a d \sqrt{a + i a \operatorname{Tan}[c + dx]}} - \frac{3 i e^{7/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + dx]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + dx]}}\right] \operatorname{Sec}[c + dx]}{\sqrt{2} \sqrt{a} d \sqrt{a - i a \operatorname{Tan}[c + dx]} \sqrt{a + i a \operatorname{Tan}[c + dx]}} + \\ & \frac{3 i e^{7/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + dx]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + dx]}}\right] \operatorname{Sec}[c + dx]}{\sqrt{2} \sqrt{a} d \sqrt{a - i a \operatorname{Tan}[c + dx]} \sqrt{a + i a \operatorname{Tan}[c + dx]}} + \\ & \left( 3 i e^{7/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + dx]}}{\sqrt{e \operatorname{Sec}[c + dx]}} + \operatorname{Cos}[c + dx] (a - i a \operatorname{Tan}[c + dx])\right] \right) \operatorname{Sec}[c + dx] \left/ \left( 2 \sqrt{2} \sqrt{a} d \sqrt{a - i a \operatorname{Tan}[c + dx]} \sqrt{a + i a \operatorname{Tan}[c + dx]} \right) - \right. \\ & \left. \left( 3 i e^{7/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + dx]}}{\sqrt{e \operatorname{Sec}[c + dx]}} + \operatorname{Cos}[c + dx] (a - i a \operatorname{Tan}[c + dx])\right] \right) \operatorname{Sec}[c + dx] \right/ \left( 2 \sqrt{2} \sqrt{a} d \sqrt{a - i a \operatorname{Tan}[c + dx]} \sqrt{a + i a \operatorname{Tan}[c + dx]} \right) \end{aligned}$$

Result (type 3, 5841 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[c + dx] (e \operatorname{Sec}[c + dx])^{7/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{3/2} \right. \\ & \left. (-i \operatorname{Cos}[c - dx] \sqrt{\operatorname{Cos}[dx] + i \operatorname{Sin}[dx]} + \sqrt{\operatorname{Cos}[dx] + i \operatorname{Sin}[dx]} \operatorname{Sin}[c - dx]) \right) \left/ \right. \\ & \left( d (a + i a \operatorname{Tan}[c + dx])^{3/2} \right) + \frac{1}{2 d (a + i a \operatorname{Tan}[c + dx])^{3/2}} \\ & 3 \operatorname{Cos}[c + dx]^2 (e \operatorname{Sec}[c + dx])^{7/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{3/2} \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left(\frac{1}{2} + \frac{i}{2}\right) \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sin[c] \sqrt{\frac{i - \tan\left[\frac{dx}{2}\right]}{i + \tan\left[\frac{dx}{2}\right]}} \right. \\
 & \quad \left( \cos\left[\frac{c}{2}\right] \left( (2 - 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \sqrt{2} \log\left[ \left(1 + i\right) \left(2 - 2i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \\
 & \quad \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ -\left( \left(2 - 2i\right) \left(\cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right]\right) \right. \right. \right. \\
 & \quad \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \\
 & \quad \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ \left(1 + i\right) \left(2 - 2i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \quad \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \right) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ - \left( \left( 2 - 2i \right) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1 + i) \cos[c]^2 \cos[dx] \sec[c + dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( \cos[dx] + i \sin[dx] \right) \right) \\
 & \left( (1 + i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + \\
 & i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) \\
 & \left( - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos [c] \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \right. \right. \\
 & \left. \left. \left( (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{dx}{2} \right]} + \sqrt{2} \operatorname{ArcTan} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + \right. \right. \\
 & \left. \left. \left. i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right. \right. \right. \\
 & \left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) \right) / \left( i - \tan \left[ \frac{dx}{2} \right] \right)^{3/2} -
 \end{aligned}$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos[c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) (i \cos[dx] - \sin[dx]) \right.$$

$$\left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right. \right.$$

$$\left. \left. \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right. \right.$$

$$\left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right. \right.$$

$$\left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) / \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) -$$

$$\frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} (1+i) \cos[c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]}$$

$$\left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[ \right. \right.$$

$$\left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \right)$$



$$\sqrt{i + \tan\left[\frac{dx}{2}\right]} + \left( i \operatorname{ArcTan}\left[\frac{\sqrt{-1+i} \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}}\right] \right)$$

$$\operatorname{Sec}\left[\frac{dx}{2}\right]^2 \sin[c] \Bigg/ \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( i\sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right.$$

$$\left. \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( 4\sqrt{-1-i} \right.$$

$$\left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \Bigg/ \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) +$$

$$\left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4\sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right.$$

$$\left. \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg/ \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \Bigg/ \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \Bigg) \Bigg) \Bigg) +$$

$$\frac{1}{2d \left(a + i a \tan[c + dx]\right)^{3/2}} 3 i \cos[c + dx]^2 \left(e \operatorname{Sec}[c + dx]\right)^{7/2} \left(\cos\left[\frac{dx}{2}\right] + i \sin\left[\frac{dx}{2}\right]\right)^{3/2}$$

$$\begin{aligned}
 & \left( \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left(\frac{1}{2} + \frac{i}{2}\right) \cos[c] \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \right. \\
 & \quad \sqrt{\cos[dx] + i \sin[dx]} \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] \left( (2 - 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \right. \right. \right. \\
 & \quad \sqrt{2} \log\left[ \left( (2 + 2i) \cos\left[\frac{dx}{2}\right] \left(1 - i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right] \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \\
 & \quad \sqrt{2} \log\left[ \left( (2 - 2i) \cos\left[\frac{dx}{2}\right] \left(\cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right]\right) \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right] + \\
 & \quad \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \\
 & \quad \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} -
 \end{aligned}$$

$$\begin{aligned}
 & \sin\left[\frac{c}{2}\right] \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ (2+2i) \cos\left[\frac{dx}{2}\right] \left(1 - i \cot\left[\frac{c}{2}\right]\right) \right. \right. \\
 & \quad \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] - \right. \\
 & \quad \quad 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \right. \\
 & \quad \quad \quad \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 & \quad \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[ (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \right. \\
 & \quad \quad \left. \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \right. \right. \\
 & \quad \quad \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \quad \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \quad \quad \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) - \\
 & \quad \left( (1+i) \cos[dx] \sec[c+dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[c]^2 \right. \\
 & \quad \left. (\cos[dx] + i \sin[dx]) \right)
 \end{aligned}$$

$$\left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)$$

$$\left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right)$$

$$\left( \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[c] \sqrt{\cos[dx] + i \sin[dx]} \right. \right. \right.$$

$$\left. \left. \left. \left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right. \right.$$

$$\left. \left. \left. \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \right) \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} - \\
 & \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[c] \left( i \cos[dx] - \sin[dx] \right) \right. \\
 & \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right. \\
 & \left. \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \right. \\
 & \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \\
 & \left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[c] \sqrt{\cos[dx] + i \sin[dx]} - \\
 & \left( -\frac{\left(\frac{1}{4} + \frac{i}{4}\right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} + \operatorname{ArcTan}\left[ \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \right. \\
 & \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \left( i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right. \\
 & \left. \sec\left[\frac{dx}{2}\right]^2 \sin[c] \right) / \left( 2\sqrt{2} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( i \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left. \left( \sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right. \\
 & \left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) + \\
 & \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left. \left( (-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \right. \right. \\
 & \left. \left. \left. \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) \right) / \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right)
 \end{aligned}$$

### Problem 424: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{5/2}}{(a + i a \operatorname{Tan}[c + d x])^{3/2}} dx$$

Optimal (type 3, 365 leaves, 11 steps):

$$\begin{aligned} & - \frac{i \sqrt{2} e^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right]}{a^{3/2} d} + \frac{i \sqrt{2} e^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right]}{a^{3/2} d} + \\ & \frac{1}{\sqrt{2} a^{3/2} d} i e^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a + i a \operatorname{Tan}[c + d x])\right] - \\ & \frac{1}{\sqrt{2} a^{3/2} d} i e^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a + i a \operatorname{Tan}[c + d x])\right] + \\ & \frac{4 i e^2 \sqrt{e \operatorname{Sec}[c + d x]}}{a d \sqrt{a + i a \operatorname{Tan}[c + d x]}} \end{aligned}$$

Result (type 3, 1563 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[c + d x] (e \operatorname{Sec}[c + d x])^{5/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^2 \right. \\ & \quad \left. (\operatorname{Cos}[d x] (4 i \operatorname{Cos}[c] - 4 \operatorname{Sin}[c]) + (4 \operatorname{Cos}[c] + 4 i \operatorname{Sin}[c]) \operatorname{Sin}[d x]) \right) / \\ & \left( d (a + i a \operatorname{Tan}[c + d x])^{3/2} - \left( (1 + i) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\operatorname{Cos}[\frac{c}{2}] - i \operatorname{Sin}[\frac{c}{2}]) \sqrt{i + \operatorname{Tan}[\frac{d x}{2}]}}{\sqrt{i - \operatorname{Tan}[\frac{d x}{2}]}} \right] - \right. \right. \\ & \quad \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} (\operatorname{Cos}[\frac{c}{2}] - i \operatorname{Sin}[\frac{c}{2}]) \sqrt{i + \operatorname{Tan}[\frac{d x}{2}]}}{\sqrt{-1 - i} \sqrt{i - \operatorname{Tan}[\frac{d x}{2}]}} \right] \right) \right) \\ & \left( e \operatorname{Sec}[c + d x] \right)^{5/2} \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[2 c] + i \operatorname{Sin}[2 c]) \\ & \left( -\operatorname{Cos}[2 c] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} - i \operatorname{Sin}[2 c] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \right) \\ & \left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{3/2} \sqrt{2 \operatorname{Cos}[d x] + 2 i \operatorname{Sin}[d x]} \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( d \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( \cos[2c] + i \sin[2c] \right) \right. \\
 & \left. \left. \sqrt{2 \cos[dx] + 2i \sin[dx]} \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) - \\
 & \left( \left( \frac{1}{4} + \frac{i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - i \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \\
 & \left( \cos[2c] + i \sin[2c] \right) \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \\
 & \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] - \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \right) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \right)
 \end{aligned}$$



$$\left. \left( \cos[2c] + i \sin[2c] \right) \left( 2i \cos[dx] - 2 \sin[dx] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right/$$

$$\left( \sqrt{2 \cos[dx] + 2i \sin[dx]} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) - \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}}$$

$$(1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \left( \cos[2c] + i \sin[2c] \right) \sqrt{2 \cos[dx] + 2i \sin[dx]}$$

$$\sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( - \left( \left( \left( \frac{\sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right. \right.

$$\left. \left. \left. \left( \sqrt{-1+i} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right. \right.

$$\left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right)$$

$$\left( \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right.$$

$$\left. \frac{(-1)^{1/4} \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2}} \right) /$$

$$\left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \left( a + i a \tan[c + dx] \right)^{3/2}$$$$$$

Problem 430: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{9/2}}{(a + i a \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 411 leaves, 12 steps):

$$\begin{aligned} & -\frac{5 i e^{9/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} a^{5/2} d} + \frac{5 i e^{9/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} a^{5/2} d} + \frac{1}{2 \sqrt{2} a^{5/2} d} \\ & 5 i e^{9/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right] - \\ & \frac{1}{2 \sqrt{2} a^{5/2} d} 5 i e^{9/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right] + \\ & \frac{4 i e^2 (e \operatorname{Sec}[c+d x])^{5/2}}{a d (a+i a \operatorname{Tan}[c+d x])^{3/2}} + \frac{5 i e^4 \sqrt{e \operatorname{Sec}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{a^3 d} \end{aligned}$$

Result (type 3, 1511 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[c+d x]^2 (e \operatorname{Sec}[c+d x])^{9/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (\operatorname{Cos}[d x] (8 i \operatorname{Cos}[2 c] - 8 \operatorname{Sin}[2 c]) + \right. \\ & \left. \operatorname{Sec}[c+d x] (i \operatorname{Cos}[3 c] - \operatorname{Sin}[3 c]) + (8 \operatorname{Cos}[2 c] + 8 i \operatorname{Sin}[2 c]) \operatorname{Sin}[d x]) \right) / \\ & \left( d (a+i a \operatorname{Tan}[c+d x])^{5/2} - \left( (5+5 i) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\operatorname{Cos}[\frac{c}{2}] - i \operatorname{Sin}[\frac{c}{2}]) \sqrt{i + \operatorname{Tan}[\frac{d x}{2}]} }{\sqrt{i - \operatorname{Tan}[\frac{d x}{2}]} } \right] - \right. \right. \\ & \left. \left. i \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} (\operatorname{Cos}[\frac{c}{2}] - i \operatorname{Sin}[\frac{c}{2}]) \sqrt{i + \operatorname{Tan}[\frac{d x}{2}]} }{\sqrt{-1-i} \sqrt{i - \operatorname{Tan}[\frac{d x}{2}]} } \right] \right) \right) \\ & \operatorname{Cos}[c+d x] (e \operatorname{Sec}[c+d x])^{9/2} \left( \operatorname{Cos}\left[\frac{5 c}{2}\right] + i \operatorname{Sin}\left[\frac{5 c}{2}\right] \right) \\ & \left( -\frac{5}{2} \operatorname{Cos}[3 c] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} - \frac{5}{2} i \operatorname{Sin}[3 c] \sqrt{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \right) \\ & \left( \operatorname{Cos}[d x] + i \operatorname{Sin}[d x] \right)^3 \sqrt{i + \operatorname{Tan}\left[\frac{d x}{2}\right]} \Bigg) / \\ & \left( d \sqrt{2 i - 2 \operatorname{Tan}\left[\frac{d x}{2}\right]} - \left( \left( \left( \frac{5}{4} + \frac{5 i}{4} \right) \left( \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} (\operatorname{Cos}[\frac{c}{2}] - i \operatorname{Sin}[\frac{c}{2}]) \sqrt{i + \operatorname{Tan}[\frac{d x}{2}]} }{\sqrt{i - \operatorname{Tan}[\frac{d x}{2}]} } \right] - \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right]}{\left( \cos \left[ \frac{5c}{2} \right] + i \sin \left[ \frac{5c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]}} \right) \operatorname{Sec} \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{5c}{2} \right] + \right. \\
 & \left. i \sin \left[ \frac{5c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \left/ \left( \sqrt{2i - 2 \tan \left[ \frac{dx}{2} \right]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \right) - \\
 & \left( \frac{5}{2} + \frac{5i}{2} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] - \right. \\
 & \left. \frac{i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right]}{\operatorname{Sec} \left[ \frac{dx}{2} \right]^2} \right) \\
 & \left. \left( \cos \left[ \frac{5c}{2} \right] + i \sin \left[ \frac{5c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \left/ \right. \\
 & \left( 2i - 2 \tan \left[ \frac{dx}{2} \right] \right)^{3/2} - \left( \frac{5}{2} + \frac{5i}{2} \right) \left( \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] - \right. \\
 & \left. \frac{i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right]}{\left( \cos \left[ \frac{5c}{2} \right] + i \sin \left[ \frac{5c}{2} \right] \right) \left( i \cos [dx] - \sin [dx] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}} \right) \left/ \right.
 \end{aligned}$$

$$\left( \sqrt{\cos[dx] + i \sin[dx]} \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) -$$

$$\left( (5 + 5i) \left( \cos\left[\frac{5c}{2}\right] + i \sin\left[\frac{5c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right)$$

$$\left( - \left( \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \right. \right.$$

$$\left. \left. \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \right.$$

$$\left. \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) +$$

$$\left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \right. \right.$$

$$\left. \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) /$$

$$\left( \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) /$$

$$\left( \sqrt{2i - 2 \tan\left[\frac{dx}{2}\right]} \right) \left( a + i a \tan[c + dx] \right)^{5/2}$$

### Problem 431: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{7/2}}{(a + i a \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 527 leaves, 12 steps):

$$\frac{4 i e^2 (e \operatorname{Sec}[c + d x])^{3/2}}{3 a d (a + i a \operatorname{Tan}[c + d x])^{3/2}} + \frac{i \sqrt{2} e^{7/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{a^{3/2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} -$$

$$\frac{i \sqrt{2} e^{7/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c + d x]}}\right] \operatorname{Sec}[c + d x]}{a^{3/2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} -$$

$$\left( i e^{7/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x])\right] \right.$$

$$\left. \operatorname{Sec}[c + d x] \right) / \left( \sqrt{2} a^{3/2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) +$$

$$\left( i e^{7/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \operatorname{Tan}[c + d x]}}{\sqrt{e \operatorname{Sec}[c + d x]}} + \operatorname{Cos}[c + d x] (a - i a \operatorname{Tan}[c + d x])\right] \right.$$

$$\left. \operatorname{Sec}[c + d x] \right) / \left( \sqrt{2} a^{3/2} d \sqrt{a - i a \operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]} \right)$$

Result (type 3, 5863 leaves):

$$\left( \operatorname{Cos}[c + d x] (e \operatorname{Sec}[c + d x])^{7/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 \right.$$

$$\left. \left( \operatorname{Cos}[2 d x] \left( \frac{4}{3} i \operatorname{Cos}[c] - \frac{4 \operatorname{Sin}[c]}{3} \right) + \left( \frac{4 \operatorname{Cos}[c]}{3} + \frac{4}{3} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 d x] \right) \right) /$$

$$\left( d (a + i a \operatorname{Tan}[c + d x])^{5/2} \right) + \frac{1}{d \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} (a + i a \operatorname{Tan}[c + d x])^{5/2}}$$

$$(1 + i) \operatorname{Cos}[c] \operatorname{Cos}[c + d x] (e \operatorname{Sec}[c + d x])^{7/2}$$

$$\left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \operatorname{Sin}[c] (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2} \sqrt{\frac{i - \operatorname{Tan}\left[\frac{d x}{2}\right]}{i + \operatorname{Tan}\left[\frac{d x}{2}\right]}}$$

$$\left( \operatorname{Cos}\left[\frac{c}{2}\right] \left( (2 - 2 i) \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} - \sqrt{2} \operatorname{Log}\left[ \left( (1 + i) \left( 2 - 2 i \operatorname{Cot}\left[\frac{c}{2}\right] \right) \operatorname{Sin}\left[\frac{c}{2}\right]^2 \right. \right. \right.$$

$$\left. \left. \left( \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} + \sqrt{2} \sqrt{-1 + \operatorname{Sin}[c]} \operatorname{Tan}\left[\frac{d x}{2}\right] - 2 \sqrt{i - \operatorname{Tan}\left[\frac{d x}{2}\right]} \right) \right] \right)$$

$$\begin{aligned}
 & \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \\
 & \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \Bigg) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \Bigg) \\
 & \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ - \left( \left( 2 - 2i \right) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \Bigg) \\
 & \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \sin\left[\frac{c}{2}\right] \left( (2 + 2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. \sqrt{2} \log \left[ \left( (1 + i) \left( 2 - 2i \cot\left[\frac{c}{2}\right] \right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1 + \sin[c]} + \sqrt{2} \sqrt{-1 + \sin[c]} \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1 + \sin[c]} + \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{-1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \Bigg) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( -\sin\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \right. \right. \\
 & \left. \left. \cos\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log \left[ \right.
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( (2 - 2i) \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] \left( -1 + \tan\left[\frac{dx}{2}\right] \right) + \sin\left[\frac{c}{2}\right] \left( 1 + \tan\left[\frac{dx}{2}\right] \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( (1 + i) \cos[2c]^2 \cos[dx] (e \sec[c + dx])^{7/2} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \left. (\cos[dx] + i \sin[dx])^{7/2} \right. \\
 & \left. \left( (1 + i) \right. \right. \\
 & \left. \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right) \\
 & \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1 + i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1 - i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)
 \end{aligned}$$

$$\left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) \right) \right) /$$

$$\left( d \sqrt{i - \tan \left[ \frac{d x}{2} \right]} \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \cos [2 c] \sec \left[ \frac{d x}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\cos [d x] + i \sin [d x]} \left( (1 + i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{d x}{2} \right]} + \right. \right. \right.$$

$$\left. \left. \left. \sqrt{2} \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} + \right. \right. \right.$$

$$\left. \left. \left. i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1 + i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{d x}{2} \right]}}{\sqrt{-1 - i} \sqrt{i - \tan \left[ \frac{d x}{2} \right]}} \right] \right. \right. \right.$$

$$\left. \left. \left. \sin [c] \sqrt{i + \tan \left[ \frac{d x}{2} \right]} \right) \right) \right) / \left( i - \tan \left[ \frac{d x}{2} \right] \right)^{3/2} -$$

$$\left( \left( \frac{1}{2} + \frac{i}{2} \right) \cos [2 c] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) (i \cos [d x] - \sin [d x]) \right)$$

$$\left( (1 + i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i - \tan \left[ \frac{d x}{2} \right]} + \sqrt{2} \right)$$



$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + i \sqrt{2} \\
 & \text{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) / \\
 & \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) - \frac{1}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \\
 & (1+i) \cos [2c] \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{\cos [dx] + i \sin [dx]} \\
 & \left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} + \right. \\
 & \frac{\text{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sec \left[ \frac{dx}{2} \right]^2 \sin [c]}{2 \sqrt{2} \sqrt{i + \tan \left[ \frac{dx}{2} \right]}} + \\
 & \left. i \text{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sec \left[ \frac{dx}{2} \right]^2 \sin [c] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) + \\
 & \left( i \sqrt{2} \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \left( \frac{\sqrt{-1+i} \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{4 \sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \sqrt{i + \tan \left[ \frac{dx}{2} \right]}} + \right. \right.
 \end{aligned}
 \right.
 \end{aligned}$$

$$\left( \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) + \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 + \frac{i \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right)^2 \left( i + \tan\left[\frac{dx}{2}\right] \right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \left( a + i a \tan[c + dx] \right)^{5/2} - \frac{1}{d \left( a + i a \tan[c + dx] \right)^{5/2}} i$$

$$\cos\left[\frac{c+dx}{2}\right] \left( e \operatorname{Sec}[c+dx] \right)^{7/2} \left( \cos[dx] + i \sin[dx] \right)^{5/2} \left( \frac{1}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \left( \frac{1}{2} + \frac{i}{2} \right) \cos[2c] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{\cos[dx] + i \sin[dx]} \right)$$

$$\begin{aligned}
 & \left( \cos\left[\frac{c}{2}\right] \left( (2-2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} - \sqrt{2} \log\left[\left(2+2i\right) \cos\left[\frac{dx}{2}\right] \left(1-i \cot\left[\frac{c}{2}\right]\right)\right] \right. \right. \\
 & \quad \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1+\sin[c]} + \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] - \right. \\
 & \quad \left. 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \left( -\sqrt{2} \sqrt{-1+\sin[c]} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \sqrt{-1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \log\left[\left(2-2i\right) \cos\left[\frac{dx}{2}\right] \left(\cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right]\right)\right] \\
 & \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} - \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + \right. \right. \\
 & \quad \left. 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1+\sin[c]} + \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) / \\
 & \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \sqrt{1+\sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} - \sin\left[\frac{c}{2}\right] \left( (2+2i) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. \sqrt{2} \log\left[\left(2+2i\right) \cos\left[\frac{dx}{2}\right] \left(1-i \cot\left[\frac{c}{2}\right]\right) \sin\left[\frac{c}{2}\right]^2 \left( \sqrt{2} \sqrt{-1+\sin[c]} + \right. \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] - 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \cot\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( -\sqrt{2} \sqrt{-1+\sin[c]} + \sqrt{2} \sqrt{-1+\sin[c]} \tan\left[\frac{dx}{2}\right] + 2 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \sqrt{-1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \\
 & \sqrt{2} \operatorname{Log}\left[ \left( (2-2i) \cos\left[\frac{dx}{2}\right] \left( \cos\left[\frac{c}{2}\right] + i \sin\left[\frac{c}{2}\right] \right) \left( \sin\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} - \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right. \right. \\
 & \left. \left. \cos\left[\frac{c}{2}\right] \left( \sqrt{2} \sqrt{1 + \sin[c]} + \sqrt{2} \sqrt{1 + \sin[c]} \tan\left[\frac{dx}{2}\right] + 2i \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) \right) \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \\
 & \left. \left. \left. \left. \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \sqrt{1 + \sin[c]} \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) - \\
 & \left( (1+i) \cos[dx] \operatorname{Sec}[c+dx] \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c]^2 (\cos[dx] + i \sin[dx]) \right) \\
 & \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. \sqrt{2} \operatorname{ArcTan}\left[ \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \\
 & \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \left( \left( \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( \sqrt{i - \tan\left[\frac{dx}{2}\right]} \right) \\
 & - \left( \left( \left( \left( \left( \frac{1}{4} + \frac{i}{4} \right) \sec\left[\frac{dx}{2}\right]^2 \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c] \sqrt{\cos[dx] + i \sin[dx]} \right. \right. \right. \right. \\
 & \left. \left. \left. \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \operatorname{ArcTan}\left[ \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(-1)^{1/4} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} + \right. \right. \right. \\
 & \left. \left. \left. \left. i \sqrt{2} \operatorname{ArcTan}\left[ \frac{\sqrt{-1+i} \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i + \tan\left[\frac{dx}{2}\right]}}{\sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]}} \right] \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right) / \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} - \\
 & \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sin[2c] (i \cos[dx] - \sin[dx]) \right) \\
 & \left( (1+i) \left( \cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right] \right) \sqrt{i - \tan\left[\frac{dx}{2}\right]} + \sqrt{2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sin [c] \right. \\
 & \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} + i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right. \\
 & \left. \sin [c] \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) \left/ \left( \sqrt{\cos [dx] + i \sin [dx]} \sqrt{i - \tan \left[ \frac{dx}{2} \right]} \right) - \right. \\
 & \left. \frac{1}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} (1+i) \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sin [2c] \sqrt{\cos [dx] + i \sin [dx]} \right. \\
 & \left. \left( - \frac{\left( \frac{1}{4} + \frac{i}{4} \right) \sec \left[ \frac{dx}{2} \right]^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right)}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} + \operatorname{ArcTan} \left[ \frac{(-1)^{1/4} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \sec \left[ \frac{dx}{2} \right]^2 \sin [c] \right) \left/ \left( 2 \sqrt{2} \right. \right. \\
 & \left. \left. \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) + \left( i \operatorname{ArcTan} \left[ \frac{\sqrt{-1+i} \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \sqrt{i + \tan \left[ \frac{dx}{2} \right]}}{\sqrt{-1-i} \sqrt{i - \tan \left[ \frac{dx}{2} \right]}} \right] \right. \\
 & \left. \left. \sec \left[ \frac{dx}{2} \right]^2 \sin [c] \right) \left/ \left( 2 \sqrt{2} \sqrt{i + \tan \left[ \frac{dx}{2} \right]} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( i \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{\sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{-1-i} \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left( \sqrt{-1+i} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \left( 4 \sqrt{-1-i} \right. \right. \\
 & \left. \left. \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) / \left( 1 - \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) + \\
 & \left( \sqrt{2} \sin[c] \sqrt{i + \tan\left[\frac{dx}{2}\right]} \left( \frac{(-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)}{4 \sqrt{i - \tan\left[\frac{dx}{2}\right]} \sqrt{i + \tan\left[\frac{dx}{2}\right]}} + \right. \right. \\
 & \left. \left( (-1)^{1/4} \operatorname{Sec}\left[\frac{dx}{2}\right]^2 \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right) \sqrt{i + \tan\left[\frac{dx}{2}\right]} \right) / \right. \\
 & \left. \left. \left( 4 \left( i - \tan\left[\frac{dx}{2}\right] \right)^{3/2} \right) \right) \right) / \left( 1 + \frac{i \left(\cos\left[\frac{c}{2}\right] - i \sin\left[\frac{c}{2}\right]\right)^2 \left(i + \tan\left[\frac{dx}{2}\right]\right)}{i - \tan\left[\frac{dx}{2}\right]} \right) \right) \right) \right)
 \end{aligned}$$

**Problem 443: Result unnecessarily involves higher level functions.**

$$\int \frac{(d \operatorname{Sec}[e + f x])^{2/3}}{(a + i a \tan[e + f x])^{7/3}} dx$$

Optimal (type 3, 437 leaves, 9 steps):

$$\frac{i (d \operatorname{Sec}[e + f x])^{2/3}}{4 f (a + i a \operatorname{Tan}[e + f x])^{7/3}} - \frac{5 x (d \operatorname{Sec}[e + f x])^{2/3}}{72 \times 2^{2/3} a^{5/3} (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} +$$

$$\frac{5 i \operatorname{ArcTan}\left[\frac{a^{1/3} + 2^{2/3} (a - i a \operatorname{Tan}[e + f x])^{1/3}}{\sqrt{3} a^{1/3}}\right] (d \operatorname{Sec}[e + f x])^{2/3}}{12 \times 2^{2/3} \sqrt{3} a^{5/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} -$$

$$\frac{5 i \operatorname{Log}[\operatorname{Cos}[e + f x]] (d \operatorname{Sec}[e + f x])^{2/3}}{72 \times 2^{2/3} a^{5/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} -$$

$$\frac{5 i \operatorname{Log}\left[2^{1/3} a^{1/3} - (a - i a \operatorname{Tan}[e + f x])^{1/3}\right] (d \operatorname{Sec}[e + f x])^{2/3}}{24 \times 2^{2/3} a^{5/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} +$$

$$\frac{5 i (d \operatorname{Sec}[e + f x])^{2/3}}{24 f (a + i a \operatorname{Tan}[e + f x])^{1/3} (a^2 + i a^2 \operatorname{Tan}[e + f x])}$$

Result (type 5, 138 leaves):

$$- \left( \left( i \operatorname{Sec}[e + f x]^2 (d \operatorname{Sec}[e + f x])^{2/3} \left( 11 + 11 \operatorname{Cos}[2 (e + f x)] + 10 e^{2 i (e + f x)} (1 + e^{-2 i (e + f x)})^{1/3} \right. \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{3}, \frac{4}{3}, -e^{-2 i (e + f x)}\right] + 5 i \operatorname{Sin}[2 (e + f x)] \right) \right) /$$

$$\left( 48 a^2 f (-i + \operatorname{Tan}[e + f x])^2 (a + i a \operatorname{Tan}[e + f x])^{1/3} \right)$$

**Problem 444: Result unnecessarily involves higher level functions.**

$$\int \frac{(d \operatorname{Sec}[e + f x])^{2/3}}{(a + i a \operatorname{Tan}[e + f x])^{4/3}} dx$$

Optimal (type 3, 378 leaves, 8 steps):

$$\frac{i (d \operatorname{Sec}[e + f x])^{2/3}}{2 f (a + i a \operatorname{Tan}[e + f x])^{4/3}} - \frac{x (d \operatorname{Sec}[e + f x])^{2/3}}{6 \times 2^{2/3} a^{2/3} (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} +$$

$$\frac{i \operatorname{ArcTan}\left[\frac{a^{1/3} + 2^{2/3} (a - i a \operatorname{Tan}[e + f x])^{1/3}}{\sqrt{3} a^{1/3}}\right] (d \operatorname{Sec}[e + f x])^{2/3}}{2^{2/3} \sqrt{3} a^{2/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} -$$

$$\frac{i \operatorname{Log}[\operatorname{Cos}[e + f x]] (d \operatorname{Sec}[e + f x])^{2/3}}{6 \times 2^{2/3} a^{2/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}} -$$

$$\frac{i \operatorname{Log}\left[2^{1/3} a^{1/3} - (a - i a \operatorname{Tan}[e + f x])^{1/3}\right] (d \operatorname{Sec}[e + f x])^{2/3}}{2 \times 2^{2/3} a^{2/3} f (a - i a \operatorname{Tan}[e + f x])^{1/3} (a + i a \operatorname{Tan}[e + f x])^{1/3}}$$

Result (type 5, 118 leaves):



$$\left( i e^{-2i(e+fx)} \right. \\ \left. \left( 1 + e^{2i(e+fx)} + 2 e^{2i(e+fx)} \left( 1 + e^{-2i(e+fx)} \right)^{1/3} \text{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{3}, \frac{4}{3}, -e^{-2i(e+fx)} \right] \right) \right) \\ \left( d \text{Sec}[e+fx] \right)^{2/3} \Big/ \left( 4 a f \left( a + i a \text{Tan}[e+fx] \right)^{1/3} \right)$$

**Problem 445: Result unnecessarily involves higher level functions.**

$$\int \frac{(d \text{Sec}[e+fx])^{2/3}}{(a + i a \text{Tan}[e+fx])^{1/3}} dx$$

Optimal (type 3, 340 leaves, 6 steps):

$$\frac{a^{1/3} x (d \text{Sec}[e+fx])^{2/3}}{2 \times 2^{2/3} (a - i a \text{Tan}[e+fx])^{1/3} (a + i a \text{Tan}[e+fx])^{1/3}} + \\ \frac{i \sqrt{3} a^{1/3} \text{ArcTan} \left[ \frac{a^{1/3} + 2^{2/3} (a - i a \text{Tan}[e+fx])^{1/3}}{\sqrt{3} a^{1/3}} \right] (d \text{Sec}[e+fx])^{2/3}}{2^{2/3} f (a - i a \text{Tan}[e+fx])^{1/3} (a + i a \text{Tan}[e+fx])^{1/3}} - \\ \frac{i a^{1/3} \text{Log}[\text{Cos}[e+fx]] (d \text{Sec}[e+fx])^{2/3}}{2 \times 2^{2/3} f (a - i a \text{Tan}[e+fx])^{1/3} (a + i a \text{Tan}[e+fx])^{1/3}} - \\ \frac{3 i a^{1/3} \text{Log} \left[ 2^{1/3} a^{1/3} - (a - i a \text{Tan}[e+fx])^{1/3} \right] (d \text{Sec}[e+fx])^{2/3}}{2 \times 2^{2/3} f (a - i a \text{Tan}[e+fx])^{1/3} (a + i a \text{Tan}[e+fx])^{1/3}}$$

Result (type 5, 116 leaves):

$$\left( 3 i \left( 1 + e^{-2i(e+fx)} \right)^{1/3} \left( \frac{d e^{i(e+fx)}}{1 + e^{2i(e+fx)}} \right)^{2/3} \text{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{3}, \frac{4}{3}, -e^{-2i(e+fx)} \right] \right) \Big/ \\ \left( 2^{2/3} \left( \frac{a e^{2i(e+fx)}}{1 + e^{2i(e+fx)}} \right)^{1/3} f \right)$$

**Problem 454: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \text{Sec}[c+dx])^m}{a + i a \text{Tan}[c+dx]} dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$\frac{1}{a d m} i 2^{-1+\frac{m}{2}} \text{Hypergeometric2F1} \left[ 2 - \frac{m}{2}, \frac{m}{2}, \frac{2+m}{2}, \frac{1}{2} (1 - i \text{Tan}[c+dx]) \right] \\ (e \text{Sec}[c+dx])^m (1 + i \text{Tan}[c+dx])^{-m/2}$$

Result (type 5, 212 leaves):

$$\begin{aligned}
 & - \left( \left( i 2^{-1+m} e^{-i(c+dx)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^m (1+e^{2i(c+dx)})^m \right. \right. \\
 & \quad \left. \left( e^{i d(-2+m)x} m \text{Hypergeometric2F1} \left[ \frac{1}{2}(-2+m), m, \frac{m}{2}, -e^{2i(c+dx)} \right] + \right. \right. \\
 & \quad \left. \left. e^{i(2c+dx)} (-2+m) \text{Hypergeometric2F1} \left[ \frac{m}{2}, m, \frac{2+m}{2}, -e^{2i(c+dx)} \right] \right) \text{Sec}[c+dx]^{1-m} \right. \\
 & \quad \left. \left. (e \text{Sec}[c+dx])^m (\text{Cos}[dx] + i \text{Sin}[dx]) \right) \right) / (d(-2+m)m(a+i a \text{Tan}[c+dx]))
 \end{aligned}$$

**Problem 455: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \text{Sec}[c+dx])^m}{(a+i a \text{Tan}[c+dx])^2} dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$\frac{1}{a^2 d m} i 2^{-2+\frac{m}{2}} \text{Hypergeometric2F1} \left[ 3 - \frac{m}{2}, \frac{m}{2}, \frac{2+m}{2}, \frac{1}{2} (1 - i \text{Tan}[c+dx]) \right] (e \text{Sec}[c+dx])^m (1+i \text{Tan}[c+dx])^{-m/2}$$

Result (type 5, 279 leaves):

$$\begin{aligned}
 & - \frac{1}{d(-4+m)(-2+m)m(a+i a \text{Tan}[c+dx])^2} i 2^{-2+m} e^{-i(2c+dx)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^m (1+e^{2i(c+dx)})^m \\
 & \quad \left( e^{i d(-4+m)x} (-2+m) m \text{Hypergeometric2F1} \left[ \frac{1}{2}(-4+m), m, \frac{1}{2}(-2+m), -e^{2i(c+dx)} \right] + \right. \\
 & \quad \left. e^{2i c} (-4+m) \left( 2 e^{i d(-2+m)x} m \text{Hypergeometric2F1} \left[ \frac{1}{2}(-2+m), m, \frac{m}{2}, -e^{2i(c+dx)} \right] + \right. \right. \\
 & \quad \left. \left. e^{i(2c+dx)} (-2+m) \text{Hypergeometric2F1} \left[ \frac{m}{2}, m, \frac{2+m}{2}, -e^{2i(c+dx)} \right] \right) \right) \\
 & \quad \text{Sec}[c+dx]^{2-m} (e \text{Sec}[c+dx])^m (\text{Cos}[dx] + i \text{Sin}[dx])^2
 \end{aligned}$$

**Problem 456: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \text{Sec}[c+dx])^m}{(a+i a \text{Tan}[c+dx])^3} dx$$

Optimal (type 5, 86 leaves, 4 steps):

$$\frac{1}{a^3 d m} i 2^{-3+\frac{m}{2}} \text{Hypergeometric2F1} \left[ 4 - \frac{m}{2}, \frac{m}{2}, \frac{2+m}{2}, \frac{1}{2} (1 - i \text{Tan}[c+dx]) \right] (e \text{Sec}[c+dx])^m (1+i \text{Tan}[c+dx])^{-m/2}$$

Result (type 5, 347 leaves):

$$\begin{aligned}
 & - \frac{1}{d (-6+m) (-4+m) (-2+m) m (a + i a \tan [c + d x])^3} \\
 & i 2^{-3+m} e^{-i (3c+dmx)} \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^m (1 + e^{2i (c+dx)})^m \\
 & \left( e^{i d (-6+m) x} m (8 - 6m + m^2) \text{Hypergeometric2F1} \left[ \frac{1}{2} (-6+m), m, \frac{1}{2} (-4+m), -e^{2i (c+dx)} \right] + e^{2i c} \right. \\
 & (-6+m) \left( 3 e^{i d (-4+m) x} (-2+m) m \text{Hypergeometric2F1} \left[ \frac{1}{2} (-4+m), m, \frac{1}{2} (-2+m), -e^{2i (c+dx)} \right] + \right. \\
 & e^{2i c} (-4+m) \left( 3 e^{i d (-2+m) x} m \text{Hypergeometric2F1} \left[ \frac{1}{2} (-2+m), m, \frac{m}{2}, -e^{2i (c+dx)} \right] + \right. \\
 & \left. \left. \left. e^{i (2c+dmx)} (-2+m) \text{Hypergeometric2F1} \left[ \frac{m}{2}, m, \frac{2+m}{2}, -e^{2i (c+dx)} \right] \right] \right) \right) \\
 & \text{Sec}[c + d x]^{3-m} (e \text{Sec}[c + d x])^m (\text{Cos}[d x] + i \text{Sin}[d x])^3
 \end{aligned}$$

**Problem 466: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^4 (a + i a \tan [c + d x])^n dx$$

Optimal (type 3, 65 leaves, 3 steps):

$$- \frac{2 i (a + i a \tan [c + d x])^{2+n}}{a^2 d (2+n)} + \frac{i (a + i a \tan [c + d x])^{3+n}}{a^3 d (3+n)}$$

Result (type 3, 143 leaves):

$$\begin{aligned}
 & - \left( \left( i 2^{3+n} e^{4i (c+dx)} (e^{i dx})^n \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^n (3 + e^{2i (c+dx)} + n) \text{Sec}[c + d x]^{-n} \right. \right. \\
 & \left. \left. (\text{Cos}[d x] + i \text{Sin}[d x])^{-n} (a + i a \tan [c + d x])^n \right) / \left( d (1 + e^{2i (c+dx)})^3 (2+n) (3+n) \right) \right)
 \end{aligned}$$

**Problem 467: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^2 (a + i a \tan [c + d x])^n dx$$

Optimal (type 3, 32 leaves, 2 steps):

$$- \frac{i (a + i a \tan [c + d x])^{1+n}}{a d (1+n)}$$

Result (type 3, 111 leaves):

$$\begin{aligned}
 & - \frac{1}{d (1+n)} i 2^{1+n} e^{i (c+dx)} (e^{i dx})^n \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^{1+n} \\
 & \text{Sec}[c + d x]^{-n} (\text{Cos}[d x] + i \text{Sin}[d x])^{-n} (a + i a \tan [c + d x])^n
 \end{aligned}$$

**Problem 468: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 56 leaves, 2 steps):

$$\frac{1}{4 d (1 - n)} i a \operatorname{Hypergeometric2F1}\left[2, -1 + n, n, \frac{1}{2} (1 + i \tan [c + d x])\right] (a + i a \tan [c + d x])^{-1+n}$$

Result (type 5, 256 leaves):

$$-\frac{1}{d n (-1 + n^2)} i 2^{-3+n} e^{-2 i (c+d n x)} (e^{i d x})^n \left(\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}\right)^n \left( (e^{2 i d (-1+n) x} + e^{2 i (c+d n x)}) n (1 + n) + \right. \\ \left. 2 e^{2 i (c+d n x)} (1 + e^{2 i (c+d x)})^n (-1 + n^2) \operatorname{Hypergeometric2F1}[n, n, 1 + n, -e^{2 i (c+d x)}] + \right. \\ \left. e^{2 i (2 c+d x+d n x)} (1 + e^{2 i (c+d x)})^n (-1 + n) n \operatorname{Hypergeometric2F1}[n, 1 + n, 2 + n, -e^{2 i (c+d x)}] \right) \\ \sec [c + d x]^{-n} (\cos [d x] + i \sin [d x])^{-n} (a + i a \tan [c + d x])^n$$

**Problem 469: Unable to integrate problem.**

$$\int \cos [c + d x]^4 (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 60 leaves, 2 steps):

$$\frac{1}{8 d (2 - n)} i a^2 \operatorname{Hypergeometric2F1}\left[3, -2 + n, -1 + n, \frac{1}{2} (1 + i \tan [c + d x])\right] (a + i a \tan [c + d x])^{-2+n}$$

Result (type 8, 26 leaves):

$$\int \cos [c + d x]^4 (a + i a \tan [c + d x])^n dx$$

**Problem 470: Unable to integrate problem.**

$$\int \cos [c + d x]^6 (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 60 leaves, 2 steps):

$$\frac{1}{16 d (3 - n)} i a^3 \operatorname{Hypergeometric2F1}\left[4, -3 + n, -2 + n, \frac{1}{2} (1 + i \tan [c + d x])\right] (a + i a \tan [c + d x])^{-3+n}$$

Result (type 8, 26 leaves):

$$\int \cos [c + d x]^6 (a + i a \tan [c + d x])^n dx$$

### Problem 474: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x] (a+i a \tan [c+d x])^n d x$$

Optimal (type 5, 85 leaves, 4 steps):

$$-\frac{1}{d} i 2^{-\frac{1}{2}+n} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{3}{2}-n, \frac{1}{2}, \frac{1}{2}(1-i \tan [c+d x])\right] \\ (1+i \tan [c+d x])^{\frac{1}{2}-n} (a+i a \tan [c+d x])^n$$

Result (type 5, 195 leaves):

$$-\frac{1}{d(-1+4 n^2)} i 2^{-1+n} \left(\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}\right)^{-1+n} \\ (1+e^{2 i(c+d x)})^{-1+n} \left( (1+2 n) \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, n, \frac{1}{2}+n, -e^{2 i(c+d x)}\right] + \right. \\ \left. e^{2 i(c+d x)}(-1+2 n) \operatorname{Hypergeometric2F1}\left[n, \frac{1}{2}+n, \frac{3}{2}+n, -e^{2 i(c+d x)}\right] \right) \\ \sec [c+d x]^{-n} (\cos [d x]+i \sin [d x])^{-n} (a+i a \tan [c+d x])^n$$

### Problem 475: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^3 (a+i a \tan [c+d x])^n d x$$

Optimal (type 5, 94 leaves, 4 steps):

$$-\frac{1}{3 a d} i 2^{-\frac{3}{2}+n} \cos [c+d x]^3 \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{5}{2}-n, -\frac{1}{2}, \frac{1}{2}(1-i \tan [c+d x])\right] \\ (1+i \tan [c+d x])^{\frac{1}{2}-n} (a+i a \tan [c+d x])^{1+n}$$

Result (type 5, 321 leaves):

$$-\frac{1}{d(9-40 n^2+16 n^4)} i 2^{-3+n} e^{-3 i(c+d x)} \left(\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}\right)^n (1+e^{2 i(c+d x)})^n \\ \left( (-3-2 n+12 n^2+8 n^3) \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}+n, n, -\frac{1}{2}+n, -e^{2 i(c+d x)}\right] + \right. \\ \left. e^{2 i(c+d x)}(-3+2 n) \left( 3(3+8 n+4 n^2) \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, n, \frac{1}{2}+n, -e^{2 i(c+d x)}\right] + \right. \right. \\ \left. \left. e^{2 i(c+d x)}(-1+2 n) \left( (9+6 n) \operatorname{Hypergeometric2F1}\left[n, \frac{1}{2}+n, \frac{3}{2}+n, -e^{2 i(c+d x)}\right] + \right. \right. \\ \left. \left. e^{2 i(c+d x)}(1+2 n) \operatorname{Hypergeometric2F1}\left[n, \frac{3}{2}+n, \frac{5}{2}+n, -e^{2 i(c+d x)}\right] \right) \right) \right) \\ \sec [c+d x]^{-n} (\cos [d x]+i \sin [d x])^{-n} (a+i a \tan [c+d x])^n$$

### Problem 476: Unable to integrate problem.

$$\int \cos [c + d x]^5 (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 94 leaves, 4 steps):

$$-\frac{1}{5 a^2 d} i 2^{-\frac{5}{2}+n} \cos [c + d x]^5 \operatorname{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{7}{2}-n, -\frac{3}{2}, \frac{1}{2}(1-i \tan [c + d x])\right] \\ (1+i \tan [c + d x])^{\frac{1}{2}-n} (a+i a \tan [c + d x])^{2+n}$$

Result (type 8, 26 leaves):

$$\int \cos [c + d x]^5 (a + i a \tan [c + d x])^n dx$$

### Problem 497: Result more than twice size of optimal antiderivative.

$$\int (e \sec [c + d x])^{-2 n} (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 65 leaves, 3 steps):

$$-\frac{1}{2 d n} \\ i \operatorname{Hypergeometric2F1}\left[1, -n, 1-n, \frac{1}{2}(1-i \tan [c + d x])\right] (e \sec [c + d x])^{-2 n} (a + i a \tan [c + d x])^n$$

Result (type 5, 152 leaves):

$$-\frac{1}{d n} \\ i 2^{-1-n} (e^{i d x})^n (1 + e^{-2 i (c+d x)})^{-n} \left(\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}\right)^{-n} \operatorname{Hypergeometric2F1}\left[-n, -n, 1-n, -e^{-2 i (c+d x)}\right] \\ \sec [c + d x]^n (e \sec [c + d x])^{-2 n} (\cos [d x] + i \sin [d x])^{-n} (a + i a \tan [c + d x])^n$$

### Problem 498: Result more than twice size of optimal antiderivative.

$$\int (e \sec [c + d x])^{-1-2 n} (a + i a \tan [c + d x])^n dx$$

Optimal (type 5, 95 leaves, 5 steps):

$$\frac{1}{d} i 2^{-\frac{1}{2}-n} \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2}(3+2 n), \frac{1}{2}, \frac{1}{2}(1+i \tan [c + d x])\right] \\ (e \sec [c + d x])^{-1-2 n} (1-i \tan [c + d x])^{\frac{1}{2}+n} (a + i a \tan [c + d x])^n$$

Result (type 5, 192 leaves):

$$\frac{1}{d} i 2^{-1-n} (e^{i d x})^n \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{-1-n}$$

$$\left( 1+e^{2i(c+dx)} \right)^{-1-n} \left( \text{Hypergeometric2F1} \left[ -\frac{1}{2}, -n, \frac{1}{2}, -e^{2i(c+dx)} \right] - \right.$$

$$\left. e^{2i(c+dx)} \text{Hypergeometric2F1} \left[ \frac{1}{2}, -n, \frac{3}{2}, -e^{2i(c+dx)} \right] \right) \text{Sec}[c+dx]^{1+n}$$

$$\left( e \text{Sec}[c+dx] \right)^{-1-2n} (\text{Cos}[dx] + i \text{Sin}[dx])^{-n} (a + i a \text{Tan}[c+dx])^n$$

**Problem 499: Result more than twice size of optimal antiderivative.**

$$\int (e \text{Sec}[c+dx])^{-2-2n} (a + i a \text{Tan}[c+dx])^n dx$$

Optimal (type 5, 74 leaves, 4 steps):

$$-\frac{1}{4 a d (1+n)} i \text{Hypergeometric2F1} \left[ 2, -1-n, -n, \frac{1}{2} (1 - i \text{Tan}[c+dx]) \right]$$

$$\left( e \text{Sec}[c+dx] \right)^{-2(1+n)} (a + i a \text{Tan}[c+dx])^{1+n}$$

Result (type 5, 335 leaves):

$$-\frac{1}{d e^2 n (-1+n^2)} i 2^{-3-n} e^{-2i(c+dx)} (e^{i d x})^n \left( 1+e^{-2i(c+dx)} \right)^{-n} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{-n} \left( 1+e^{2i(c+dx)} \right)^{-n}$$

$$\left( \left( 1+e^{2i(c+dx)} \right)^n n (1+n) \text{Hypergeometric2F1} \left[ 1-n, -n, 2-n, -e^{-2i(c+dx)} \right] + \right.$$

$$\left. e^{2i(c+dx)} (-1+n) \left( \left( 1+e^{-2i(c+dx)} \right)^n (-1 + (1+e^{2i(c+dx)})^n + e^{2i(c+dx)} (1+e^{2i(c+dx)})^n \right) n + \right.$$

$$\left. 2 \left( 1+e^{2i(c+dx)} \right)^n (1+n) \text{Hypergeometric2F1} \left[ -n, -n, 1-n, -e^{-2i(c+dx)} \right] \right)$$

$$\text{Sec}[c+dx]^n \left( e \text{Sec}[c+dx] \right)^{-2n} (\text{Cos}[dx] + i \text{Sin}[dx])^{-n} (a + i a \text{Tan}[c+dx])^n$$

**Problem 500: Result more than twice size of optimal antiderivative.**

$$\int (e \text{Sec}[c+dx])^{-3-2n} (a + i a \text{Tan}[c+dx])^n dx$$

Optimal (type 5, 97 leaves, 5 steps):

$$\frac{1}{3 d} i 2^{-\frac{3}{2}-n} \text{Hypergeometric2F1} \left[ -\frac{3}{2}, \frac{1}{2} (5+2n), -\frac{1}{2}, \frac{1}{2} (1 + i \text{Tan}[c+dx]) \right]$$

$$\left( e \text{Sec}[c+dx] \right)^{-3-2n} (1 - i \text{Tan}[c+dx])^{\frac{3}{2}+n} (a + i a \text{Tan}[c+dx])^n$$

Result (type 5, 273 leaves):

$$\begin{aligned} & \frac{1}{3d} \int 2^{-3-n} e^{-3i(c+dx)} (e^{idx})^n \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{-n} \\ & (1+e^{2i(c+dx)})^{-n} \left( \text{Hypergeometric2F1} \left[ -\frac{3}{2}, -n, -\frac{1}{2}, -e^{2i(c+dx)} \right] + \right. \\ & 9e^{2i(c+dx)} \text{Hypergeometric2F1} \left[ -\frac{1}{2}, -n, \frac{1}{2}, -e^{2i(c+dx)} \right] - \\ & 9e^{4i(c+dx)} \text{Hypergeometric2F1} \left[ \frac{1}{2}, -n, \frac{3}{2}, -e^{2i(c+dx)} \right] - \\ & \left. e^{6i(c+dx)} \text{Hypergeometric2F1} \left[ \frac{3}{2}, -n, \frac{5}{2}, -e^{2i(c+dx)} \right] \right) \text{Sec}[c+dx]^{3+n} \\ & (e \text{Sec}[c+dx])^{-3-2n} (\text{Cos}[dx] + i \text{Sin}[dx])^{-n} (a + i a \text{Tan}[c+dx])^n \end{aligned}$$

**Problem 501: Result more than twice size of optimal antiderivative.**

$$\int (d \text{Sec}[e+fx])^{2n} (a + i a \text{Tan}[e+fx])^{-2-n} dx$$

Optimal (type 5, 66 leaves, 4 steps):

$$\frac{1}{8a^2fn} i \text{Hypergeometric2F1} \left[ 3, n, 1+n, \frac{1}{2} (1 - i \text{Tan}[e+fx]) \right] \\ (d \text{Sec}[e+fx])^{2n} (a + i a \text{Tan}[e+fx])^{-n}$$

Result (type 5, 257 leaves):

$$\frac{1}{fn(1+n)(2+n)} \int 2^{-3+n} e^{-2i(e+2fx)} (e^{ifx})^{-n} (1+e^{-2i(e+fx)})^n \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^n \\ (e^{4i(e+fx)} (2+3n+n^2) \text{Hypergeometric2F1} [n, n, 1+n, -e^{-2i(e+fx)}] + \\ 2e^{2i(e+fx)} n(2+n) \text{Hypergeometric2F1} [n, 1+n, 2+n, -e^{-2i(e+fx)}] + \\ n(1+n) \text{Hypergeometric2F1} [n, 2+n, 3+n, -e^{-2i(e+fx)}]) \text{Sec}[e+fx]^{2-n} \\ (d \text{Sec}[e+fx])^{2n} (\text{Cos}[fx] + i \text{Sin}[fx])^{2+n} (a + i a \text{Tan}[e+fx])^{-2-n}$$

**Problem 502: Result more than twice size of optimal antiderivative.**

$$\int (d \text{Sec}[e+fx])^{2n} (a + i a \text{Tan}[e+fx])^{-1-n} dx$$

Optimal (type 5, 66 leaves, 4 steps):

$$\frac{1}{4afn} i \text{Hypergeometric2F1} \left[ 2, n, 1+n, \frac{1}{2} (1 - i \text{Tan}[e+fx]) \right] \\ (d \text{Sec}[e+fx])^{2n} (a + i a \text{Tan}[e+fx])^{-n}$$

Result (type 5, 206 leaves):

$$\frac{1}{fn(1+n)} \int 2^{-2+n} e^{-i(e+2fx)} (e^{ifx})^{-n} (1+e^{-2i(e+fx)})^n \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^n \\ (e^{2i(e+fx)} (1+n) \text{Hypergeometric2F1} [n, n, 1+n, -e^{-2i(e+fx)}] + \\ n \text{Hypergeometric2F1} [n, 1+n, 2+n, -e^{-2i(e+fx)}]) \text{Sec}[e+fx]^{1-n} \\ (d \text{Sec}[e+fx])^{2n} (\text{Cos}[fx] + i \text{Sin}[fx])^{1+n} (a + i a \text{Tan}[e+fx])^{-1-n}$$



### Problem 503: Result more than twice size of optimal antiderivative.

$$\int (d \sec [e + f x])^{2n} (a + i a \tan [e + f x])^{-n} dx$$

Optimal (type 5, 63 leaves, 3 steps):

$$\frac{1}{2 f n} i \operatorname{Hypergeometric2F1}\left[1, n, 1+n, \frac{1}{2} (1 - i \tan [e + f x])\right] (d \sec [e + f x])^{2n} (a + i a \tan [e + f x])^{-n}$$

Result (type 5, 144 leaves):

$$\frac{1}{f n} i 2^{-1+n} (e^{i f x})^{-n} (1 + e^{-2 i (e+f x)})^n \left( \frac{e^{i (e+f x)}}{1 + e^{2 i (e+f x)}} \right)^n \operatorname{Hypergeometric2F1}[n, n, 1+n, -e^{-2 i (e+f x)}] \sec [e + f x]^{-n} (d \sec [e + f x])^{2n} (\cos [f x] + i \sin [f x])^n (a + i a \tan [e + f x])^{-n}$$

### Problem 508: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^5 (a + b \tan [c + d x]) dx$$

Optimal (type 3, 74 leaves, 4 steps):

$$\frac{3 a \operatorname{ArcTanh}[\sin [c + d x]]}{8 d} + \frac{b \sec [c + d x]^5}{5 d} + \frac{3 a \sec [c + d x] \tan [c + d x]}{8 d} + \frac{a \sec [c + d x]^3 \tan [c + d x]}{4 d}$$

Result (type 3, 207 leaves):

$$\begin{aligned} & - \frac{3 a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\ & \frac{3 a \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{b \sec [c + d x]^5}{5 d} + \\ & \frac{3 a}{a} \frac{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} - \\ & \frac{3 a}{a} \frac{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{16 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} \end{aligned}$$

### Problem 512: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x] (a + b \tan [c + d x]) dx$$

Optimal (type 3, 24 leaves, 2 steps):

$$\frac{a \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{b \sec [c + d x]}{d}$$

Result (type 3, 81 leaves):

$$-\frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b \operatorname{Sec}[c + dx]}{d}$$

**Problem 520: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^2 (a + b \operatorname{Tan}[c + dx])^2 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + b \operatorname{Tan}[c + dx])^3}{3bd}$$

Result (type 3, 56 leaves):

$$\frac{1}{6d} \operatorname{Sec}[c + dx]^2 (6ab + (3a^2 + b^2 + (3a^2 - b^2) \cos[2(c + dx)]) \operatorname{Tan}[c + dx])$$

**Problem 523: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^7 (a + b \operatorname{Tan}[c + dx])^2 dx$$

Optimal (type 3, 163 leaves, 6 steps):

$$\frac{5(8a^2 - b^2) \operatorname{ArcTanh}[\sin[c + dx]]}{128d} + \frac{9ab \operatorname{Sec}[c + dx]^7}{56d} +$$

$$\frac{5(8a^2 - b^2) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{128d} + \frac{5(8a^2 - b^2) \operatorname{Sec}[c + dx]^3 \operatorname{Tan}[c + dx]}{192d} +$$

$$\frac{(8a^2 - b^2) \operatorname{Sec}[c + dx]^5 \operatorname{Tan}[c + dx]}{48d} + \frac{b \operatorname{Sec}[c + dx]^7 (a + b \operatorname{Tan}[c + dx])}{8d}$$

Result (type 3, 1521 leaves):

$$\frac{5ab \cos[c + dx]^2 (a + b \operatorname{Tan}[c + dx])^2}{56d (a \cos[c + dx] + b \sin[c + dx])^2} -$$

$$\left( \frac{5(8a^2 - b^2) \cos[c + dx]^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] (a + b \operatorname{Tan}[c + dx])^2}{128d (a \cos[c + dx] + b \sin[c + dx])^2} + \right.$$

$$\left. \frac{5(8a^2 - b^2) \cos[c + dx]^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] (a + b \operatorname{Tan}[c + dx])^2}{128d (a \cos[c + dx] + b \sin[c + dx])^2} + \right.$$

$$\left. \frac{(b^2 \cos[c + dx]^2 (a + b \operatorname{Tan}[c + dx])^2)}{128d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^8 (a \cos[c + dx] + b \sin[c + dx])^2} + \right.$$

$$\left. \frac{(28a^2 + 24ab + 7b^2) \cos[c + dx]^2 (a + b \operatorname{Tan}[c + dx])^2}{1344d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^6 (a \cos[c + dx] + b \sin[c + dx])^2} + \right.$$

$$\begin{aligned}
 & \left( (112 a^2 + 64 a b - 7 b^2) \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\
 & \left( 1792 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( 5 (56 a^2 + 16 a b - 7 b^2) \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\
 & \left( 1792 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 28 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^7 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 14 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( 5 a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 56 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( 5 a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 56 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\
 & \left( b^2 \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\
 & \left( 128 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^8 (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\
 & \left( a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 28 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^7 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( -28 a^2 + 24 a b - 7 b^2 \right) \cos [c + d x]^2 (a + b \tan [c + d x])^2 / \\
 & \left( 1344 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\
 & \left( a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\
 & \left( 14 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \left( -112 a^2 + 64 a b + 7 b^2 \right) \cos [c + d x]^2 (a + b \tan [c + d x])^2 / \\
 & \left( 1792 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\
 & \left( 5 a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) /
 \end{aligned}$$

$$\begin{aligned} & \left( 56 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\ & \left( 5 (56 a^2 - 16 a b - 7 b^2) \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\ & \left( 1792 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 (a \cos [c + d x] + b \sin [c + d x])^2 \right) - \\ & \left( 5 a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\ & \left( 56 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) (a \cos [c + d x] + b \sin [c + d x])^2 \right) \end{aligned}$$

**Problem 524: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^5 (a + b \tan [c + d x])^2 dx$$

Optimal (type 3, 131 leaves, 5 steps):

$$\begin{aligned} & \frac{(6 a^2 - b^2) \operatorname{ArcTanh}[\sin [c + d x]]}{16 d} + \frac{7 a b \sec [c + d x]^5}{30 d} + \frac{(6 a^2 - b^2) \sec [c + d x] \tan [c + d x]}{16 d} + \\ & \frac{(6 a^2 - b^2) \sec [c + d x]^3 \tan [c + d x]}{24 d} + \frac{b \sec [c + d x]^5 (a + b \tan [c + d x])}{6 d} \end{aligned}$$

Result (type 3, 1175 leaves):

$$\begin{aligned} & \frac{3 a b \cos [c + d x]^2 (a + b \tan [c + d x])^2}{20 d (a \cos [c + d x] + b \sin [c + d x])^2} + \\ & \left( (-6 a^2 + b^2) \cos [c + d x]^2 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a + b \tan [c + d x])^2 \right) / \\ & \left( 16 d (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\ & \left( (6 a^2 - b^2) \cos [c + d x]^2 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a + b \tan [c + d x])^2 \right) / \\ & \left( 16 d (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \left( b^2 \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\ & \left( 48 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\ & \left( (5 a^2 + 4 a b) \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\ & \left( 80 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\ & \left( (30 a^2 + 12 a b - 5 b^2) \cos [c + d x]^2 (a + b \tan [c + d x])^2 \right) / \\ & \left( 160 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\ & \left( a b \cos [c + d x]^2 \sin \left[ \frac{1}{2} (c + d x) \right] (a + b \tan [c + d x])^2 \right) / \\ & \left( 10 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \end{aligned}$$

$$\begin{aligned}
 & \left( 3 a b \cos [c+d x]^2 \sin \left[ \frac{1}{2}(c+d x) \right] (a+b \tan [c+d x])^2 \right) / \\
 & \left( 20 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] - \sin \left[ \frac{1}{2}(c+d x) \right] \right)^3 (a \cos [c+d x] + b \sin [c+d x])^2 \right) + \\
 & \left( 3 a b \cos [c+d x]^2 \sin \left[ \frac{1}{2}(c+d x) \right] (a+b \tan [c+d x])^2 \right) / \\
 & \left( 20 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] - \sin \left[ \frac{1}{2}(c+d x) \right] \right) (a \cos [c+d x] + b \sin [c+d x])^2 \right) - \\
 & \left( b^2 \cos [c+d x]^2 (a+b \tan [c+d x])^2 \right) / \\
 & \left( 48 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right)^6 (a \cos [c+d x] + b \sin [c+d x])^2 \right) - \\
 & \left( a b \cos [c+d x]^2 \sin \left[ \frac{1}{2}(c+d x) \right] (a+b \tan [c+d x])^2 \right) / \\
 & \left( 10 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right)^5 (a \cos [c+d x] + b \sin [c+d x])^2 \right) + \\
 & \left( -5 a^2 + 4 a b \right) \cos [c+d x]^2 (a+b \tan [c+d x])^2 / \\
 & \left( 80 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right)^4 (a \cos [c+d x] + b \sin [c+d x])^2 \right) - \\
 & \left( 3 a b \cos [c+d x]^2 \sin \left[ \frac{1}{2}(c+d x) \right] (a+b \tan [c+d x])^2 \right) / \\
 & \left( 20 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right)^3 (a \cos [c+d x] + b \sin [c+d x])^2 \right) + \\
 & \left( -30 a^2 + 12 a b + 5 b^2 \right) \cos [c+d x]^2 (a+b \tan [c+d x])^2 / \\
 & \left( 160 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right)^2 (a \cos [c+d x] + b \sin [c+d x])^2 \right) - \\
 & \left( 3 a b \cos [c+d x]^2 \sin \left[ \frac{1}{2}(c+d x) \right] (a+b \tan [c+d x])^2 \right) / \\
 & \left( 20 d \left( \cos \left[ \frac{1}{2}(c+d x) \right] + \sin \left[ \frac{1}{2}(c+d x) \right] \right) (a \cos [c+d x] + b \sin [c+d x])^2 \right)
 \end{aligned}$$

**Problem 525: Result more than twice size of optimal antiderivative.**

$$\int \sec [c+d x]^3 (a+b \tan [c+d x])^2 dx$$

Optimal (type 3, 99 leaves, 4 steps):

$$\frac{(4 a^2 - b^2) \operatorname{ArcTanh}[\sin [c+d x]]}{8 d} + \frac{5 a b \sec [c+d x]^3}{12 d} + \frac{(4 a^2 - b^2) \sec [c+d x] \tan [c+d x]}{8 d} + \frac{b \sec [c+d x]^3 (a+b \tan [c+d x])}{4 d}$$

Result (type 3, 851 leaves):

$$\begin{aligned}
& \frac{a b \cos [c+d x]^2 (a+b \tan [c+d x])^2}{3 d (a \cos [c+d x]+b \sin [c+d x])^2} + \\
& \left( (-4 a^2+b^2) \cos [c+d x]^2 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right] (a+b \tan [c+d x])^2\right) / \\
& \left(8 d (a \cos [c+d x]+b \sin [c+d x])^2\right) + \\
& \left( (4 a^2-b^2) \cos [c+d x]^2 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right] (a+b \tan [c+d x])^2\right) / \\
& \left(8 d (a \cos [c+d x]+b \sin [c+d x])^2\right) + \left(b^2 \cos [c+d x]^2 (a+b \tan [c+d x])^2\right) / \\
& \left(16 d \left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4 (a \cos [c+d x]+b \sin [c+d x])^2\right) + \\
& \left((12 a^2+8 a b-3 b^2) \cos [c+d x]^2 (a+b \tan [c+d x])^2\right) / \\
& \left(48 d \left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2 (a \cos [c+d x]+b \sin [c+d x])^2\right) + \\
& \left(a b \cos [c+d x]^2 \sin \left[\frac{1}{2}(c+d x)\right] (a+b \tan [c+d x])^2\right) / \\
& \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^3 (a \cos [c+d x]+b \sin [c+d x])^2\right) + \\
& \left(a b \cos [c+d x]^2 \sin \left[\frac{1}{2}(c+d x)\right] (a+b \tan [c+d x])^2\right) / \\
& \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right) (a \cos [c+d x]+b \sin [c+d x])^2\right) - \\
& \left(b^2 \cos [c+d x]^2 (a+b \tan [c+d x])^2\right) / \\
& \left(16 d \left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4 (a \cos [c+d x]+b \sin [c+d x])^2\right) - \\
& \left(a b \cos [c+d x]^2 \sin \left[\frac{1}{2}(c+d x)\right] (a+b \tan [c+d x])^2\right) / \\
& \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^3 (a \cos [c+d x]+b \sin [c+d x])^2\right) + \\
& \left((-12 a^2+8 a b+3 b^2) \cos [c+d x]^2 (a+b \tan [c+d x])^2\right) / \\
& \left(48 d \left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2 (a \cos [c+d x]+b \sin [c+d x])^2\right) - \\
& \left(a b \cos [c+d x]^2 \sin \left[\frac{1}{2}(c+d x)\right] (a+b \tan [c+d x])^2\right) / \\
& \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right) (a \cos [c+d x]+b \sin [c+d x])^2\right)
\end{aligned}$$

**Problem 526: Result more than twice size of optimal antiderivative.**

$$\int \sec [c+d x] (a+b \tan [c+d x])^2 dx$$

Optimal (type 3, 65 leaves, 3 steps):

$$\frac{(2a^2 - b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2d} + \frac{3ab \operatorname{Sec}[c + dx]}{2d} + \frac{b \operatorname{Sec}[c + dx] (a + b \operatorname{Tan}[c + dx])}{2d}$$

Result (type 3, 181 leaves):

$$\begin{aligned} & \frac{1}{4d} \left( 8ab + (-4a^2 + 2b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \right. \\ & 4a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \\ & 2b^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \frac{b^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\ & \left. 16ab \operatorname{Sec}[c + dx] \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]^2 - \frac{b^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)^2} \right) \end{aligned}$$

**Problem 534: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^2 (a + b \operatorname{Tan}[c + dx])^3 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + b \operatorname{Tan}[c + dx])^4}{4bd}$$

Result (type 3, 79 leaves):

$$\frac{1}{8d} \operatorname{Sec}[c + dx]^4 \left( (6a^2b - 2b^3) \operatorname{Cos}[2(c + dx)] + a(6ab + 2(a^2 + b^2) \operatorname{Sin}[2(c + dx)] + (a^2 - b^2) \operatorname{Sin}[4(c + dx)]) \right)$$

**Problem 537: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^5 (a + b \operatorname{Tan}[c + dx])^3 dx$$

Optimal (type 3, 159 leaves, 6 steps):

$$\begin{aligned} & \frac{3a(2a^2 - b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{16d} + \\ & \frac{3a(2a^2 - b^2) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{16d} + \frac{a(2a^2 - b^2) \operatorname{Sec}[c + dx]^3 \operatorname{Tan}[c + dx]}{8d} + \\ & \frac{b \operatorname{Sec}[c + dx]^5 (a + b \operatorname{Tan}[c + dx])^2}{7d} + \frac{b \operatorname{Sec}[c + dx]^5 (4(8a^2 - b^2) + 15ab \operatorname{Tan}[c + dx])}{70d} \end{aligned}$$

Result (type 3, 637 leaves):

$$\begin{aligned} & \frac{1}{35840d} \operatorname{Sec}[c+dx]^7 \left( 10752a^2b + 1536b^3 + 3584(3a^2b - b^3) \operatorname{Cos}[2(c+dx)] - \right. \\ & 4410a^3 \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 2205a^2b \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 1470a^3 \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 735a^2b \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 210a^3 \operatorname{Cos}[7(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 105a^2b \operatorname{Cos}[7(c+dx)] \\ & \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 3675a(2a^2 - b^2) \operatorname{Cos}[c+dx] \\ & \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \right. \\ & 4410a^3 \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 2205a^2b \operatorname{Cos}[3(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 1470a^3 \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 735a^2b \operatorname{Cos}[5(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 210a^3 \operatorname{Cos}[7(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 105a^2b \operatorname{Cos}[7(c+dx)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & 4340a^3 \operatorname{Sin}[2(c+dx)] + 6790a^2b \operatorname{Sin}[2(c+dx)] + 2800a^3 \operatorname{Sin}[4(c+dx)] - \\ & \left. 1400a^2b \operatorname{Sin}[4(c+dx)] + 420a^3 \operatorname{Sin}[6(c+dx)] - 210a^2b \operatorname{Sin}[6(c+dx)] \right) \end{aligned}$$

**Problem 538: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Tan}[c+dx])^3 dx$$

Optimal (type 3, 126 leaves, 5 steps):

$$\begin{aligned} & \frac{a(4a^2 - 3b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \frac{a(4a^2 - 3b^2) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \\ & \frac{b \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Tan}[c+dx])^2}{5d} + \frac{b \operatorname{Sec}[c+dx]^3 (8(6a^2 - b^2) + 21ab \operatorname{Tan}[c+dx])}{60d} \end{aligned}$$

Result (type 3, 464 leaves):



$$\begin{aligned}
 & \frac{1}{1920 d} \operatorname{Sec}[c+d x]^5 \left( 960 a^2 b + 64 b^3 + 320 (3 a^2 b - b^3) \operatorname{Cos}[2(c+d x)] - \right. \\
 & 300 a^3 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + \\
 & 225 a b^2 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \\
 & 60 a^3 \operatorname{Cos}[5(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + 45 a b^2 \operatorname{Cos}[5(c+d x)] \\
 & \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - 150 a (4 a^2 - 3 b^2) \operatorname{Cos}[c+d x] \\
 & \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right) + \right. \\
 & 300 a^3 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \\
 & 225 a b^2 \operatorname{Cos}[3(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + \\
 & 60 a^3 \operatorname{Cos}[5(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \\
 & 45 a b^2 \operatorname{Cos}[5(c+d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + 240 a^3 \operatorname{Sin}[2(c+d x)] + \\
 & \left. 540 a b^2 \operatorname{Sin}[2(c+d x)] + 120 a^3 \operatorname{Sin}[4(c+d x)] - 90 a b^2 \operatorname{Sin}[4(c+d x)] \right)
 \end{aligned}$$

**Problem 539: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x] (a+b \operatorname{Tan}[c+d x])^3 dx$$

Optimal (type 3, 91 leaves, 4 steps):

$$\begin{aligned}
 & \frac{a (2 a^2 - 3 b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \\
 & \frac{b \operatorname{Sec}[c+d x] (a+b \operatorname{Tan}[c+d x])^2}{3 d} + \frac{b \operatorname{Sec}[c+d x] (4 (4 a^2 - b^2) + 5 a b \operatorname{Tan}[c+d x])}{6 d}
 \end{aligned}$$

Result (type 3, 293 leaves):

$$\frac{1}{12 d} \left( 36 a^2 b - 10 b^3 - 6 a (2 a^2 - 3 b^2) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + 12 a^3 \right. \\ \left. \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - 18 a b^2 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \\ \frac{9 a b^2}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \frac{b^3}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\ 2 b (18 a^2 - b^2 + 2 b^2 \operatorname{Cos} [c + d x] + (18 a^2 - 5 b^2) \operatorname{Cos} [2 (c + d x)]) \operatorname{Sec} [c + d x]^3 \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]^2 - \\ \left. \frac{9 a b^2}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \frac{b^3}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^2} \right)$$

**Problem 547: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Cos} [c + d x]^2}{a + b \operatorname{Tan} [c + d x]} dx$$

Optimal (type 3, 93 leaves, 7 steps):

$$\frac{a (a^2 + 3 b^2) x}{2 (a^2 + b^2)^2} + \frac{b^3 \operatorname{Log} [a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]]}{(a^2 + b^2)^2 d} + \frac{\operatorname{Cos} [c + d x]^2 (b + a \operatorname{Tan} [c + d x])}{2 (a^2 + b^2) d}$$

Result (type 3, 143 leaves):

$$\frac{1}{4 (a^2 + b^2)^2 d} \left( 2 a^3 c + 6 a b^2 c + 4 i b^3 c + 2 a^3 d x + 6 a b^2 d x + \right. \\ \left. 4 i b^3 d x - 4 i b^3 \operatorname{ArcTan} [\operatorname{Tan} [c + d x]] + b (a^2 + b^2) \operatorname{Cos} [2 (c + d x)] + \right. \\ \left. 2 b^3 \operatorname{Log} [(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2] + a^3 \operatorname{Sin} [2 (c + d x)] + a b^2 \operatorname{Sin} [2 (c + d x)] \right)$$

**Problem 549: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]^5}{a + b \operatorname{Tan} [c + d x]} dx$$

Optimal (type 3, 140 leaves, 9 steps):

$$\frac{a (2 a^2 + 3 b^2) \operatorname{ArcTanh} [\operatorname{Sin} [c + d x]]}{2 b^4 d} - \frac{(a^2 + b^2)^{3/2} \operatorname{ArcTanh} \left[ \frac{\operatorname{Cos} [c + d x] (b - a \operatorname{Tan} [c + d x])}{\sqrt{a^2 + b^2}} \right]}{b^4 d} + \\ \frac{(a^2 + b^2) \operatorname{Sec} [c + d x]}{b^3 d} + \frac{\operatorname{Sec} [c + d x]^3}{3 b d} - \frac{a \operatorname{Sec} [c + d x] \operatorname{Tan} [c + d x]}{2 b^2 d}$$

Result (type 3, 321 leaves):

$$\frac{1}{24 b^4 d} \left( 48 (a^2 + b^2)^{3/2} \operatorname{ArcTanh} \left[ \frac{-b + a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}} \right] + \right. \\
 \operatorname{Sec} [c + d x]^3 \left( 12 a^2 b + 20 b^3 + 12 b (a^2 + b^2) \operatorname{Cos} [2 (c + d x)] + \right. \\
 6 a^3 \operatorname{Cos} [3 (c + d x)] \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + \\
 9 a b^2 \operatorname{Cos} [3 (c + d x)] \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + 9 a (2 a^2 + 3 b^2) \operatorname{Cos} [c + d x] \\
 \left. \left( \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \\
 6 a^3 \operatorname{Cos} [3 (c + d x)] \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - \\
 \left. \left. 9 a b^2 \operatorname{Cos} [3 (c + d x)] \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - 6 a b^2 \operatorname{Sin} [2 (c + d x)] \right) \right) \right)$$

**Problem 554: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]^8}{(a + b \operatorname{Tan} [c + d x])^2} dx$$

Optimal (type 3, 178 leaves, 3 steps):

$$\frac{6 a (a^2 + b^2)^2 \operatorname{Log} [a + b \operatorname{Tan} [c + d x]]}{b^7 d} + \\
 \frac{(5 a^4 + 9 a^2 b^2 + 3 b^4) \operatorname{Tan} [c + d x]}{b^6 d} - \frac{a (2 a^2 + 3 b^2) \operatorname{Tan} [c + d x]^2}{b^5 d} + \\
 \frac{(a^2 + b^2) \operatorname{Tan} [c + d x]^3}{b^4 d} - \frac{a \operatorname{Tan} [c + d x]^4}{2 b^3 d} + \frac{\operatorname{Tan} [c + d x]^5}{5 b^2 d} - \frac{(a^2 + b^2)^3}{b^7 d (a + b \operatorname{Tan} [c + d x])}$$

Result (type 3, 373 leaves):

$$\frac{1}{160 a b^7 d (a + b \operatorname{Tan} [c + d x])} \\
 (b \operatorname{Sec} [c + d x]^6 (-70 a^5 b - 60 a^3 b^3 + 50 a b^5 - 5 a b (27 a^4 + 32 a^2 b^2 + b^4) \operatorname{Cos} [2 (c + d x)] - \\
 2 (45 a^5 b + 70 a^3 b^3 + 17 a b^5) \operatorname{Cos} [4 (c + d x)] - 25 a^5 b \operatorname{Cos} [6 (c + d x)] - \\
 40 a^3 b^3 \operatorname{Cos} [6 (c + d x)] - 11 a b^5 \operatorname{Cos} [6 (c + d x)] + 120 a^6 \operatorname{Sin} [4 (c + d x)] + 200 a^4 b^2 \\
 \operatorname{Sin} [4 (c + d x)] + 76 a^2 b^4 \operatorname{Sin} [4 (c + d x)] + 20 b^6 \operatorname{Sin} [4 (c + d x)] + 30 a^6 \operatorname{Sin} [6 (c + d x)] + \\
 55 a^4 b^2 \operatorname{Sin} [6 (c + d x)] + 26 a^2 b^4 \operatorname{Sin} [6 (c + d x)] + 5 b^6 \operatorname{Sin} [6 (c + d x)]) + \\
 10 b (30 a^6 + 47 a^4 b^2 + 10 a^2 b^4 + 5 b^6) \operatorname{Sec} [c + d x]^4 \operatorname{Tan} [c + d x] + \\
 960 a^2 (a^2 + b^2)^2 (\operatorname{Log} [\operatorname{Cos} [c + d x]] - \operatorname{Log} [a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]]) (a + b \operatorname{Tan} [c + d x]))$$

### Problem 558: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2}{(a+b \tan [c+d x])^2} d x$$

Optimal (type 3, 152 leaves, 7 steps):

$$\frac{(a^4 + 6 a^2 b^2 - 3 b^4) x}{2 (a^2 + b^2)^3} + \frac{4 a b^3 \operatorname{Log}[a \cos [c+d x] + b \sin [c+d x]]}{(a^2 + b^2)^3 d} +$$

$$\frac{b (a^2 - 3 b^2)}{2 (a^2 + b^2)^2 d (a+b \tan [c+d x])} + \frac{\cos [c+d x]^2 (b+a \tan [c+d x])}{2 (a^2 + b^2) d (a+b \tan [c+d x])}$$

Result (type 3, 331 leaves):

$$\frac{1}{4 a (a^2 + b^2)^3 d (a+b \tan [c+d x])} (2 a^6 c + 12 a^4 b^2 c - 6 a^2 b^4 c + 2 a^6 d x + 12 a^4 b^2 d x - 6 a^2 b^4 d x +$$

$$16 a^3 b^3 \operatorname{Log}[a \cos [c+d x] + b \sin [c+d x]] + 2 a b (a^4 - b^4) \sin [c+d x]^2 + a^6 \sin [2 (c+d x)] -$$

$$a^2 b^4 \sin [2 (c+d x)] + 4 a^2 b^4 \tan [c+d x] + 4 b^6 \tan [c+d x] + 2 a^5 b c \tan [c+d x] +$$

$$12 a^3 b^3 c \tan [c+d x] - 6 a b^5 c \tan [c+d x] + 2 a^5 b d x \tan [c+d x] + 12 a^3 b^3 d x \tan [c+d x] -$$

$$6 a b^5 d x \tan [c+d x] + 16 a^2 b^4 \operatorname{Log}[a \cos [c+d x] + b \sin [c+d x]] \tan [c+d x] +$$

$$2 a^2 b (a^2 + b^2) \cos [2 (c+d x)] (a+b \tan [c+d x]))$$

### Problem 559: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4}{(a+b \tan [c+d x])^2} d x$$

Optimal (type 3, 235 leaves, 8 steps):

$$\frac{3 (a^6 + 5 a^4 b^2 + 15 a^2 b^4 - 5 b^6) x}{8 (a^2 + b^2)^4} + \frac{6 a b^5 \operatorname{Log}[a \cos [c+d x] + b \sin [c+d x]]}{(a^2 + b^2)^4 d} +$$

$$\frac{3 b (a^2 - b^2) (a^2 + 5 b^2)}{8 (a^2 + b^2)^3 d (a+b \tan [c+d x])} + \frac{\cos [c+d x]^4 (b+a \tan [c+d x])}{4 (a^2 + b^2) d (a+b \tan [c+d x])} -$$

$$\frac{\cos [c+d x]^2 (b (a^2 - 5 b^2) - 3 a (a^2 + 3 b^2) \tan [c+d x])}{8 (a^2 + b^2)^2 d (a+b \tan [c+d x])}$$

Result (type 3, 737 leaves):

1

$$\begin{aligned}
 & 64 a (a^2 + b^2)^4 d (a + b \tan [c + d x]) \\
 & \left( 13 a^7 b + 59 a^5 b^3 + 15 a^3 b^5 - 31 a b^7 + 24 a^8 c + 120 a^6 b^2 c + 360 a^4 b^4 c + 384 a^3 b^5 c - \right. \\
 & \quad 120 a^2 b^6 c + 24 a^8 d x + 120 a^6 b^2 d x + 360 a^4 b^4 d x + 384 a^3 b^5 d x - 120 a^2 b^6 d x + \\
 & \quad 6 a b (a^2 + b^2)^2 (a^2 + 5 b^2) \cos [2 (c + d x)] + 192 a^3 b^5 \log [(a \cos [c + d x] + b \sin [c + d x])^2] + \\
 & \quad a^7 b \cos [5 (c + d x)] \sec [c + d x] + 3 a^5 b^3 \cos [5 (c + d x)] \sec [c + d x] + \\
 & \quad 3 a^3 b^5 \cos [5 (c + d x)] \sec [c + d x] + a b^7 \cos [5 (c + d x)] \sec [c + d x] + \\
 & \quad 9 a^8 \sec [c + d x] \sin [3 (c + d x)] + 39 a^6 b^2 \sec [c + d x] \sin [3 (c + d x)] + \\
 & \quad 51 a^4 b^4 \sec [c + d x] \sin [3 (c + d x)] + 21 a^2 b^6 \sec [c + d x] \sin [3 (c + d x)] + \\
 & \quad a^8 \sec [c + d x] \sin [5 (c + d x)] + 3 a^6 b^2 \sec [c + d x] \sin [5 (c + d x)] + \\
 & \quad 3 a^4 b^4 \sec [c + d x] \sin [5 (c + d x)] + a^2 b^6 \sec [c + d x] \sin [5 (c + d x)] + \\
 & \quad 8 a^8 \tan [c + d x] + 24 a^6 b^2 \tan [c + d x] - 40 a^4 b^4 \tan [c + d x] + 8 a^2 b^6 \tan [c + d x] + \\
 & \quad 64 b^8 \tan [c + d x] + 24 a^7 b c \tan [c + d x] + 120 a^5 b^3 c \tan [c + d x] + 360 a^3 b^5 c \tan [c + d x] + \\
 & \quad 384 a^2 b^6 c \tan [c + d x] - 120 a b^7 c \tan [c + d x] + 24 a^7 b d x \tan [c + d x] + \\
 & \quad 120 a^5 b^3 d x \tan [c + d x] + 360 a^3 b^5 d x \tan [c + d x] + 384 a^2 b^6 d x \tan [c + d x] - \\
 & \quad 120 a b^7 d x \tan [c + d x] + 192 a^2 b^6 \log [(a \cos [c + d x] + b \sin [c + d x])^2] \tan [c + d x] - \\
 & \quad \left. 384 a^2 b^5 \operatorname{ArcTan}[\tan [c + d x]] (a + b \tan [c + d x]) \right)
 \end{aligned}$$

Problem 560: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^7}{(a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 235 leaves, 8 steps):

$$\begin{aligned}
 & \frac{5 (8 a^4 + 12 a^2 b^2 + 3 b^4) \operatorname{ArcSinh}[\tan [c + d x]] \sec [c + d x]}{8 b^6 d \sqrt{\sec [c + d x]^2}} + \\
 & \frac{5 a (a^2 + b^2)^{3/2} \operatorname{ArcTanh}\left[\frac{b - a \tan [c + d x]}{\sqrt{a^2 + b^2} \sqrt{\sec [c + d x]^2}}\right] \sec [c + d x]}{b^6 d \sqrt{\sec [c + d x]^2}} - \frac{5 \sec [c + d x]^3 (4 a - 3 b \tan [c + d x])}{12 b^3 d} - \\
 & \frac{\sec [c + d x]^5}{b d (a + b \tan [c + d x])} - \frac{5 \sec [c + d x] (8 a (a^2 + b^2) - b (4 a^2 + 3 b^2) \tan [c + d x])}{8 b^5 d}
 \end{aligned}$$

Result (type 3, 1152 leaves):

$$\begin{aligned}
 & - \frac{(a - ib)^2 (a + ib)^2 \operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])}{b^5 d (a + b \operatorname{Tan}[c + dx])^2} - \\
 & \frac{a (12 a^2 + 13 b^2) \operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{3 b^5 d (a + b \operatorname{Tan}[c + dx])^2} + \\
 & \left( 10 i a (a + ib) (i a + b) \sqrt{a^2 + b^2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a^2 + b^2} \left( -b \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + a \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)}{a^2 \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + b^2 \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right]} \right] \right) \\
 & \operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \Big/ (b^6 d (a + b \operatorname{Tan}[c + dx])^2) - \\
 & \left( 5 (8 a^4 + 12 a^2 b^2 + 3 b^4) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right] \operatorname{Sec}[c + dx]^2 \right. \\
 & \left. (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \right) \Big/ (8 b^6 d (a + b \operatorname{Tan}[c + dx])^2) + \\
 & \left( 5 (8 a^4 + 12 a^2 b^2 + 3 b^4) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right] \operatorname{Sec}[c + dx]^2 \right. \\
 & \left. (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \right) \Big/ (8 b^6 d (a + b \operatorname{Tan}[c + dx])^2) + \\
 & \frac{\operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{16 b^2 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^4 (a + b \operatorname{Tan}[c + dx])^2} + \\
 & \frac{(36 a^2 - 8 a b + 21 b^2) \operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{48 b^4 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^2 (a + b \operatorname{Tan}[c + dx])^2} - \\
 & \frac{a \operatorname{Sec}[c + dx]^2 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{3 b^3 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^3 (a + b \operatorname{Tan}[c + dx])^2} - \\
 & \frac{\operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{16 b^2 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^4 (a + b \operatorname{Tan}[c + dx])^2} + \\
 & \frac{a \operatorname{Sec}[c + dx]^2 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{3 b^3 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^3 (a + b \operatorname{Tan}[c + dx])^2} + \\
 & \frac{(-36 a^2 - 8 a b - 21 b^2) \operatorname{Sec}[c + dx]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2}{48 b^4 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right)^2 (a + b \operatorname{Tan}[c + dx])^2} + \left( \operatorname{Sec}[c + dx]^2 \right. \\
 & \left. \left( -12 a^3 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] - 13 a b^2 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \right) \Big/ \\
 & \left( 3 b^5 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) (a + b \operatorname{Tan}[c + dx])^2 \right) + \left( \operatorname{Sec}[c + dx]^2 \right. \\
 & \left. \left( 12 a^3 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + 13 a b^2 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \right) \Big/ \\
 & \left( 3 b^5 d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) (a + b \operatorname{Tan}[c + dx])^2 \right)
 \end{aligned}$$

Problem 561: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^5}{(a + b \text{Tan}[c + d x])^2} dx$$

Optimal (type 3, 176 leaves, 7 steps):

$$\frac{3 (2 a^2 + b^2) \text{ArcSinh}[\text{Tan}[c + d x]] \text{Sec}[c + d x]}{2 b^4 d \sqrt{\text{Sec}[c + d x]^2}} +$$

$$\frac{3 a \sqrt{a^2 + b^2} \text{ArcTanh}\left[\frac{b - a \text{Tan}[c + d x]}{\sqrt{a^2 + b^2} \sqrt{\text{Sec}[c + d x]^2}}\right] \text{Sec}[c + d x]}{b^4 d \sqrt{\text{Sec}[c + d x]^2}} -$$

$$\frac{3 \text{Sec}[c + d x] (2 a - b \text{Tan}[c + d x])}{2 b^3 d} - \frac{\text{Sec}[c + d x]^3}{b d (a + b \text{Tan}[c + d x])}$$

Result (type 3, 709 leaves):

$$\begin{aligned}
& - \frac{(a - i b) (a + i b) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])}{b^3 d (a + b \operatorname{Tan}[c + d x])^2} - \\
& \frac{2 a \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2}{b^3 d (a + b \operatorname{Tan}[c + d x])^2} - \\
& \left( 6 a \sqrt{a^2 + b^2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a^2 + b^2} (-b \operatorname{Cos}[\frac{1}{2}(c + d x)] + a \operatorname{Sin}[\frac{1}{2}(c + d x)])}{a^2 \operatorname{Cos}[\frac{1}{2}(c + d x)] + b^2 \operatorname{Cos}[\frac{1}{2}(c + d x)]} \right] \right) \\
& \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \Big/ (b^4 d (a + b \operatorname{Tan}[c + d x])^2) - \\
& \left( 3 (2 a^2 + b^2) \operatorname{Log}[\operatorname{Cos}[\frac{1}{2}(c + d x)] - \operatorname{Sin}[\frac{1}{2}(c + d x)]] \right) \operatorname{Sec}[c + d x]^2 \\
& (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \Big/ (2 b^4 d (a + b \operatorname{Tan}[c + d x])^2) + \\
& \left( 3 (2 a^2 + b^2) \operatorname{Log}[\operatorname{Cos}[\frac{1}{2}(c + d x)] + \operatorname{Sin}[\frac{1}{2}(c + d x)]] \right) \operatorname{Sec}[c + d x]^2 \\
& (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \Big/ (2 b^4 d (a + b \operatorname{Tan}[c + d x])^2) + \\
& \frac{\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2}{4 b^2 d (\operatorname{Cos}[\frac{1}{2}(c + d x)] - \operatorname{Sin}[\frac{1}{2}(c + d x)])^2 (a + b \operatorname{Tan}[c + d x])^2} - \\
& \frac{2 a \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[\frac{1}{2}(c + d x)] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2}{b^3 d (\operatorname{Cos}[\frac{1}{2}(c + d x)] - \operatorname{Sin}[\frac{1}{2}(c + d x)]) (a + b \operatorname{Tan}[c + d x])^2} - \\
& \frac{\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2}{4 b^2 d (\operatorname{Cos}[\frac{1}{2}(c + d x)] + \operatorname{Sin}[\frac{1}{2}(c + d x)])^2 (a + b \operatorname{Tan}[c + d x])^2} + \\
& \frac{2 a \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[\frac{1}{2}(c + d x)] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2}{b^3 d (\operatorname{Cos}[\frac{1}{2}(c + d x)] + \operatorname{Sin}[\frac{1}{2}(c + d x)]) (a + b \operatorname{Tan}[c + d x])^2}
\end{aligned}$$

**Problem 566: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^8}{(a + b \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 3, 185 leaves, 3 steps):



$$\frac{3 (a^2 + b^2) (5 a^2 + b^2) \operatorname{Log}[a + b \operatorname{Tan}[c + d x]]}{b^7 d} - \frac{a (10 a^2 + 9 b^2) \operatorname{Tan}[c + d x]}{b^6 d} + \frac{3 (2 a^2 + b^2) \operatorname{Tan}[c + d x]^2}{2 b^5 d} - \frac{a \operatorname{Tan}[c + d x]^3}{b^4 d} + \frac{\operatorname{Tan}[c + d x]^4}{4 b^3 d} - \frac{(a^2 + b^2)^3}{2 b^7 d (a + b \operatorname{Tan}[c + d x])^2} + \frac{6 a (a^2 + b^2)^2}{b^7 d (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 1677 leaves):

$$\begin{aligned} & - \left( \left( 3 (5 a^4 + 6 a^2 b^2 + b^4) \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / \right. \\ & \quad \left. (b^7 d (a + b \operatorname{Tan}[c + d x])^3) \right) + \\ & \left( 3 (5 a^4 + 6 a^2 b^2 + b^4) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] \operatorname{Sec}[c + d x]^3 \right. \\ & \quad \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / (b^7 d (a + b \operatorname{Tan}[c + d x])^3) + \\ & \quad \frac{1}{672 a^2 b^6 (7 a^4 + 14 a^2 b^2 - 9 b^4) d (a + b \operatorname{Tan}[c + d x])^3} \\ & \operatorname{Sec}[c + d x]^7 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (-2940 a^{10} b + 294 a^7 b^3 - 14406 a^8 b^3 - 214284 a^6 b^4 - \\ & \quad 156180432 a^5 b^5 - 24276 a^6 b^5 + 113833223438 a^4 b^6 + 82968158000042 a^3 b^7 - 13664 a^4 b^7 - \\ & \quad 60471934588030612 a^2 b^8 - 388894133623929672573646381388896840320 a b^9 + \\ & \quad 9680 a^2 b^9 + 283448267107041312781534833978021668473234 a b^{10} - 1242 b^{11} + \\ & \quad 2205 a^{10} b \operatorname{Cos}[2(c + d x)] + 147 a^7 b^3 \operatorname{Cos}[2(c + d x)] + 147 a^8 b^3 \operatorname{Cos}[2(c + d x)] - \\ & \quad 107142 a^6 b^4 \operatorname{Cos}[2(c + d x)] - 78090216 a^5 b^5 \operatorname{Cos}[2(c + d x)] - 18774 a^6 b^5 \operatorname{Cos}[2(c + d x)] + \\ & \quad 56916611719 a^4 b^6 \operatorname{Cos}[2(c + d x)] + 41484079000021 a^3 b^7 \operatorname{Cos}[2(c + d x)] - \\ & \quad 10654 a^4 b^7 \operatorname{Cos}[2(c + d x)] - 30235967294015306 a^2 b^8 \operatorname{Cos}[2(c + d x)] - \\ & \quad 194447066811964836286823190694448420160 a b^9 \operatorname{Cos}[2(c + d x)] + \\ & \quad 7297 a^2 b^9 \operatorname{Cos}[2(c + d x)] + 141724133553520656390767416989010834236617 \\ & \quad a b^{10} \operatorname{Cos}[2(c + d x)] - 621 b^{11} \operatorname{Cos}[2(c + d x)] + 8820 a^{10} b \operatorname{Cos}[4(c + d x)] - \\ & \quad 294 a^7 b^3 \operatorname{Cos}[4(c + d x)] + 26754 a^8 b^3 \operatorname{Cos}[4(c + d x)] + 214284 a^6 b^4 \operatorname{Cos}[4(c + d x)] + \\ & \quad 156180432 a^5 b^5 \operatorname{Cos}[4(c + d x)] + 17304 a^6 b^5 \operatorname{Cos}[4(c + d x)] - \\ & \quad 113833223438 a^4 b^6 \operatorname{Cos}[4(c + d x)] - 82968158000042 a^3 b^7 \operatorname{Cos}[4(c + d x)] + \\ & \quad 11732 a^4 b^7 \operatorname{Cos}[4(c + d x)] + 60471934588030612 a^2 b^8 \operatorname{Cos}[4(c + d x)] + \\ & \quad 388894133623929672573646381388896840320 a b^9 \operatorname{Cos}[4(c + d x)] - \\ & \quad 8924 a^2 b^9 \operatorname{Cos}[4(c + d x)] - 283448267107041312781534833978021668473234 \\ & \quad a b^{10} \operatorname{Cos}[4(c + d x)] + 1242 b^{11} \operatorname{Cos}[4(c + d x)] + 3675 a^{10} b \operatorname{Cos}[6(c + d x)] - \\ & \quad 147 a^7 b^3 \operatorname{Cos}[6(c + d x)] + 12201 a^8 b^3 \operatorname{Cos}[6(c + d x)] + 107142 a^6 b^4 \operatorname{Cos}[6(c + d x)] + \\ & \quad 78090216 a^5 b^5 \operatorname{Cos}[6(c + d x)] + 10626 a^6 b^5 \operatorname{Cos}[6(c + d x)] - \\ & \quad 56916611719 a^4 b^6 \operatorname{Cos}[6(c + d x)] - 41484079000021 a^3 b^7 \operatorname{Cos}[6(c + d x)] + \\ & \quad 6370 a^4 b^7 \operatorname{Cos}[6(c + d x)] + 30235967294015306 a^2 b^8 \operatorname{Cos}[6(c + d x)] + \\ & \quad 194447066811964836286823190694448420160 a b^9 \operatorname{Cos}[6(c + d x)] - \\ & \quad 5029 a^2 b^9 \operatorname{Cos}[6(c + d x)] - 141724133553520656390767416989010834236617 \\ & \quad a b^{10} \operatorname{Cos}[6(c + d x)] + 621 b^{11} \operatorname{Cos}[6(c + d x)] - 11025 a^{11} \operatorname{Sin}[2(c + d x)] + \\ & \quad 735 a^8 b^2 \operatorname{Sin}[2(c + d x)] - 38955 a^9 b^2 \operatorname{Sin}[2(c + d x)] - 535710 a^7 b^3 \operatorname{Sin}[2(c + d x)] - \\ & \quad 390451080 a^6 b^4 \operatorname{Sin}[2(c + d x)] - 49056 a^7 b^4 \operatorname{Sin}[2(c + d x)] + \\ & \quad 284583058595 a^5 b^5 \operatorname{Sin}[2(c + d x)] + 207420395000105 a^4 b^6 \operatorname{Sin}[2(c + d x)] - \\ & \quad 43652 a^5 b^6 \operatorname{Sin}[2(c + d x)] - 151179836470076530 a^3 b^7 \operatorname{Sin}[2(c + d x)] - \\ & \quad 972235334059824181434115953472242100800 a^2 b^8 \operatorname{Sin}[2(c + d x)] + \end{aligned}$$

$$\begin{aligned}
& 26\,657\,a^3\,b^8\,\text{Sin}[2(c+dx)] + 708\,620\,667\,767\,603\,281\,953\,837\,084\,945\,054\,171\,183\,085 \\
& \quad \cdot a\,b^9\,\text{Sin}[2(c+dx)] - 3105\,a\,b^{10}\,\text{Sin}[2(c+dx)] - 8820\,a^{11}\,\text{Sin}[4(c+dx)] + \\
& 588\,a^8\,b^2\,\text{Sin}[4(c+dx)] - 29\,400\,a^9\,b^2\,\text{Sin}[4(c+dx)] - 428\,568\,a^7\,b^3\,\text{Sin}[4(c+dx)] - \\
& 312\,360\,864\,a^6\,b^4\,\text{Sin}[4(c+dx)] - 33\,012\,a^7\,b^4\,\text{Sin}[4(c+dx)] + \\
& 227\,666\,446\,876\,a^5\,b^5\,\text{Sin}[4(c+dx)] + 165\,936\,316\,000\,084\,a^4\,b^6\,\text{Sin}[4(c+dx)] - \\
& 31\,780\,a^5\,b^6\,\text{Sin}[4(c+dx)] - 120\,943\,869\,176\,061\,224\,a^3\,b^7\,\text{Sin}[4(c+dx)] - \\
& 777\,788\,267\,247\,859\,345\,147\,292\,762\,777\,793\,680\,640\,a^2\,b^8\,\text{Sin}[4(c+dx)] + \\
& 17\,848\,a^3\,b^8\,\text{Sin}[4(c+dx)] + 566\,896\,534\,214\,082\,625\,563\,069\,667\,956\,043\,336\,946\,468 \\
& \quad \cdot a\,b^9\,\text{Sin}[4(c+dx)] - 2484\,a\,b^{10}\,\text{Sin}[4(c+dx)] - 2205\,a^{11}\,\text{Sin}[6(c+dx)] + \\
& 147\,a^8\,b^2\,\text{Sin}[6(c+dx)] - 6615\,a^9\,b^2\,\text{Sin}[6(c+dx)] - 107\,142\,a^7\,b^3\,\text{Sin}[6(c+dx)] - \\
& 78\,090\,216\,a^6\,b^4\,\text{Sin}[6(c+dx)] - 6048\,a^7\,b^4\,\text{Sin}[6(c+dx)] + \\
& 56\,916\,611\,719\,a^5\,b^5\,\text{Sin}[6(c+dx)] + 41\,484\,079\,000\,021\,a^4\,b^6\,\text{Sin}[6(c+dx)] - \\
& 7420\,a^5\,b^6\,\text{Sin}[6(c+dx)] - 30\,235\,967\,294\,015\,306\,a^3\,b^7\,\text{Sin}[6(c+dx)] - \\
& 194\,447\,066\,811\,964\,836\,286\,823\,190\,694\,448\,420\,160\,a^2\,b^8\,\text{Sin}[6(c+dx)] + \\
& 3517\,a^3\,b^8\,\text{Sin}[6(c+dx)] + 141\,724\,133\,553\,520\,656\,390\,767\,416\,989\,010\,834\,236\,617 \\
& \quad \cdot a\,b^9\,\text{Sin}[6(c+dx)] - 621\,a\,b^{10}\,\text{Sin}[6(c+dx)]
\end{aligned}$$

**Problem 569: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c+dx]^2}{(a+b\tan[c+dx])^3} dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$-\frac{1}{2bd(a+b\tan[c+dx])^2}$$

Result (type 3, 58 leaves):

$$\frac{-b\text{Sec}[c+dx]^2 + 2\tan[c+dx](a+b\tan[c+dx])}{2(a^2+b^2)d(a+b\tan[c+dx])^2}$$

**Problem 570: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c+dx]^2}{(a+b\tan[c+dx])^3} dx$$

Optimal (type 3, 202 leaves, 7 steps):

$$\begin{aligned}
& \frac{a(a^4 + 10a^2b^2 - 15b^4)x}{2(a^2 + b^2)^4} + \\
& \frac{2b^3(5a^2 - b^2)\text{Log}[a\text{Cos}[c+dx] + b\text{Sin}[c+dx]]}{(a^2 + b^2)^4 d} + \frac{b(a^2 - 2b^2)}{2(a^2 + b^2)^2 d(a+b\tan[c+dx])^2} + \\
& \frac{\text{Cos}[c+dx]^2(b+a\tan[c+dx])}{2(a^2 + b^2)d(a+b\tan[c+dx])^2} + \frac{ab(a^2 - 11b^2)}{2(a^2 + b^2)^3 d(a+b\tan[c+dx])}
\end{aligned}$$

Result (type 3, 713 leaves):

$$\begin{aligned}
 & - \frac{b^5 \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{2 (a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3} + \\
 & \left( a (a^4 + 10 a^2 b^2 - 15 b^4) (c+dx) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
 & \left( 2 (a-ib)^4 (a+ib)^4 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
 & \left( 2 (5 i a^{11} b^3 + 5 a^{10} b^4 + 14 i a^9 b^5 + 14 a^8 b^6 + 12 i a^7 b^7 + 12 a^6 b^8 + 2 i a^5 b^9 + 2 a^4 b^{10} - i a^3 b^{11} - a^2 b^{12}) \right. \\
 & \quad \left. (c+dx) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
 & \left( a^2 (a-ib)^8 (a+ib)^7 d (a+b \operatorname{Tan}[c+dx])^3 \right) - \\
 & \left( 2 i (5 a^2 b^3 - b^5) \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
 & \left( (a^2 + b^2)^4 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
 & \left( b (3 a^2 - b^2) \operatorname{Cos}[2(c+dx)] \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
 & \left( 4 (a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
 & \left( (5 a^2 b^3 - b^5) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2] \operatorname{Sec}[c+dx]^3 \right. \\
 & \quad \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \left( (a^2 + b^2)^4 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
 & \left( a (a^2 - 3 b^2) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \operatorname{Sin}[2(c+dx)] \right) / \\
 & \left( 4 (a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
 & \frac{5 b^4 \operatorname{Sec}[c+dx]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 \operatorname{Tan}[c+dx]}{(a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3}
 \end{aligned}$$

**Problem 571: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx]^4}{(a+b \operatorname{Tan}[c+dx])^3} dx$$

Optimal (type 3, 295 leaves, 8 steps):

$$\begin{aligned}
 & \frac{3 a (a^6 + 7 a^4 b^2 + 35 a^2 b^4 - 35 b^6) x}{8 (a^2 + b^2)^5} + \frac{3 b^5 (7 a^2 - b^2) \operatorname{Log}[a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]]}{(a^2 + b^2)^5 d} + \\
 & \frac{3 b (a^4 + 5 a^2 b^2 - 4 b^4)}{8 (a^2 + b^2)^3 d (a+b \operatorname{Tan}[c+dx])^2} + \frac{\operatorname{Cos}[c+dx]^4 (b+a \operatorname{Tan}[c+dx])}{4 (a^2 + b^2) d (a+b \operatorname{Tan}[c+dx])^2} + \\
 & \frac{3 a b (a^4 + 6 a^2 b^2 - 27 b^4)}{8 (a^2 + b^2)^4 d (a+b \operatorname{Tan}[c+dx])} - \frac{\operatorname{Cos}[c+dx]^2 (2 b (a^2 - 3 b^2) - a (3 a^2 + 11 b^2) \operatorname{Tan}[c+dx])}{8 (a^2 + b^2)^2 d (a+b \operatorname{Tan}[c+dx])^2}
 \end{aligned}$$

Result (type 3, 924 leaves):

$$\begin{aligned}
& - \frac{b^7 \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{2 (a-ib)^4 (a+ib)^4 d (a+b \operatorname{Tan}[c+dx])^3} + \\
& \left( 3 a (a^6 + 7 a^4 b^2 + 35 a^2 b^4 - 35 b^6) (c+dx) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
& \left( 8 (a-ib)^5 (a+ib)^5 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( 3 (7 ia^{13} b^5 + 7 a^{12} b^6 + 27 ia^{11} b^7 + 27 a^{10} b^8 + 38 ia^9 b^9 + 38 a^8 b^{10} + 22 ia^7 b^{11} + 22 a^6 b^{12} + 3 ia^5 b^{13} + \right. \\
& \quad \left. 3 a^4 b^{14} - ia^3 b^{15} - a^2 b^{16}) (c+dx) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
& \left( a^2 (a-ib)^{10} (a+ib)^9 d (a+b \operatorname{Tan}[c+dx])^3 \right) - \\
& \left( 3 ia (7 a^2 b^5 - b^7) \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
& \left( (a^2 + b^2)^5 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( b (3 a^4 + 22 a^2 b^2 - 5 b^4) \operatorname{Cos}[2(c+dx)] \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
& \left( 8 (a-ib)^4 (a+ib)^4 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( b (3 a^2 - b^2) \operatorname{Cos}[4(c+dx)] \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \\
& \left( 32 (a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( 3 (7 a^2 b^5 - b^7) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2] \operatorname{Sec}[c+dx]^3 \right. \\
& \quad \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) / \left( 2 (a^2 + b^2)^5 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( a (a^4 + 4 a^2 b^2 - 9 b^4) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \operatorname{Sin}[2(c+dx)] \right) / \\
& \left( 4 (a-ib)^4 (a+ib)^4 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \left( a (a^2 - 3 b^2) \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \operatorname{Sin}[4(c+dx)] \right) / \\
& \left( 32 (a-ib)^3 (a+ib)^3 d (a+b \operatorname{Tan}[c+dx])^3 \right) + \\
& \frac{7 b^6 \operatorname{Sec}[c+dx]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 \operatorname{Tan}[c+dx]}{(a-ib)^4 (a+ib)^4 d (a+b \operatorname{Tan}[c+dx])^3}
\end{aligned}$$

**Problem 572: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^7}{(a+b \operatorname{Tan}[c+dx])^3} dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\begin{aligned}
& \frac{5 a (4 a^2 + 3 b^2) \operatorname{ArcSinh}[\operatorname{Tan}[c+dx]] \operatorname{Sec}[c+dx]}{2 b^6 d \sqrt{\operatorname{Sec}[c+dx]^2}} - \\
& \frac{5 \sqrt{a^2 + b^2} (4 a^2 + b^2) \operatorname{ArcTanh}\left[\frac{b-a \operatorname{Tan}[c+dx]}{\sqrt{a^2+b^2} \sqrt{\operatorname{Sec}[c+dx]^2}}\right] \operatorname{Sec}[c+dx]}{2 b^6 d \sqrt{\operatorname{Sec}[c+dx]^2}} - \frac{\operatorname{Sec}[c+dx]^5}{2 b d (a+b \operatorname{Tan}[c+dx])^2} + \\
& \frac{5 \operatorname{Sec}[c+dx]^3 (4 a + b \operatorname{Tan}[c+dx])}{6 b^3 d (a+b \operatorname{Tan}[c+dx])} + \frac{5 \operatorname{Sec}[c+dx] (4 a^2 + b^2 - 2 a b \operatorname{Tan}[c+dx])}{2 b^5 d}
\end{aligned}$$

Result (type 3, 688 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^6 d (a + b \tan [c + d x])^3} \operatorname{Sec}[c + d x]^3 (a \cos [c + d x] + b \sin [c + d x]) \\
 & \left( \frac{6 b^2 (a^2 + b^2)^2 \sin [c + d x]}{a} + \frac{6 (a - i b) (a + i b) b (8 a^2 - b^2) (a \cos [c + d x] + b \sin [c + d x])}{a} \right) + \\
 & 2 b (36 a^2 + 13 b^2) (a \cos [c + d x] + b \sin [c + d x])^2 + \\
 & 60 \sqrt{a^2 + b^2} (4 a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{-b + a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}} \right] (a \cos [c + d x] + b \sin [c + d x])^2 + \\
 & 30 a (4 a^2 + 3 b^2) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a \cos [c + d x] + b \sin [c + d x])^2 - \\
 & 30 a (4 a^2 + 3 b^2) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a \cos [c + d x] + b \sin [c + d x])^2 + \\
 & \frac{b^2 (-9 a + b) (a \cos [c + d x] + b \sin [c + d x])^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
 & \frac{2 b^3 \sin \left[ \frac{1}{2} (c + d x) \right] (a \cos [c + d x] + b \sin [c + d x])^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \left( 2 b (36 a^2 + 13 b^2) \sin \left[ \frac{1}{2} (c + d x) \right] (a \cos [c + d x] + b \sin [c + d x])^2 \right) / \\
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) - \\
 & \frac{2 b^3 \sin \left[ \frac{1}{2} (c + d x) \right] (a \cos [c + d x] + b \sin [c + d x])^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{b^2 (9 a + b) (a \cos [c + d x] + b \sin [c + d x])^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} - \\
 & \left( 2 b (36 a^2 + 13 b^2) \sin \left[ \frac{1}{2} (c + d x) \right] (a \cos [c + d x] + b \sin [c + d x])^2 \right) / \\
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \Big)
 \end{aligned}$$

**Problem 573: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^5}{(a + b \tan [c + d x])^3} dx$$

Optimal (type 3, 148 leaves, 7 steps):

$$-\frac{3 a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{b^4 d}-\frac{3\left(2 a^2+b^2\right) \operatorname{ArcTanh}\left[\frac{b \operatorname{Cos}[c+d x]-a \operatorname{Sin}[c+d x]}{\sqrt{a^2+b^2}}\right]}{2 b^4 \sqrt{a^2+b^2} d}-\frac{\operatorname{Sec}[c+d x]^3}{2 b d(a+b \operatorname{Tan}[c+d x])^2}+\frac{3 \operatorname{Sec}[c+d x](2 a+b \operatorname{Tan}[c+d x])}{2 b^3 d(a+b \operatorname{Tan}[c+d x])}$$

Result (type 3, 396 leaves):

$$\frac{1}{2 b^4 d(a+b \operatorname{Tan}[c+d x])^3} \operatorname{Sec}[c+d x]^3(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])\left(\frac{b^2\left(a^2+b^2\right) \operatorname{Sin}[c+d x]}{a}+\frac{(2 a-b) b(2 a+b)(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])}{a}\right)+2 b(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2+\frac{1}{\sqrt{a^2+b^2}} 6\left(2 a^2+b^2\right) \operatorname{ArcTanh}\left[\frac{-b+a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2+b^2}}\right](a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2+6 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right](a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2-6 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right](a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2+\frac{2 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right](a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2}{\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}-\frac{2 b \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right](a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2}{\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]})$$

**Problem 574: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Sec}[c+d x]^3}{(a+b \operatorname{Tan}[c+d x])^3} d x$$

Optimal (type 3, 95 leaves, 4 steps):

$$-\frac{\operatorname{ArcTanh}\left[\frac{b \operatorname{Cos}[c+d x]-a \operatorname{Sin}[c+d x]}{\sqrt{a^2+b^2}}\right]}{2\left(a^2+b^2\right)^{3 / 2} d}-\frac{\operatorname{Sec}[c+d x](b-a \operatorname{Tan}[c+d x])}{2\left(a^2+b^2\right) d(a+b \operatorname{Tan}[c+d x])^2}$$

Result (type 3, 132 leaves):

$$\left( (a^2 + b^2) (-b \cos [c + d x] + a \sin [c + d x]) + 2 \sqrt{a^2 + b^2} \operatorname{ArcTanh} \left[ \frac{-b + a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}} \right] (a \cos [c + d x] + b \sin [c + d x])^2 \right) / (2 (a - i b)^2 (a + i b)^2 d (a \cos [c + d x] + b \sin [c + d x])^2)$$

**Problem 601: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan [e + f x])^3}{(d \sec [e + f x])^{9/2}} dx$$

Optimal (type 4, 176 leaves, 4 steps):

$$\left( 2 a (7 a^2 + 6 b^2) \operatorname{EllipticE} \left[ \frac{1}{2} \operatorname{ArcTan} [\tan [e + f x]], 2 \right] (\sec [e + f x]^2)^{1/4} \right) / \left( 15 d^4 f \sqrt{d \sec [e + f x]} \right) - \frac{2 \cos [e + f x]^4 (b - a \tan [e + f x]) (a + b \tan [e + f x])^2}{9 d^4 f \sqrt{d \sec [e + f x]}} - \frac{2 \cos [e + f x]^2 (2 b (5 a^2 + 2 b^2) - a (7 a^2 + b^2) \tan [e + f x])}{45 d^4 f \sqrt{d \sec [e + f x]}}$$

Result (type 4, 372 leaves):

$$\left( \sec [e + f x]^{3/2} \left( \frac{2 (56 a^3 + 48 a b^2) \operatorname{EllipticE} \left[ \frac{1}{2} (e + f x), 2 \right]}{\sqrt{\cos [e + f x]} \sqrt{\sec [e + f x]}} - (2 (15 a^2 b + 7 b^3) \sin [e + f x]^2) \right) \right) / \left( \sqrt{1 - \cos [e + f x]^2} \sqrt{\sec [e + f x]} \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \left( a + b \tan [e + f x] \right)^3 \Big/ \left( 120 f (d \sec [e + f x])^{9/2} (a \cos [e + f x] + b \sin [e + f x])^3 \right) + \left( \sec [e + f x]^2 \left( -\frac{1}{90} b (15 a^2 + 4 b^2) \cos [e + f x] - \frac{1}{360} b (75 a^2 + 11 b^2) \cos [3 (e + f x)] - \frac{1}{72} b (3 a^2 - b^2) \cos [5 (e + f x)] + \frac{1}{180} a (19 a^2 - 3 b^2) \sin [e + f x] + \frac{1}{360} a (43 a^2 - 21 b^2) \sin [3 (e + f x)] + \frac{1}{72} a (a^2 - 3 b^2) \sin [5 (e + f x)] \right) \right) \Big/ \left( f (d \sec [e + f x])^{9/2} (a \cos [e + f x] + b \sin [e + f x])^3 \right)$$

**Problem 603: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \sec [e + f x])^{7/2}}{a + b \tan [e + f x]} dx$$

Optimal (type 4, 456 leaves, 17 steps):

$$\frac{2 d^2 (d \operatorname{Sec}[e+f x])^{3/2}}{3 b f} + \frac{(a^2 + b^2)^{3/4} d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{b^{5/2} f (\operatorname{Sec}[e+f x]^2)^{3/4}} -$$

$$\frac{(a^2 + b^2)^{3/4} d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{b^{5/2} f (\operatorname{Sec}[e+f x]^2)^{3/4}} +$$

$$\frac{2 a d^2 \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (d \operatorname{Sec}[e+f x])^{3/2}}{b^2 f (\operatorname{Sec}[e+f x]^2)^{3/4}} -$$

$$\frac{2 a d^2 \operatorname{Cos}[e+f x] (d \operatorname{Sec}[e+f x])^{3/2} \operatorname{Sin}[e+f x]}{b^2 f} -$$

$$\left( a \sqrt{a^2 + b^2} d^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right.$$

$$\left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / (b^3 f (\operatorname{Sec}[e+f x]^2)^{3/4}) +$$

$$\left( a \sqrt{a^2 + b^2} d^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right.$$

$$\left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / (b^3 f (\operatorname{Sec}[e+f x]^2)^{3/4})$$

Result (type 4, 31275 leaves): Display of huge result suppressed!

**Problem 604: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e+f x])^{5/2}}{a+b \operatorname{Tan}[e+f x]} dx$$

Optimal (type 4, 396 leaves, 17 steps):



$$\begin{aligned}
 & \frac{2 d^2 \sqrt{d \operatorname{Sec}[e+f x]}}{b f} - \frac{(a^2+b^2)^{1/4} d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b}(\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{b^{3/2} f (\operatorname{Sec}[e+f x]^2)^{1/4}} - \\
 & \frac{(a^2+b^2)^{1/4} d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b}(\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{b^{3/2} f (\operatorname{Sec}[e+f x]^2)^{1/4}} - \\
 & \frac{2 a d^2 \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] \sqrt{d \operatorname{Sec}[e+f x]}}{b^2 f (\operatorname{Sec}[e+f x]^2)^{1/4}} + \\
 & \left( a d^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+f x]} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( b^2 f (\operatorname{Sec}[e+f x]^2)^{1/4} \right) + \\
 & \left( a d^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+f x]} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( b^2 f (\operatorname{Sec}[e+f x]^2)^{1/4} \right)
 \end{aligned}$$

Result (type 4, 40058 leaves): Display of huge result suppressed!

### Problem 605: Result unnecessarily involves higher level functions.

$$\int \frac{(d \operatorname{Sec}[e+f x])^{3/2}}{a+b \operatorname{Tan}[e+f x]} dx$$

Optimal (type 4, 334 leaves, 13 steps):

$$\begin{aligned}
 & \frac{\operatorname{ArcTan}\left[\frac{\sqrt{b}(\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{\sqrt{b} (a^2+b^2)^{1/4} f (\operatorname{Sec}[e+f x]^2)^{3/4}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{b}(\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{\sqrt{b} (a^2+b^2)^{1/4} f (\operatorname{Sec}[e+f x]^2)^{3/4}} - \\
 & \left( a \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( b \sqrt{a^2+b^2} f (\operatorname{Sec}[e+f x]^2)^{3/4} \right) + \\
 & \left( a \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( b \sqrt{a^2+b^2} f (\operatorname{Sec}[e+f x]^2)^{3/4} \right)
 \end{aligned}$$

Result (type 6, 276 leaves):

$$\begin{aligned}
 & - \left( \left( 12 d^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{4}, \frac{1}{4}, \frac{3}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] (a + b \operatorname{Tan}[e + f x]) \right) \right) / \\
 & \left( b f \sqrt{d \operatorname{Sec}[e + f x]} \left( (a + i b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{4}, \frac{5}{4}, \frac{5}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] + \right. \\
 & \quad (a - i b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{4}, \frac{1}{4}, \frac{5}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] + \\
 & \quad \left. 6 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{4}, \frac{1}{4}, \frac{3}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] (a + b \operatorname{Tan}[e + f x]) \right) \right) \Big)
 \end{aligned}$$

**Problem 606: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{d \operatorname{Sec}[e + f x]}}{a + b \operatorname{Tan}[e + f x]} dx$$

Optimal (type 4, 324 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{\sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{b} (\operatorname{Sec}[e + f x]^2)^{1/4}}{(a^2 + b^2)^{1/4}} \right] \sqrt{d \operatorname{Sec}[e + f x]} - \sqrt{b} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} (\operatorname{Sec}[e + f x]^2)^{1/4}}{(a^2 + b^2)^{1/4}} \right] \sqrt{d \operatorname{Sec}[e + f x]}}{(a^2 + b^2)^{3/4} f (\operatorname{Sec}[e + f x]^2)^{1/4}} + \\
 & \left( a \operatorname{Cot}[e + f x] \operatorname{EllipticPi} \left[ -\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e + f x]^2)^{1/4}], -1 \right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e + f x]} \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( (a^2 + b^2) f (\operatorname{Sec}[e + f x]^2)^{1/4} + \right. \\
 & \left( a \operatorname{Cot}[e + f x] \operatorname{EllipticPi} \left[ \frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e + f x]^2)^{1/4}], -1 \right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e + f x]} \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( (a^2 + b^2) f (\operatorname{Sec}[e + f x]^2)^{1/4} \right)
 \end{aligned}$$

Result (type 6, 280 leaves):

$$\begin{aligned}
 & - \left( \left( 20 d^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{4}, \frac{3}{4}, \frac{5}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] (a + b \operatorname{Tan}[e + f x]) \right) \right) / \left( 3 b f \right. \\
 & \quad (d \operatorname{Sec}[e + f x])^{3/2} \left( 3 (a + i b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{4}, \frac{7}{4}, \frac{7}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] + \right. \\
 & \quad \left. 3 (a - i b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{4}, \frac{3}{4}, \frac{7}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] + \right. \\
 & \quad \left. \left. 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{4}, \frac{3}{4}, \frac{5}{2}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] (a + b \operatorname{Tan}[e + f x]) \right) \right) \Big)
 \end{aligned}$$

**Problem 607: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{d \operatorname{Sec}[e + f x]} (a + b \operatorname{Tan}[e + f x])} dx$$

Optimal (type 4, 451 leaves, 17 steps):

$$\begin{aligned}
 & \frac{b^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{5/4} f \sqrt{d \operatorname{Sec}[e+fx]}} - \frac{b^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{5/4} f \sqrt{d \operatorname{Sec}[e+fx]}} + \\
 & \frac{2 a \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2) f \sqrt{d \operatorname{Sec}[e+fx]}} - \frac{2 a \operatorname{Tan}[e+fx]}{(a^2+b^2) f \sqrt{d \operatorname{Sec}[e+fx]}} - \\
 & \left( a b \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+fx]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( (a^2+b^2)^{3/2} f \sqrt{d \operatorname{Sec}[e+fx]} \right) + \\
 & \left( a b \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] (\operatorname{Sec}[e+fx]^2)^{1/4} \right. \\
 & \quad \left. \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( (a^2+b^2)^{3/2} f \sqrt{d \operatorname{Sec}[e+fx]} \right) + \frac{2 (b+a \operatorname{Tan}[e+fx])}{(a^2+b^2) f \sqrt{d \operatorname{Sec}[e+fx]}}
 \end{aligned}$$

Result (type 4, 34824 leaves): Display of huge result suppressed!

**Problem 608: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e+fx])^{3/2} (a+b \operatorname{Tan}[e+fx])} dx$$

Optimal (type 4, 422 leaves, 17 steps):

$$\begin{aligned}
 & \frac{b^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{3/4}}{(a^2+b^2)^{7/4} f (d \operatorname{Sec}[e+fx])^{3/2}} - \\
 & \frac{b^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{3/4}}{(a^2+b^2)^{7/4} f (d \operatorname{Sec}[e+fx])^{3/2}} + \\
 & \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] (\operatorname{Sec}[e+fx]^2)^{3/4}}{3 (a^2+b^2) f (d \operatorname{Sec}[e+fx])^{3/2}} + \\
 & \left( a b^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+fx]^2)^{3/4} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( (a^2+b^2)^2 f (d \operatorname{Sec}[e+fx])^{3/2} \right) + \\
 & \left( a b^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] (\operatorname{Sec}[e+fx]^2)^{3/4} \right. \\
 & \quad \left. \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( (a^2+b^2)^2 f (d \operatorname{Sec}[e+fx])^{3/2} \right) + \frac{2 (b+a \operatorname{Tan}[e+fx])}{3 (a^2+b^2) f (d \operatorname{Sec}[e+fx])^{3/2}}
 \end{aligned}$$

Result (type 4, 11857 leaves):

$$\left( \text{Sec}[e + f x]^3 (a \text{Cos}[e + f x] + b \text{Sin}[e + f x]) \right. \\ \left. \left( \frac{b}{3(a - i b)(a + i b)} + \frac{b \text{Cos}[2(e + f x)]}{3(a - i b)(a + i b)} + \frac{a \text{Sin}[2(e + f x)]}{3(a - i b)(a + i b)} \right) \right) / \\ \left( f (d \text{Sec}[e + f x])^{3/2} (a + b \text{Tan}[e + f x]) \right) + \left( 2 \text{Sec}[e + f x]^{5/2} (a \text{Cos}[e + f x] + b \text{Sin}[e + f x]) \right. \\ \left. \left( a^2 / \left( 3(a - i b)(a + i b) \sqrt{\text{Sec}[e + f x]} (a \text{Cos}[e + f x] + b \text{Sin}[e + f x]) \right) + \right. \right. \\ \left. \left. b^2 / \left( (a - i b)(a + i b) \sqrt{\text{Sec}[e + f x]} (a \text{Cos}[e + f x] + b \text{Sin}[e + f x]) \right) + \right. \right. \\ \left. \left. \frac{a b \sqrt{\text{Sec}[e + f x]} \text{Sin}[e + f x]}{3(a - i b)(a + i b)(a \text{Cos}[e + f x] + b \text{Sin}[e + f x])} \right) \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2}} \right. \\ \left. \left( a^3 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2} + \right. \right. \\ \left. \left. 3 a b^2 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2} + \right. \right. \\ \left. \left. \left( 3 a b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\text{Tan}\left[\frac{1}{2}(e+f x)\right] )}{i+\text{Tan}\left[\frac{1}{2}(e+f x)\right]}}}{\sqrt{2}}}\right], 2\right] - (1 - i) a \right. \right. \\ \left. \left. \text{EllipticPi}\left[\frac{(1 + i)(a + i(-b + \sqrt{a^2 + b^2}))}{a + b - \sqrt{a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\text{Tan}\left[\frac{1}{2}(e+f x)\right] )}{i+\text{Tan}\left[\frac{1}{2}(e+f x)\right]}}}{\sqrt{2}}}\right], 2\right] \right) \right) \right)$$

$$\left( \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( (-a-b+\sqrt{a^2+b^2}) (-i a-b+\sqrt{a^2+b^2}) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) -$$

$$\left( 3 a b^4 \left( (a+b-\sqrt{a^2+b^2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) a \right. \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \right) \right)$$

$$\left( \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} (-a-b+\sqrt{a^2+b^2}) (-i a-b+\sqrt{a^2+b^2}) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 3 a b^4 \left( (a+b+\sqrt{a^2+b^2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) a \right. \right.$$

$$\left. \text{EllipticPi} \left[ \frac{(1+i)(a-i(b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\text{Tan}[\frac{1}{2}(e+fx)])}{i+\text{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2+2i \text{Tan}[\frac{1}{2}(e+fx)]}{i+\text{Tan}[\frac{1}{2}(e+fx)]}} \left( i+\text{Tan} \left[ \frac{1}{2}(e+fx) \right] \right)^2 \sqrt{\frac{-1+\text{Tan}[\frac{1}{2}(e+fx)]^2}{\left( i+\text{Tan} \left[ \frac{1}{2}(e+fx) \right] \right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} \left( i a+b+\sqrt{a^2+b^2} \right) \left( a+b+\sqrt{a^2+b^2} \right) \sqrt{1+\text{Tan} \left[ \frac{1}{2}(e+fx) \right]^2} \right) +$$

$$\left( 3 a b^3 \left( -i \left( a+b+\sqrt{a^2+b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\text{Tan}[\frac{1}{2}(e+fx)])}{i+\text{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] + (1+i) \right) \right)$$

$$\left. a \text{EllipticPi} \left[ \frac{(1+i)(a-i(b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\text{Tan}[\frac{1}{2}(e+fx)])}{i+\text{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2+2i \text{Tan}[\frac{1}{2}(e+fx)]}{i+\text{Tan}[\frac{1}{2}(e+fx)]}} \left( i+\text{Tan} \left[ \frac{1}{2}(e+fx) \right] \right)^2 \sqrt{\frac{-1+\text{Tan}[\frac{1}{2}(e+fx)]^2}{\left( i+\text{Tan} \left[ \frac{1}{2}(e+fx) \right] \right)^2}} \right) /$$

$$\left( \left( a+b+\sqrt{a^2+b^2} \right) \left( a-i \left( b+\sqrt{a^2+b^2} \right) \right) \sqrt{1+\text{Tan} \left[ \frac{1}{2}(e+fx) \right]^2} \right) /$$

$$\left( 3 a^2 (a - i b) (a + i b) f (d \operatorname{Sec}[e + f x])^{3/2} \right.$$

$$\left( \frac{1}{3 a^2 (a - i b) (a + i b)} \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \left(\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}\right)^{3/2} \right.$$

$$\left( a^3 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} + \right.$$

$$3 a b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} +$$

$$\left( 3 a b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - \right.$$

$$(1 - i) a \operatorname{EllipticPi}\left[\frac{(1 + i) (a + i (-b + \sqrt{a^2 + b^2}))}{a + b - \sqrt{a^2 + b^2}}\right],$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \sqrt{\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} \right)$$

$$\left( \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) / \left( (-a-b + \sqrt{a^2+b^2}) \right.$$

$$\left. (-i a - b + \sqrt{a^2+b^2}) \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} - 3 a b^4 \left( a + b - \sqrt{a^2+b^2} \right) \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \right)$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} (-a-b + \sqrt{a^2+b^2}) (-i a - b + \sqrt{a^2+b^2}) \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 3 a b^4 \left( a + b + \sqrt{a^2+b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) \right)$$



$$\begin{aligned}
 & a \operatorname{EllipticPi} \left[ \frac{(1+i) (a-i (b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}} \right], \right. \\
 & \left. 2 \right] \sqrt{-\frac{2+2i \operatorname{Tan}[\frac{1}{2} (e+fx)]}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]} \left( i+\operatorname{Tan}[\frac{1}{2} (e+fx)] \right)^2} \\
 & \left. \sqrt{\frac{-1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2}{(i+\operatorname{Tan}[\frac{1}{2} (e+fx)])^2}} \right) / \left( \sqrt{a^2+b^2} (i a+b+\sqrt{a^2+b^2}) \right) \\
 & \left( a+b+\sqrt{a^2+b^2} \right) \sqrt{1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2} + \left( 3 a b^3 - i (a+b+\sqrt{a^2+b^2}) \right) \\
 & \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}} \right], 2 \right] + (1+i) a \operatorname{EllipticPi} \left[ \right. \\
 & \left. \frac{(1+i) (a-i (b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}} \right], 2 \right] \\
 & \left. \sqrt{-\frac{2+2i \operatorname{Tan}[\frac{1}{2} (e+fx)]}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]} \left( i+\operatorname{Tan}[\frac{1}{2} (e+fx)] \right)^2} \sqrt{\frac{-1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2}{(i+\operatorname{Tan}[\frac{1}{2} (e+fx)])^2}} \right) /
 \end{aligned}$$

$$\left( \left( a + b + \sqrt{a^2 + b^2} \right) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2} \right) +$$

$$\frac{1}{3 a^2 (a - i b) (a + i b)} 2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(e + fx)\right]^2}}$$

$$\left( - \left( a^3 \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(e + fx)\right]\right], -1\right] \sec\left[\frac{1}{2}(e + fx)\right]^2 \tan\left[\frac{1}{2}(e + fx)\right] \right) / \right.$$

$$\left. \left( 2 \sqrt{1 - \tan\left[\frac{1}{2}(e + fx)\right]^2} \right) \right) - \left( 3 a b^2 \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(e + fx)\right]\right], -1\right] \right.$$

$$\left. \sec\left[\frac{1}{2}(e + fx)\right]^2 \tan\left[\frac{1}{2}(e + fx)\right] \right) / \left( 2 \sqrt{1 - \tan\left[\frac{1}{2}(e + fx)\right]^2} \right) -$$

$$\left( 3 a b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] -$$

$$(1 - i) a \text{EllipticPi}\left[\frac{(1 + i) (a + i (-b + \sqrt{a^2 + b^2}))}{a + b - \sqrt{a^2 + b^2}}\right],$$

$$\left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \sec\left[\frac{1}{2}(e + fx)\right]^2 \tan\left[\frac{1}{2}(e + fx)\right] \right)$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left(2\left(-a-b+\sqrt{a^2+b^2}\right)\left(-i a-b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^{3/2}\right)+$$

$$\left(3 a b^4\left(a+b-\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right)-\right.$$

$$\left.(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}\right],\right.$$

$$\left.\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left(2 \sqrt{a^2+b^2}\left(-a-b+\sqrt{a^2+b^2}\right)\left(-i a-b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2\right)^{3/2}-$$

$$\left(3 a b^4\left(a+b+\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right)-\right.$$

$$\left.(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right],\right.$$

$$\begin{aligned}
 & \left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \sqrt{-\frac{2+2i \tan\left[\frac{1}{2}(e+fx)\right]}{i+\tan\left[\frac{1}{2}(e+fx)\right]}} \left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right. \\
 & \left. \left(2\sqrt{a^2+b^2} \left(i a+b+\sqrt{a^2+b^2}\right) \left(a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{3/2}\right) - \right. \\
 & \left. \left(3 a b^3 \left[-i \left(a+b+\sqrt{a^2+b^2}\right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] + \right. \right. \\
 & \left. \left. (1+i) a \text{EllipticPi}\left[\frac{(1+i) \left(a-i \left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. \sqrt{-\frac{2+2i \tan\left[\frac{1}{2}(e+fx)\right]}{i+\tan\left[\frac{1}{2}(e+fx)\right]}} \left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right. \right. \\
 & \left. \left. \left(2 \left(a+b+\sqrt{a^2+b^2}\right) \left(a-i \left(b+\sqrt{a^2+b^2}\right)\right) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{3/2}\right) + \right. \right. \\
 & \left. \left. \frac{a^3 \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} + \frac{3 a b^2 \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} \right. \right. \\
 & \left. \left. 2\sqrt{1+\tan\left[\frac{1}{2}(e+fx)\right]^2} \right. \right.
 \end{aligned}$$

$$\left( 3 a b^3 \left( (a + b - \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}}} \right], 2 \right] - \right. \right.$$

$$(1 - i) a \operatorname{EllipticPi} \left[ \frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}}} \right], 2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)$$

$$\left. \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right)$$

$$\left( (-a - b + \sqrt{a^2 + b^2}) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) -$$

$$\left( 3 a b^4 \left( (a + b - \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}}} \right], 2 \right] - \right. \right.$$

$$(1 - i) a \operatorname{EllipticPi} \left[ \frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}}} \right], 2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)$$

$$\left( \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} \left(-a-b+\sqrt{a^2+b^2}\right) \left(-ia-b+\sqrt{a^2+b^2}\right) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 3ab^4 \left( a+b+\sqrt{a^2+b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - \right.$$

$$\left. (1-i)a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)$$

$$\left( \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} \left(ia+b+\sqrt{a^2+b^2}\right) \left(a+b+\sqrt{a^2+b^2}\right) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 3ab^3 \left( -i\left(a+b+\sqrt{a^2+b^2}\right) \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] + \right.$$

$$\begin{aligned}
 & (1+i) a \operatorname{EllipticPi} \left[ \frac{(1+i) (a-i (b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \right. \\
 & \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}}, 2 \right] \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \\
 & \left. \sqrt{-\frac{2+2i \operatorname{Tan}[\frac{1}{2} (e+fx)]}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}} (i+\operatorname{Tan}[\frac{1}{2} (e+fx)]) \sqrt{\frac{-1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2}{(i+\operatorname{Tan}[\frac{1}{2} (e+fx)])^2}} \right) \\
 & \left( (a+b+\sqrt{a^2+b^2}) (a-i (b+\sqrt{a^2+b^2})) \sqrt{1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2} + \right. \\
 & \left. 3 a b^3 \left( (a+b-\sqrt{a^2+b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}}, 2 \right] - (1-i) \right. \right. \right. \\
 & \left. \left. \left. a \operatorname{EllipticPi} \left[ \frac{(1+i) (a+i (-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1+\operatorname{Tan}[\frac{1}{2} (e+fx)])}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]}}}{\sqrt{2}} \right], \right. \right. \right. \\
 & \left. \left. \left. 2 \right] \left( i+\operatorname{Tan}[\frac{1}{2} (e+fx)] \right)^2 \sqrt{\frac{-1+\operatorname{Tan}[\frac{1}{2} (e+fx)]^2}{(i+\operatorname{Tan}[\frac{1}{2} (e+fx)])^2}} \right) \right) \\
 & \left. \left( \frac{\operatorname{Sec}[\frac{1}{2} (e+fx)]^2 (2+2i \operatorname{Tan}[\frac{1}{2} (e+fx)])}{2 (i+\operatorname{Tan}[\frac{1}{2} (e+fx)])^2} - \frac{i \operatorname{Sec}[\frac{1}{2} (e+fx)]^2}{i+\operatorname{Tan}[\frac{1}{2} (e+fx)]} \right) \right) /
 \end{aligned}$$

$$\left( 2 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{-\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}} \right.$$

$$\left. \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2} \right) -$$

$$\left( 3 a b^4 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - (1-i)$$

$$a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right]$$

$$\left. \left( i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2}} \right)$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \left(2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}{2 \left(i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2} - \frac{i \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]} \right) \sqrt{$$

$$\left( 2 \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \right.$$

$$\left. \sqrt{-\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}} \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2} \right) +$$



$$\left( 3 a b^4 \left( (a + b + \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1 - i) \right. \right.$$

$$a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], \right.$$

$$\left. \left. 2 \right] \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right.$$

$$\left. \left. \left( \frac{\operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \left( 2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}{2 \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2} - \frac{i \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]} \right) \right) \right)$$

$$\left( 2 \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \right.$$

$$\left. \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}} \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2} \right) +$$

$$\left( 3 a b^3 \left( -i \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] + (1 + i) \right. \right.$$

$$a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], \right.$$

$$\left. \begin{aligned}
 & 2 \left[ \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right. \\
 & \left. \left( \frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 (2 + 2i \tan\left[\frac{1}{2}(e+fx)\right])}{2 \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2} - \frac{i \sec\left[\frac{1}{2}(e+fx)\right]^2}{i + \tan\left[\frac{1}{2}(e+fx)\right]} \right) \right] \\
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e+fx)\right]}{i + \tan\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \left. \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 3 a b^3 \left( \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) \right. \right. \\
 & \left. \left. a \text{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], \right. \right. \\
 & \left. \left. 2 \right) \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e+fx)\right]}{i + \tan\left[\frac{1}{2}(e+fx)\right]}} \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \right)
 \end{aligned} \right)$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \Big/$$

$$\left( 2 \left(-a - b + \sqrt{a^2 + b^2}\right) \left(-i a - b + \sqrt{a^2 + b^2}\right) \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right.$$

$$\left. \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) -$$

$$\left( 3 a b^4 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - (1 - i) \right.$$

$$\left. a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a + i\left(-b + \sqrt{a^2 + b^2}\right)\right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], \right.$$

$$\left. 2\right] \sqrt{-\frac{2 + 2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \Big/$$

$$\left( 2 \sqrt{a^2 + b^2} \left(-a - b + \sqrt{a^2 + b^2}\right) \left(-i a - b + \sqrt{a^2 + b^2}\right) \right)$$

$$\begin{aligned}
 & \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} + \\
 & \left( 3 a b^4 \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) \right. \\
 & a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], \right. \\
 & \left. \left. 2\right] \sqrt{-\frac{2+2i \tan\left[\frac{1}{2}(e+fx)\right]}{i+\tan\left[\frac{1}{2}(e+fx)\right]}} \left(i + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2} \right) \\
 & \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]}{\left(i + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \tan\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \Big/ \\
 & \left( 2 \sqrt{a^2 + b^2} \left(i a + b + \sqrt{a^2 + b^2}\right) \left(a + b + \sqrt{a^2 + b^2}\right) \right. \\
 & \left. \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} + \right. \\
 & \left. \left( 3 a b^3 \left( -i \left(a + b + \sqrt{a^2 + b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] + (1+i) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}} \right], \right. \\
 & \left. 2 \right] \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} \\
 & \left( \frac{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} - \frac{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^3} \right) / \\
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \\
 & \left. \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) + \\
 & \left( 3 a b^3 \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \\
 & \left. \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \right. \\
 & \left. \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \quad \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( 1 - \left( i \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \right) / \\
 & \quad \left. \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \\
 & \left( \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) - \\
 & \left( 3 a b^4 \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \\
 & \quad \left. \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \quad \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) - \\
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right] \right) / \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \Bigg) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1 - \frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
 & \left. \sqrt{1 - \frac{(\frac{1}{2} + \frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \left( 1 - \left( i \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right) \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \Bigg) / \\
 & \left( \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 3 a b^4 \sqrt{-\frac{2 + 2 i \tan[\frac{1}{2}(e+fx)]}{i + \tan[\frac{1}{2}(e+fx)]}} \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \tan[\frac{1}{2}(e+fx)]^2}{\left( i + \tan[\frac{1}{2}(e+fx)] \right)^2}} \right. \\
 & \left. \left( \left( a + b + \sqrt{a^2 + b^2} \right) \left( \frac{(\frac{1}{2} + \frac{i}{2}) \sec[\frac{1}{2}(e+fx)]^2}{i + \tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2} + \frac{i}{2} \right) \sec[\frac{1}{2}(e+fx)]^2 \right) \right) \right) / \\
 & \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right] \right) / \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \Bigg) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1 - \frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
 & \left. \sqrt{1 - \frac{(\frac{1}{2} + \frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right) - \\
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{(\frac{1}{2} + \frac{i}{2}) \sec[\frac{1}{2}(e+fx)]^2}{i + \tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2} + \frac{i}{2} \right) \sec[\frac{1}{2}(e+fx)]^2 \right) \right) / \\
 & \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right] \right) / \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
& \left. \sqrt{1-\frac{(\frac{1}{2}+\frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \left(1-i(a-i(b+\sqrt{a^2+b^2}))\left(1+\tan[\frac{1}{2}(e+fx)]\right)\right)\right) \Big/ \left( \left( (a+b+\sqrt{a^2+b^2})(i+\tan[\frac{1}{2}(e+fx)]) \right) \right) \Big) \Big) \\
& \left( \sqrt{a^2+b^2}(ia+b+\sqrt{a^2+b^2})(a+b+\sqrt{a^2+b^2}) \sqrt{1+\tan[\frac{1}{2}(e+fx)]^2} + \right. \\
& \left. 3ab^3 \sqrt{-\frac{2+2i\tan[\frac{1}{2}(e+fx)]}{i+\tan[\frac{1}{2}(e+fx)]}} (i+\tan[\frac{1}{2}(e+fx)])^2 \sqrt{\frac{-1+\tan[\frac{1}{2}(e+fx)]^2}{(i+\tan[\frac{1}{2}(e+fx)])^2}} \right. \\
& \left. - \left( \left( i(a+b+\sqrt{a^2+b^2}) \left( \frac{(\frac{1}{2}+\frac{i}{2})\operatorname{Sec}[\frac{1}{2}(e+fx)]^2}{i+\tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2}+\frac{i}{2} \right) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2 \right. \right. \right. \right. \\
& \left. \left. \left( 1+\tan[\frac{1}{2}(e+fx)] \right) \right) \right) \Big/ (i+\tan[\frac{1}{2}(e+fx)]^2) \Big) \Big) \Big/ \\
& \left( 2\sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
& \left. \sqrt{1-\frac{(\frac{1}{2}+\frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right) \Big) + \\
& \left( \left( \frac{1}{2}+\frac{i}{2} \right) a \left( \frac{(\frac{1}{2}+\frac{i}{2})\operatorname{Sec}[\frac{1}{2}(e+fx)]^2}{i+\tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2}+\frac{i}{2} \right) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2 \right. \right. \\
& \left. \left. \left( 1+\tan[\frac{1}{2}(e+fx)] \right) \right) \right) \Big/ \left( i+\tan[\frac{1}{2}(e+fx)]^2 \right) \Big) \Big/ \\
& \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right.
\end{aligned}$$



$$\sqrt{1 - \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)}{i + \tan\left[\frac{1}{2}(e + f x)\right]}} \left(1 - \left(i \left(a - i \left(b + \sqrt{a^2 + b^2}\right)\right) \left(1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)\right) \right) / \left( \left( \left(a + b + \sqrt{a^2 + b^2}\right) \left(i + \tan\left[\frac{1}{2}(e + f x)\right]\right) \right) \right) / \left( \left(a + b + \sqrt{a^2 + b^2}\right) \right) \left( a - i \left(b + \sqrt{a^2 + b^2}\right) \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) \left( a + b \tan[e + f x] \right)$$

**Problem 609: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e + f x])^{5/2} (a + b \operatorname{Tan}[e + f x])} dx$$

Optimal (type 4, 568 leaves, 18 steps):

$$\frac{b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x])^{3/4}}{(a^2 + b^2)^{1/4}}\right] (\operatorname{Sec}[e + f x])^{1/4} - b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x])^{3/4}}{(a^2 + b^2)^{1/4}}\right] (\operatorname{Sec}[e + f x])^{1/4}}{(a^2 + b^2)^{9/4} d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} + \frac{\left(2 a (3 a^2 + 8 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e + f x]], 2\right] (\operatorname{Sec}[e + f x])^{1/4}\right) / \left(5 (a^2 + b^2)^2 d^2 f \sqrt{d \operatorname{Sec}[e + f x]}\right) - \frac{2 a (3 a^2 + 8 b^2) \operatorname{Tan}[e + f x]}{5 (a^2 + b^2)^2 d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} - \left(a b^3 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e + f x])^{1/4}\right], -1\right] (\operatorname{Sec}[e + f x])^{1/4} \sqrt{-\operatorname{Tan}[e + f x]^2}\right) / \left((a^2 + b^2)^{5/2} d^2 f \sqrt{d \operatorname{Sec}[e + f x]}\right) + \left(a b^3 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e + f x])^{1/4}\right], -1\right] (\operatorname{Sec}[e + f x])^{1/4} \sqrt{-\operatorname{Tan}[e + f x]^2}\right) / \left((a^2 + b^2)^{5/2} d^2 f \sqrt{d \operatorname{Sec}[e + f x]}\right) + \frac{2 \operatorname{Cos}[e + f x]^2 (b + a \operatorname{Tan}[e + f x])}{5 (a^2 + b^2) d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} + \frac{2 (5 b^3 + a (3 a^2 + 8 b^2) \operatorname{Tan}[e + f x])}{5 (a^2 + b^2)^2 d^2 f \sqrt{d \operatorname{Sec}[e + f x]}}$$

Result (type 4, 33345 leaves): Display of huge result suppressed!

**Problem 610: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e + f x])^{7/2}}{(a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 4, 480 leaves, 17 steps):

$$\begin{aligned} & \frac{3 a d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x]^2)^{1/4}}{(a^2 + b^2)^{1/4}}\right] (d \operatorname{Sec}[e + f x])^{3/2}}{2 b^{5/2} (a^2 + b^2)^{1/4} f (\operatorname{Sec}[e + f x]^2)^{3/4}} + \\ & \frac{3 a d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x]^2)^{1/4}}{(a^2 + b^2)^{1/4}}\right] (d \operatorname{Sec}[e + f x])^{3/2}}{2 b^{5/2} (a^2 + b^2)^{1/4} f (\operatorname{Sec}[e + f x]^2)^{3/4}} - \\ & \frac{3 d^2 \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e + f x]], 2\right] (d \operatorname{Sec}[e + f x])^{3/2}}{b^2 f (\operatorname{Sec}[e + f x]^2)^{3/4}} + \\ & \frac{3 d^2 \operatorname{Cos}[e + f x] (d \operatorname{Sec}[e + f x])^{3/2} \operatorname{Sin}[e + f x]}{b^2 f} + \\ & \left( 3 a^2 d^2 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e + f x]^2)^{1/4}\right], -1\right] \right. \\ & \quad \left. (d \operatorname{Sec}[e + f x])^{3/2} \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( 2 b^3 \sqrt{a^2 + b^2} f (\operatorname{Sec}[e + f x]^2)^{3/4} \right) - \\ & \left( 3 a^2 d^2 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e + f x]^2)^{1/4}\right], -1\right] (d \operatorname{Sec}[e + f x])^{3/2} \right. \\ & \quad \left. \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( 2 b^3 \sqrt{a^2 + b^2} f (\operatorname{Sec}[e + f x]^2)^{3/4} \right) - \frac{d^2 (d \operatorname{Sec}[e + f x])^{3/2}}{b f (a + b \operatorname{Tan}[e + f x])} \end{aligned}$$

Result (type 4, 31777 leaves): Display of huge result suppressed!

**Problem 611: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e + f x])^{5/2}}{(a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 4, 440 leaves, 17 steps):

$$\begin{aligned}
 & \frac{a d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx])^{3/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+fx]}}{2 b^{3/2} (a^2+b^2)^{3/4} f (\operatorname{Sec}[e+fx])^{1/4}} + \frac{a d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx])^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+fx]}}{2 b^{3/2} (a^2+b^2)^{3/4} f (\operatorname{Sec}[e+fx])^{1/4}} + \\
 & \frac{d^2 \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] \sqrt{d \operatorname{Sec}[e+fx]}}{b^2 f (\operatorname{Sec}[e+fx])^{1/4}} - \\
 & \left( a^2 d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx])^{1/4}], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+fx]} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 2 b^2 (a^2+b^2) f (\operatorname{Sec}[e+fx])^{1/4} \right) - \\
 & \left( a^2 d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx])^{1/4}], -1\right] \sqrt{d \operatorname{Sec}[e+fx]} \right. \\
 & \quad \left. \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 2 b^2 (a^2+b^2) f (\operatorname{Sec}[e+fx])^{1/4} \right) - \frac{d^2 \sqrt{d \operatorname{Sec}[e+fx]}}{b f (a+b \operatorname{Tan}[e+fx])}
 \end{aligned}$$

Result (type 4, 3091 leaves):

$$\begin{aligned}
 & \left( (d \operatorname{Sec}[e+fx])^{5/2} (a \operatorname{Cos}[e+fx] + b \operatorname{Sin}[e+fx])^2 \left( -\frac{1}{ab} + \frac{\operatorname{Sin}[e+fx]}{a(a \operatorname{Cos}[e+fx] + b \operatorname{Sin}[e+fx])} \right) \right) / \\
 & \left( f (a+b \operatorname{Tan}[e+fx])^2 \right) - \\
 & \left( \left( -2 i b \sqrt{a^2+b^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-i \operatorname{Cos}[e+fx] + \operatorname{Sin}[e+fx]}}{\sqrt{2}}\right], 2\right] + \right. \right. \\
 & \quad a \left( a - i b + \sqrt{a^2+b^2} \right) \operatorname{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}\right], \\
 & \quad \operatorname{ArcSin}\left[\frac{\sqrt{1-i \operatorname{Cos}[e+fx] + \operatorname{Sin}[e+fx]}}{\sqrt{2}}\right], 2 \right) + a \left( -a+i b + \sqrt{a^2+b^2} \right) \operatorname{EllipticPi}\left[ \right. \\
 & \quad \left. \frac{(1+i)(a-i(b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{1-i \operatorname{Cos}[e+fx] + \operatorname{Sin}[e+fx]}}{\sqrt{2}}\right], 2 \right) \left. \right) \\
 & (d \operatorname{Sec}[e+fx])^{5/2} \sqrt{\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \sqrt{i \operatorname{Cos}[e+fx] - \operatorname{Sin}[e+fx]}} \\
 & \sqrt{\operatorname{Cos}[e+fx] (\operatorname{Cos}[e+fx] + i \operatorname{Sin}[e+fx])} \operatorname{Sin}[e+fx] \\
 & (a \operatorname{Cos}[e+fx] + b \operatorname{Sin}[e+fx]) \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \Bigg) / \\
 & \left( 4 (a-i b) b^3 \sqrt{a^2+b^2} f \sqrt{\frac{1}{1+\operatorname{Cos}[e+fx]}} (a+b \operatorname{Tan}[e+fx])^2 \right)
 \end{aligned}$$

$$\left( -\frac{1}{2(a-ib)b^2\sqrt{a^2+b^2}}\sqrt{\frac{1}{1+\cos[e+fx]}} \right.$$

$$\left. \left( -2ib\sqrt{a^2+b^2}\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] + \right. \right.$$

$$\left. a\left(a-ib+\sqrt{a^2+b^2}\right)\operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] + a\left(-a+ib+\sqrt{a^2+b^2}\right)\operatorname{EllipticPi}\left[ \right.$$

$$\left. \frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] \left. \right)$$

$$\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\sqrt{\cos\left[\frac{1}{2}(e+fx)\right]^2\operatorname{Sec}[e+fx]\sqrt{ib\cos[e+fx]-\sin[e+fx]}}$$

$$\sqrt{\cos[e+fx]\left(\cos[e+fx]+ib\sin[e+fx]\right)}\left(ib+\tan\left[\frac{1}{2}(e+fx)\right]\right) -$$

$$\left( 1/\left( 4(a-ib)b^2\sqrt{a^2+b^2}\sqrt{\frac{1}{1+\cos[e+fx]}}\sqrt{ib\cos[e+fx]-\sin[e+fx]} \right) \right)$$

$$\left( -2ib\sqrt{a^2+b^2}\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] + \right.$$

$$\left. a\left(a-ib+\sqrt{a^2+b^2}\right)\operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] + a\left(-a+ib+\sqrt{a^2+b^2}\right)\operatorname{EllipticPi}\left[ \right.$$

$$\left. \frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{1-ib\cos[e+fx]+\sin[e+fx]}}{\sqrt{2}}\right], 2\right] \left. \right)$$

$$\sqrt{\cos\left[\frac{1}{2}(e+fx)\right]^2\operatorname{Sec}[e+fx]\left(-\cos[e+fx]-ib\sin[e+fx]\right)}$$

$$\sqrt{\cos[e+fx]\left(\cos[e+fx]+ib\sin[e+fx]\right)}\left(ib+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2 +$$

$$\frac{1}{4(a-ib)b^2\sqrt{a^2+b^2}}\sqrt{\frac{1}{1+\cos[e+fx]}}$$

$$\begin{aligned}
 & \left( -2 i b \sqrt{a^2 + b^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}}\right], 2\right] + \right. \\
 & a \left( a - i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[\frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right. \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] + a \left( -a + i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[ \right. \\
 & \left. \frac{(1 + i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] \left. \right) \\
 & \sqrt{\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x] \sqrt{i \cos[e + f x] - \sin[e + f x]}} \\
 & \sqrt{\cos[e + f x] (\cos[e + f x] + i \sin[e + f x]) \sin[e + f x] \left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2} - \\
 & \left( \left( -2 i b \sqrt{a^2 + b^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}}\right], 2\right] + \right. \right. \\
 & a \left( a - i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[\frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right. \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] + a \left( -a + i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[ \right. \\
 & \left. \frac{(1 + i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] \left. \right) \\
 & \sqrt{\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x] \sqrt{i \cos[e + f x] - \sin[e + f x]}} \\
 & \left( \cos[e + f x] (i \cos[e + f x] - \sin[e + f x]) - (\cos[e + f x] + i \sin[e + f x]) \sin[e + f x] \right) \\
 & \left. \left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 \right) / \\
 & \left( 4 (a - i b) b^2 \sqrt{a^2 + b^2} \sqrt{\frac{1}{1 + \cos[e + f x]}} \sqrt{\cos[e + f x] (\cos[e + f x] + i \sin[e + f x])} \right) - \\
 & \frac{1}{2 (a - i b) b^2 \sqrt{a^2 + b^2} \sqrt{\frac{1}{1 + \cos[e + f x]}}} \sqrt{\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x]} \\
 & \sqrt{i \cos[e + f x] - \sin[e + f x]} \sqrt{\cos[e + f x] (\cos[e + f x] + i \sin[e + f x])}
 \end{aligned}$$

$$\begin{aligned}
 & \left( - \left( \left( i b \sqrt{a^2 + b^2} (\cos[e + f x] + i \sin[e + f x]) \right) / \right. \right. \\
 & \left. \left( \sqrt{2} \sqrt{1 + \frac{1}{2} (-1 + i \cos[e + f x] - \sin[e + f x])} \sqrt{i \cos[e + f x] - \sin[e + f x]} \right. \right. \\
 & \left. \left. \sqrt{1 - i \cos[e + f x] + \sin[e + f x]} \right) \right) + \left( a \left( a - i b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. (\cos[e + f x] + i \sin[e + f x]) \right) / \left( 2 \sqrt{2} \sqrt{1 + \frac{1}{2} (-1 + i \cos[e + f x] - \sin[e + f x])} \right. \\
 & \left. \sqrt{i \cos[e + f x] - \sin[e + f x]} \sqrt{1 - i \cos[e + f x] + \sin[e + f x]} \right. \\
 & \left. \left( 1 - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right) \left( 1 - i \cos[e + f x] + \sin[e + f x] \right) \right) \right) / \right. \\
 & \left. \left( a + b - \sqrt{a^2 + b^2} \right) \right) + \left( a \left( -a + i b + \sqrt{a^2 + b^2} \right) (\cos[e + f x] + i \sin[e + f x]) \right) / \\
 & \left( 2 \sqrt{2} \sqrt{1 + \frac{1}{2} (-1 + i \cos[e + f x] - \sin[e + f x])} \sqrt{i \cos[e + f x] - \sin[e + f x]} \right. \\
 & \left. \sqrt{1 - i \cos[e + f x] + \sin[e + f x]} \left( 1 - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) \left( 1 - i \cos[e + f x] + \sin[e + f x] \right) \right) \right) / \right. \\
 & \left. \left( a + b + \sqrt{a^2 + b^2} \right) \right) \right) \left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 - \\
 & \left( \left( -2 i b \sqrt{a^2 + b^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] + \right. \right. \\
 & a \left( a - i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[\frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right. \\
 & \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] + a \left( -a + i b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticPi}\left[\frac{(1 + i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{1 - i \cos[e + f x] + \sin[e + f x]}}{\sqrt{2}}\right], 2\right] \right) \\
 & \sqrt{i \cos[e + f x] - \sin[e + f x]} \sqrt{\cos[e + f x] (\cos[e + f x] + i \sin[e + f x])} \\
 & \left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 \left( -\cos\left[\frac{1}{2}(e + f x)\right] \operatorname{Sec}[e + f x] \sin\left[\frac{1}{2}(e + f x)\right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & - \frac{3 a \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x])^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{2 (a^2+b^2)^{7/4} f (\operatorname{Sec}[e+f x])^{1/4}} - \\
 & \frac{3 a \sqrt{b} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x])^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{2 (a^2+b^2)^{7/4} f (\operatorname{Sec}[e+f x])^{1/4}} - \\
 & \frac{\operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] \sqrt{d \operatorname{Sec}[e+f x]}}{(a^2+b^2) f (\operatorname{Sec}[e+f x])^{1/4}} + \\
 & \left(3 a^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x])^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+f x]} \sqrt{-\operatorname{Tan}[e+f x]^2}\right) / \left(2 (a^2+b^2)^2 f (\operatorname{Sec}[e+f x])^{1/4}\right) + \\
 & \left(3 a^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x])^{1/4}\right], -1\right] \sqrt{d \operatorname{Sec}[e+f x]} \right. \\
 & \quad \left. \sqrt{-\operatorname{Tan}[e+f x]^2}\right) / \left(2 (a^2+b^2)^2 f (\operatorname{Sec}[e+f x])^{1/4}\right) - \frac{b \sqrt{d \operatorname{Sec}[e+f x]}}{(a^2+b^2) f (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 11501 leaves):

$$\begin{aligned}
 & \left(\operatorname{Sec}[e+f x]^2 \sqrt{d \operatorname{Sec}[e+f x]} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])^2 \right. \\
 & \quad \left. \left(-\frac{b}{a(a-i b)(a+i b)} + \frac{b^2 \operatorname{Sin}[e+f x]}{a(a-i b)(a+i b)(a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])}\right)\right) / \\
 & \left(f (a+b \operatorname{Tan}[e+f x])^2\right) + \left(\operatorname{Sec}[e+f x]^{3/2} \sqrt{d \operatorname{Sec}[e+f x]} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])^2 \right. \\
 & \quad \left. \left(a / \left((a-i b)(a+i b) \sqrt{\operatorname{Sec}[e+f x]} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])\right) - \right. \right. \\
 & \quad \left. \left. \frac{b \sqrt{\operatorname{Sec}[e+f x]} \operatorname{Sin}[e+f x]}{2(a-i b)(a+i b)(a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])}\right) \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} \right. \\
 & \quad \left. \left(2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]\right], -1\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} + \right. \right.
 \end{aligned}$$



$$\left( 3 b \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1-i) a \right.$$

$$\left. \text{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}} \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right) /$$

$$\left( \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} \right) -$$

$$\left( 3 b^2 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1-i) a \right.$$

$$\left. \text{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}} \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right) /$$

$$\begin{aligned}
 & \left( \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) + \\
 & \left( 3 b \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{i+\tan\left[\frac{1}{2}(e+f x)\right]}\right], 2\right] - (1-i) a \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{i+\tan\left[\frac{1}{2}(e+f x)\right]}\right], 2\right] \right) \right. \right. \\
 & \left. \left. \sqrt{-\frac{2+2 i \tan\left[\frac{1}{2}(e+f x)\right]}{i+\tan\left[\frac{1}{2}(e+f x)\right]}\left(i+\tan\left[\frac{1}{2}(e+f x)\right]\right)^2 \sqrt{\frac{-1+\tan\left[\frac{1}{2}(e+f x)\right]^2}{\left(i+\tan\left[\frac{1}{2}(e+f x)\right]\right)^2}} \right) \right. \right. \\
 & \left. \left( \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) + \right. \\
 & \left. \left( 3 b^2 \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{i+\tan\left[\frac{1}{2}(e+f x)\right]}\right], 2\right] - (1-i) a \right. \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{i+\tan\left[\frac{1}{2}(e+f x)\right]}\right], 2\right] \right) \right. \right. \right.
 \end{aligned}$$

$$\left( \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( \sqrt{a^2+b^2} \left(i a+b+\sqrt{a^2+b^2}\right) \left(a+b+\sqrt{a^2+b^2}\right) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) /$$

$$\left( (a-i b) (a+i b) f \left( \frac{1}{2(a-i b)(a+i b)} \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right)$$

$$\left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^{3/2} \left( 2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right], -1\right] \right)$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} + 3 b \left( a+b-\sqrt{a^2+b^2} \right)$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right]$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left( (-a-b+\sqrt{a^2+b^2}) (-i a-b+\sqrt{a^2+b^2}) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) -$$

$$\left( 3 b^2 \left( a+b-\sqrt{a^2+b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - \right.$$

$$\left. (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}\right], \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right)$$

$$\left. \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left( \sqrt{a^2+b^2} (-a-b+\sqrt{a^2+b^2}) (-i a-b+\sqrt{a^2+b^2}) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 3 b \left( a+b+\sqrt{a^2+b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - \right.$$

$$\begin{aligned}
 & (1 - i) a \operatorname{EllipticPi} \left[ \frac{(1 + i) (a - i (b + \sqrt{a^2 + b^2}))}{a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1 + \operatorname{Tan}[\frac{1}{2} (e + f x)])}{i + \operatorname{Tan}[\frac{1}{2} (e + f x)]}}}{\sqrt{2}}, 2 \right], \sqrt{-\frac{2 + 2 i \operatorname{Tan}[\frac{1}{2} (e + f x)]}{i + \operatorname{Tan}[\frac{1}{2} (e + f x)]}} \right. \\
 & \left. \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}[\frac{1}{2} (e + f x)]^2}{(i + \operatorname{Tan}[\frac{1}{2} (e + f x)])^2}} \right) / \left( (i a + b + \sqrt{a^2 + b^2}) \right. \\
 & \left. (a + b + \sqrt{a^2 + b^2}) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) + \left( 3 b^2 (a + b + \sqrt{a^2 + b^2}) \right. \\
 & \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1 + \operatorname{Tan}[\frac{1}{2} (e + f x)])}{i + \operatorname{Tan}[\frac{1}{2} (e + f x)]}}}{\sqrt{2}}, 2 \right] - (1 - i) a \operatorname{EllipticPi} \left[ \right. \right. \\
 & \left. \left. \frac{(1 + i) (a - i (b + \sqrt{a^2 + b^2}))}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) (1 + \operatorname{Tan}[\frac{1}{2} (e + f x)])}{i + \operatorname{Tan}[\frac{1}{2} (e + f x)]}}}{\sqrt{2}}, 2 \right] \right] \right) \\
 & \left. \sqrt{-\frac{2 + 2 i \operatorname{Tan}[\frac{1}{2} (e + f x)]}{i + \operatorname{Tan}[\frac{1}{2} (e + f x)]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}[\frac{1}{2} (e + f x)]^2}{(i + \operatorname{Tan}[\frac{1}{2} (e + f x)])^2}} \right) / \right.
 \end{aligned}$$

$$\left( \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) +$$

$$\frac{1}{(a - i b)(a + i b)} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(e + f x)\right]^2}} \left( \left( \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(e + f x)\right]\right], 2\right] - \right. \right.$$

$$\left. \left. -1\right) \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right) / \left( \sqrt{1 - \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) -$$

$$\left( 3 b \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - \right.$$

$$\left. (1 - i) a \text{EllipticPi}\left[\frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}\right], \right.$$

$$\left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right)$$

$$\left( \sqrt{-\frac{2 + 2 i \tan\left[\frac{1}{2}(e + f x)\right]}{i + \tan\left[\frac{1}{2}(e + f x)\right]}} \left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2}} \right) /$$

$$\left( 2 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan\left[\frac{1}{2}(e + f x)\right] \right)^{3/2} \right) +$$

$$\left( 3 b^2 \left( (a + b - \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - \right. \right.$$

$$(1 - i) a \operatorname{EllipticPi} \left[ \frac{(1 + i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)$$

$$\left. \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right)$$

$$\left( 2 \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right)^{3/2} -$$

$$\left( 3 b \left( (a + b + \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - \right. \right.$$

$$(1 - i) a \operatorname{EllipticPi} \left[ \frac{(1 + i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left(2\left(i a+b+\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^{3/2}\right)-$$

$$\left(3 b^2\left(a+b+\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right)-\right.$$

$$\left.(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right],\right.$$

$$\left.\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left(2 \sqrt{a^2+b^2}\left(i a+b+\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^{3/2}\right)+$$

$$\frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{\sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}}+$$

$$\left(3 b\left(a+b-\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right)-$$



$$\begin{aligned}
 & (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}\right], \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}[\frac{1}{2}(e+fx)])}{i+\operatorname{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}}\right], 2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}\right. \\
 & \left. \left(\left(-a-b+\sqrt{a^2+b^2}\right)\left(-i a-b+\sqrt{a^2+b^2}\right) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)-\right. \\
 & \left. \left(3 b^2\left(a+b-\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}[\frac{1}{2}(e+fx)])}{i+\operatorname{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}}\right], 2\right]-\right. \right. \\
 & \left. \left. (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}\right], \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}[\frac{1}{2}(e+fx)])}{i+\operatorname{Tan}[\frac{1}{2}(e+fx)]}}}{\sqrt{2}}\right], 2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \left. \left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}\right. \right. \\
 & \left. \left. \right. \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) + \\
 & \left( 3 b \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{2}\right], 2\right] - \right. \right. \\
 & \quad \left. \left. (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{2}\right], 2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \right. \right. \\
 & \quad \left. \left. \sqrt{-\frac{2+2 i \tan\left[\frac{1}{2}(e+f x)\right]}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\left(i+\tan\left[\frac{1}{2}(e+f x)\right]\right)^2}} \sqrt{\frac{-1+\tan\left[\frac{1}{2}(e+f x)\right]^2}{\left(i+\tan\left[\frac{1}{2}(e+f x)\right]\right)^2}} \right) \right) / \\
 & \left( \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) + \\
 & \left( 3 b^2 \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+f x)\right)}{i+\tan\left[\frac{1}{2}(e+f x)\right]}}{\sqrt{2}}}}{2}\right], 2\right] - \right. \right. \\
 & \quad \left. \left. (1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], \right. \right.
 \end{aligned}$$

$$\left. \begin{aligned} & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], 2 \right] \text{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \\ & \left. \sqrt{-\frac{2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]} \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right) \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right) \right. \\ & \left( \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} \right) + \\ & \left( 3 b \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], 2 \right] - (1 - i) \right. \\ & \left. a \text{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], \right. \right. \\ & \left. \left. 2 \right] \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right) \right. \\ & \left. \left( \frac{\text{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \left( 2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right] \right)}{2 \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2} - \frac{i \text{Sec} \left[ \frac{1}{2} (e+fx) \right]^2}{i + \tan \left[ \frac{1}{2} (e+fx) \right]} \right) \right) \sqrt{\quad} \end{aligned} \right) \sqrt{\quad}$$

$$\left( 2 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{-\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}} \right.$$

$$\left. \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2} \right) -$$

$$\left( 3 b^2 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i) \left(1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right)}}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}}}{\sqrt{2}}}\right], 2\right] - (1 - i)$$

$$a \operatorname{EllipticPi}\left[\frac{(1+i) \left(a + i \left(-b + \sqrt{a^2 + b^2}\right)\right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i) \left(1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right)}}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}}}{\sqrt{2}}}\right],$$

$$2 \right] \left( i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2}}$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \left(2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}{2 \left(i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2} - \frac{i \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]} \right) \sqrt{$$

$$2 \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right)$$

$$\sqrt{-\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}} \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2} +$$

$$\left( 3 b \left( a + b + \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], 2 \right] - (1-i) \right.$$

$$a \text{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], \right.$$

$$\left. \left. 2 \right] \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right.$$

$$\left. \left. \left( \frac{\sec \left[ \frac{1}{2} (e+fx) \right]^2 \left( 2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right] \right)}{2 \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2} - \frac{i \sec \left[ \frac{1}{2} (e+fx) \right]^2}{i + \tan \left[ \frac{1}{2} (e+fx) \right]} \right) \right. \right.$$

$$\left. \left. \left( 2 \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{-\frac{2 + 2 i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}} \right. \right.$$

$$\left. \left. \sqrt{1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} \right) + \right.$$

$$\left( 3 b^2 \left( a + b + \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], 2 \right] - (1-i) \right.$$

$$a \text{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], \right.$$

$$\left. \begin{aligned}
 & 2 \left[ \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right. \\
 & \left. \left( \frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 (2 + 2i \tan\left[\frac{1}{2}(e+fx)\right])}{2 \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2} - \frac{i \sec\left[\frac{1}{2}(e+fx)\right]^2}{i + \tan\left[\frac{1}{2}(e+fx)\right]} \right) \right] \\
 & \left( 2 \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e+fx)\right]}{i + \tan\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 3 b \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i + \tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1 - i) \right. \\
 & \left. a \text{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i + \tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], \right. \\
 & \left. 2 \right] \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e+fx)\right]}{i + \tan\left[\frac{1}{2}(e+fx)\right]}} \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2
 \end{aligned} \right)$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \Big/$$

$$\left( 2 \left(-a - b + \sqrt{a^2 + b^2}\right) \left(-i a - b + \sqrt{a^2 + b^2}\right) \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right.$$

$$\left. \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) -$$

$$\left( 3 b^2 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - (1 - i) \right.$$

$$\left. a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a + i\left(-b + \sqrt{a^2 + b^2}\right)\right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], \right.$$

$$\left. 2\right] \sqrt{-\frac{2 + 2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \right) \Big/$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \Big/$$

$$\left( 2 \sqrt{a^2 + b^2} \left(-a - b + \sqrt{a^2 + b^2}\right) \left(-i a - b + \sqrt{a^2 + b^2}\right) \right)$$

$$\begin{aligned}
 & \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right)^2}} \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} + \\
 & \left( 3 b \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}}\right], 2\right] - (1 - i) \right. \\
 & \quad a \operatorname{EllipticPi}\left[\frac{(1 + i)\left(a - i\left(b + \sqrt{a^2 + b^2}\right)\right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}\right], \right. \\
 & \quad \left. \left. 2\right] \sqrt{-\frac{2 + 2 i \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}} \left(i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right)^2 \right. \\
 & \quad \left. \left. \left. \left. \left. \frac{\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right)^3} \right] \right) \right) \right) / \\
 & \left( 2 \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right)^2}} \right. \\
 & \quad \left. \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} \right) + \\
 & \left( 3 b^2 \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}}\right], 2\right] - (1 - i) \right)
 \end{aligned}$$



$$\begin{aligned}
 & a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}}{\sqrt{2}} \right], \right. \\
 & \left. 2 \right] \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} \\
 & \left( \frac{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} - \frac{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^3} \right) / \\
 & \left( 2 \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) + \\
 & \left( 3 b \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2} \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \\
 & \left. \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \right. \\
 & \left. \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \Bigg) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \right. \\
 & \quad \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( 1 - \left( i \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \right. \right. \\
 & \quad \left. \left. \left( a + b - \sqrt{a^2 + b^2} \right) \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \Bigg) / \\
 & \left( \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) - \\
 & \left( 3 b^2 \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \right. \\
 & \quad \left. \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right. \right. \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \right) / \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \Bigg) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \right. \\
 & \quad \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) - \\
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \Big/ \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \Big) \Big/ \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( 1 - \left( i \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \right) \Big/ \\
 & \left( \left( a + b - \sqrt{a^2 + b^2} \right) \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \Big) \Big) \Big/ \\
 & \left( \sqrt{a^2 + b^2} \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) + \\
 & \left( 3 b \sqrt{-\frac{2 + 2 i \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2}} \right. \\
 & \left. \left( \left( a + b + \sqrt{a^2 + b^2} \right) \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \right) \Big/ \\
 & \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \Big/ \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \Big) \Big/ \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) - \\
 & \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \Big/ \\
 & \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \Big/ \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \Big) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
 & \left. \sqrt{1-\frac{(\frac{1}{2}+\frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \left(1-i(a-i(b+\sqrt{a^2+b^2}))\left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right)\right) \right) / \left( (a+b+\sqrt{a^2+b^2})(i+\tan[\frac{1}{2}(e+fx)]) \right) \right) / \\
 & \left( (i a+b+\sqrt{a^2+b^2})(a+b+\sqrt{a^2+b^2}) \sqrt{1+\tan[\frac{1}{2}(e+fx)]^2} + \right. \\
 & \left. 3b^2 \sqrt{-\frac{2+2i \tan[\frac{1}{2}(e+fx)]}{i+\tan[\frac{1}{2}(e+fx)]}} (i+\tan[\frac{1}{2}(e+fx)])^2 \sqrt{\frac{-1+\tan[\frac{1}{2}(e+fx)]^2}{(i+\tan[\frac{1}{2}(e+fx)])^2}} \right. \\
 & \left. \left( (a+b+\sqrt{a^2+b^2}) \left( \frac{(\frac{1}{2}+\frac{i}{2}) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2}{i+\tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2}+\frac{i}{2} \right) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2 \right. \right. \right. \\
 & \left. \left. \left. (1+\tan[\frac{1}{2}(e+fx)]) \right) \right) / (i+\tan[\frac{1}{2}(e+fx)]^2) \right) / \\
 & \left( 2\sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right. \\
 & \left. \sqrt{1-\frac{(\frac{1}{2}+\frac{i}{2})(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right) - \\
 & \left( \left( \frac{1}{2}-\frac{i}{2} \right) a \left( \frac{(\frac{1}{2}+\frac{i}{2}) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2}{i+\tan[\frac{1}{2}(e+fx)]} - \left( \frac{1}{2}+\frac{i}{2} \right) \operatorname{Sec}[\frac{1}{2}(e+fx)]^2 \right. \right. \\
 & \left. \left. (1+\tan[\frac{1}{2}(e+fx)]) \right) \right) / (i+\tan[\frac{1}{2}(e+fx)]^2) \right) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \sqrt{1-\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}} \right.
 \end{aligned}$$

$$\sqrt{\frac{\left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)}{i + \tan\left[\frac{1}{2}(e + f x)\right]}} \left(1 - \left(i \left(a - i \left(b + \sqrt{a^2 + b^2}\right)\right) \left(1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)\right) / \left(\left(a + b + \sqrt{a^2 + b^2}\right) \left(i + \tan\left[\frac{1}{2}(e + f x)\right]\right)\right)\right) / \left(\sqrt{a^2 + b^2} \left(i a + b + \sqrt{a^2 + b^2}\right)\right) \left(a + b + \sqrt{a^2 + b^2}\right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \left(a + b \tan[e + f x]\right)^2$$

**Problem 614: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{d \operatorname{Sec}[e + f x]} (a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 4, 555 leaves, 18 steps):

$$\begin{aligned}
 & \frac{5 a b^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{1/4}}{2 (a^2+b^2)^{9/4} f \sqrt{d \operatorname{Sec}[e+f x]}} - \\
 & \frac{5 a b^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{1/4}}{2 (a^2+b^2)^{9/4} f \sqrt{d \operatorname{Sec}[e+f x]}} + \\
 & \left( (2 a^2 - 3 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (\operatorname{Sec}[e+f x]^2)^{1/4} \right) / \\
 & \left( (a^2+b^2)^2 f \sqrt{d \operatorname{Sec}[e+f x]} \right) - \frac{(2 a^2 - 3 b^2) \operatorname{Tan}[e+f x]}{(a^2+b^2)^2 f \sqrt{d \operatorname{Sec}[e+f x]}} - \\
 & \left( 5 a^2 b \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+f x]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 2 (a^2+b^2)^{5/2} f \sqrt{d \operatorname{Sec}[e+f x]} \right) + \\
 & \left( 5 a^2 b \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+f x]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 2 (a^2+b^2)^{5/2} f \sqrt{d \operatorname{Sec}[e+f x]} \right) + \\
 & \frac{b (2 a^2 - 3 b^2) \operatorname{Sec}[e+f x]^2}{(a^2+b^2)^2 f \sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])} + \frac{2 (b+a \operatorname{Tan}[e+f x])}{(a^2+b^2) f \sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 33334 leaves): Display of huge result suppressed!

**Problem 615: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])^2} dx$$

Optimal (type 4, 520 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{7 a b^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x])^{3/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x])^{3/4}}{2 (a^2+b^2)^{11/4} f (d \operatorname{Sec}[e+f x])^{3/2}} - \\
 & \frac{7 a b^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x])^{3/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x])^{3/4}}{2 (a^2+b^2)^{11/4} f (d \operatorname{Sec}[e+f x])^{3/2}} + \\
 & \left( (2 a^2 - 5 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (\operatorname{Sec}[e+f x])^{3/4} \right) / \\
 & \left( 3 (a^2+b^2)^2 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \left( 7 a^2 b^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x])^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+f x])^{3/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 2 (a^2+b^2)^3 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \left( 7 a^2 b^2 \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x])^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+f x])^{3/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 2 (a^2+b^2)^3 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \frac{b (2 a^2 - 5 b^2) \operatorname{Sec}[e+f x]^2}{3 (a^2+b^2)^2 f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])} + \\
 & \frac{2 (b+a \operatorname{Tan}[e+f x])}{3 (a^2+b^2) f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 11962 leaves):

$$\begin{aligned}
 & \left( \operatorname{Sec}[e+f x]^4 (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])^2 \left( \frac{b (2 a^2 - 3 b^2)}{3 a (a - i b)^2 (a + i b)^2} + \frac{2 a b \operatorname{Cos}[2 (e+f x)]}{3 (a - i b)^2 (a + i b)^2} \right. \right. \\
 & \left. \left. + \frac{b^4 \operatorname{Sin}[e+f x]}{a (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])} + \frac{(a^2 - b^2) \operatorname{Sin}[2 (e+f x)]}{3 (a - i b)^2 (a + i b)^2} \right) \right) / \\
 & \left( f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])^2 \right) + \left( 2 \operatorname{Sec}[e+f x]^{7/2} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])^2 \right. \\
 & \left. \left( a^3 / \left( 3 (a - i b)^2 (a + i b)^2 \sqrt{\operatorname{Sec}[e+f x]} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x]) \right) + \right. \right. \\
 & \left. \left. (8 a b^2) / \left( 3 (a - i b)^2 (a + i b)^2 \sqrt{\operatorname{Sec}[e+f x]} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x]) \right) \right) + \right. \\
 & \left. \frac{a^2 b \sqrt{\operatorname{Sec}[e+f x]} \operatorname{Sin}[e+f x]}{3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])} - \right)
 \end{aligned}$$

$$\left( \frac{5 b^3 \sqrt{\text{Sec}[e + f x]} \text{Sin}[e + f x]}{6 (a - i b)^2 (a + i b)^2 (a \text{Cos}[e + f x] + b \text{Sin}[e + f x])} \right) \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2}}$$

$$\left( a^2 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (e + f x)\right]\right], -1\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2} + \right.$$

$$8 b^2 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (e + f x)\right]\right], -1\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2} +$$

$$\left. 21 b^4 \left( (a + b + \sqrt{a^2 + b^2}) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\text{Tan}\left[\frac{1}{2} (e+fx)\right] )}}{i+\text{Tan}\left[\frac{1}{2} (e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1 - i) a \right. \right.$$

$$\left. \left. \text{EllipticPi}\left[\frac{(1+i)(a-i(b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\text{Tan}\left[\frac{1}{2} (e+fx)\right] )}}{i+\text{Tan}\left[\frac{1}{2} (e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] \right) \right)$$

$$\left. \sqrt{-\frac{1+i \text{Tan}\left[\frac{1}{2} (e + f x)\right]}{i + \text{Tan}\left[\frac{1}{2} (e + f x)\right]} \left(i + \text{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2 \frac{-1 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2}{\left(i + \text{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2}} \right)$$

$$\left( \sqrt{2} \sqrt{a^2 + b^2} (i a + b + \sqrt{a^2 + b^2}) (a + b + \sqrt{a^2 + b^2}) \sqrt{1 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2} \right) +$$

$$\left( 21 b^3 \left( (a + b - \sqrt{a^2 + b^2}) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\text{Tan}\left[\frac{1}{2} (e+fx)\right] )}}{i+\text{Tan}\left[\frac{1}{2} (e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1 - i) a \right. \right.$$



$$\left. \text{EllipticPi} \left[ \frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2+2i \tan[\frac{1}{2}(e+fx)]}{i+\tan[\frac{1}{2}(e+fx)]}} \left( i+\tan[\frac{1}{2}(e+fx)] \right)^2 \sqrt{\frac{-1+\tan[\frac{1}{2}(e+fx)]^2}{\left( i+\tan[\frac{1}{2}(e+fx)] \right)^2}} \right) /$$

$$\left( 2(-a-b+\sqrt{a^2+b^2})(-ia-b+\sqrt{a^2+b^2}) \sqrt{1+\tan[\frac{1}{2}(e+fx)]^2} \right) -$$

$$\left( 21b^4 \left( (a+b-\sqrt{a^2+b^2}) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] - (1-i)a \right. \right.$$

$$\left. \text{EllipticPi} \left[ \frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}}}{\sqrt{2}} \right], 2 \right] \right)$$

$$\left. \sqrt{-\frac{2+2i \tan[\frac{1}{2}(e+fx)]}{i+\tan[\frac{1}{2}(e+fx)]}} \left( i+\tan[\frac{1}{2}(e+fx)] \right)^2 \sqrt{\frac{-1+\tan[\frac{1}{2}(e+fx)]^2}{\left( i+\tan[\frac{1}{2}(e+fx)] \right)^2}} \right) /$$

$$\left( 2\sqrt{a^2+b^2}(-a-b+\sqrt{a^2+b^2})(-ia-b+\sqrt{a^2+b^2}) \sqrt{1+\tan[\frac{1}{2}(e+fx)]^2} \right) +$$

$$\left( 21 b^3 \left( (a + b + \sqrt{a^2 + b^2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}}}{\sqrt{2}}}\right], 2\right] - (1-i) a \right. \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{(1+i)(a-i(b+\sqrt{a^2+b^2}))}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan[\frac{1}{2}(e+fx)])}{i+\tan[\frac{1}{2}(e+fx)]}}}{\sqrt{2}}}\right], 2\right] \right) \right)$$

$$\left. \left. \sqrt{-\frac{2+2i\tan[\frac{1}{2}(e+fx)]}{i+\tan[\frac{1}{2}(e+fx)]}} \left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\tan[\frac{1}{2}(e+fx)]^2}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) \right) /$$

$$\left( 2 \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) \right) / \left( 3 (a^2 + b^2)^2 f \right)$$

$$(d \operatorname{Sec}[e + f x])^{3/2} \left( \frac{1}{3 (a^2 + b^2)^2} \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \left( \frac{1}{1 - \tan\left[\frac{1}{2}(e + f x)\right]^2} \right)^{3/2} \right)$$

$$\left( a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \tan\left[\frac{1}{2}(e + f x)\right]^2} + \right.$$

$$\left. 8 b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(e + f x)\right]\right], -1\right] \sqrt{1 - \tan\left[\frac{1}{2}(e + f x)\right]^2} + \right)$$

$$\left( 21 b^4 \left( a + b + \sqrt{a^2 + b^2} \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1-i) a \right.$$

$$\text{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], \right.$$

$$\left. 2 \right] \sqrt{\frac{1 + i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}} \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2$$

$$\left. \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right) / \left( \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \right)$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} + \left( 21 b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \right.$$

$$\text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1-i) a \text{EllipticPi} \left[ \right.$$

$$\left. \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right]$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/$$

$$\left(2\left(-a-b+\sqrt{a^2+b^2}\right)\left(-ia-b+\sqrt{a^2+b^2}\right)\sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right) -$$

$$\left(21b^4\left(a+b-\sqrt{a^2+b^2}\right)\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right)-(1-i)$$

$$a\operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right],$$

$$2\right)\sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2$$

$$\left.\sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right/ \left(2\sqrt{a^2+b^2}\left(-a-b+\sqrt{a^2+b^2}\right)\right)$$

$$\left(-ia-b+\sqrt{a^2+b^2}\right)\sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} + 21b^3\left(a+b+\sqrt{a^2+b^2}\right)$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right)\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right] - (1-i) a \text{EllipticPi}\left[\right. \\
 & \left. \frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right)\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right] \right) \\
 & \left. \sqrt{-\frac{2+2i \text{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} \sqrt{\frac{-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}\right) \sqrt{2} \\
 & \left( 2 \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \frac{1}{3(a^2 + b^2)^2} 2 \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}} \left( \left( a^2 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right]\right], \right. \right. \\
 & \left. \left. -1\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) / \left( 2 \sqrt{1 - \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) - \\
 & \left( 4 b^2 \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right]\right], -1\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) / \\
 & \left( \sqrt{1 - \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) -
 \end{aligned}$$

$$\left( 21 b^4 \left( (a + b + \sqrt{a^2 + b^2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right) - \right.$$

$$(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)(a-i)(b+\sqrt{a^2+b^2})}{a+b+\sqrt{a^2+b^2}}\right],$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right.$$

$$\left. \sqrt{-\frac{1+i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right) /$$

$$\left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left(i a + b + \sqrt{a^2 + b^2}\right) \left(a + b + \sqrt{a^2 + b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \right)^{3/2} -$$

$$\left( 21 b^3 \left( (a + b - \sqrt{a^2 + b^2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right) - \right.$$

$$(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)(a+i)(-b+\sqrt{a^2+b^2})}{a+b-\sqrt{a^2+b^2}}\right],$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)$$

$$\left. \begin{aligned}
 & \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \\
 & \left(4\left(-a-b+\sqrt{a^2+b^2}\right)\left(-i a-b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^{3/2}\right) + \\
 & \left(21 b^4\left(a+b-\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right) - \right. \\
 & \left.(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}\right], 2\right) \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
 & \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \\
 & \left(4 \sqrt{a^2+b^2}\left(-a-b+\sqrt{a^2+b^2}\right)\left(-i a-b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2\right)^{3/2} - \\
 & \left(21 b^3\left(a+b+\sqrt{a^2+b^2}\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right) - \right. \\
 & \left.(1-i) a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], 2\right)
 \end{aligned} \right)$$

$$\left. \begin{aligned}
 & \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \\
 & \sqrt{-\frac{2+2i\text{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \Big/ \\
 & \left(4\left(i a+b+\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^{3/2}\right)+ \\
 & \frac{a^2 \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}}+\frac{4 b^2 \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{\sqrt{1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}}+ \\
 & \left(21 b^4\left(a+b+\sqrt{a^2+b^2}\right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], 2\right]-\right. \\
 & \left.(1-i) a \text{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right], \right. \\
 & \left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \left. \sqrt{-\frac{1+i\text{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \Big/ \right.
 \end{aligned} \right)$$



$$\begin{aligned}
 & \left( \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) + \\
 & \left( 21 b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right] - \right. \\
 & \quad (1-i) a \text{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}\right], \right. \\
 & \quad \left. \left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & \left. \sqrt{-\frac{2+2i \tan\left[\frac{1}{2}(e+fx)\right]}{i+\tan\left[\frac{1}{2}(e+fx)\right]}} \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right) \sqrt{\frac{-1+\tan\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right) / \\
 & \left( 2 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \tan\left[\frac{1}{2}(e + f x)\right]^2} \right) - \\
 & \left( 21 b^4 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}}\right], 2\right] - \right. \\
 & \quad \left. (1-i) a \text{EllipticPi}\left[\frac{(1+i)\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)}{a+b-\sqrt{a^2+b^2}}\right], \right.
 \end{aligned}$$

$$\left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right)\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2
 \right)$$

$$\left. \sqrt{-\frac{2+2i\text{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\sqrt{\frac{-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}
 \right)$$

$$\left(2\sqrt{a^2+b^2}\left(-a-b+\sqrt{a^2+b^2}\right)\left(-ia-b+\sqrt{a^2+b^2}\right)\sqrt{1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)+$$

$$\left(21b^3\left(a+b+\sqrt{a^2+b^2}\right)\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right)\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}\right], 2\right]-
 \right.$$

$$\left.(1-i)a\text{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}\right],
 \right.$$

$$\left. \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right)\right)}}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}\right], 2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2
 \right)$$

$$\left. \sqrt{-\frac{2+2i\text{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]}}\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\sqrt{\frac{-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}
 \right)$$

$$\left(2\left(ia+b+\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\sqrt{1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)+$$

$$\left( 21 b^4 \left( (a + b + \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1 - i) \right. \right.$$

$$a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], \right.$$

$$\left. \left. 2 \right] \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2 \sqrt{\frac{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right.$$

$$\left. \left. \left( \frac{\sec \left[ \frac{1}{2} (e+fx) \right]^2 \left( 1 + i \tan \left[ \frac{1}{2} (e+fx) \right] \right)}{2 \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)^2} - \frac{i \sec \left[ \frac{1}{2} (e+fx) \right]^2}{2 \left( i + \tan \left[ \frac{1}{2} (e+fx) \right] \right)} \right) \right) \right)$$

$$\left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \right.$$

$$\left. \sqrt{-\frac{1 + i \tan \left[ \frac{1}{2} (e+fx) \right]}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}} \sqrt{1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} \right) +$$

$$\left( 21 b^3 \left( (a + b - \sqrt{a^2 + b^2}) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], 2 \right] - (1 - i) \right. \right.$$

$$a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left(1 + \tan \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \tan \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}}} \right], \right.$$

$$\left. \begin{aligned}
 & 2 \left[ \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right. \\
 & \left. \left( \frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 (2 + 2i \tan\left[\frac{1}{2}(e+fx)\right])}{2 \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2} - \frac{i \sec\left[\frac{1}{2}(e+fx)\right]^2}{i + \tan\left[\frac{1}{2}(e+fx)\right]} \right) \right] \\
 & \left( 4 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e+fx)\right]}{i + \tan\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \left. \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right) - \\
 & \left( 21 b^4 \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) \right. \\
 & \left. a \operatorname{EllipticPi}\left[\frac{(1+i)(a+i(-b+\sqrt{a^2+b^2}))}{a+b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)(1+\tan\left[\frac{1}{2}(e+fx)\right])}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], \right. \\
 & \left. 2 \left[ \left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right) \right]
 \end{aligned} \right)$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{2 \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{i \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} \right) \sqrt{$$

$$\left( 4 \sqrt{a^2+b^2} \left(-a-b+\sqrt{a^2+b^2}\right) \left(-i a-b+\sqrt{a^2+b^2}\right) \right.$$

$$\left. \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 21 b^3 \left( a+b+\sqrt{a^2+b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], 2\right] - (1-i) \right.$$

$$\left. a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}}{\sqrt{2}}}\right], \right.$$

$$\left. 2 \right] \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}}$$

$$\left. \right) \sqrt{$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{2 \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{i \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} \right) \sqrt{$$

$$\left( 4 \left(i a+b+\sqrt{a^2+b^2}\right) \left(a+b+\sqrt{a^2+b^2}\right) \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right)$$

$$\begin{aligned}
 & \sqrt{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2} + \\
 & \left( 21 b^4 \left( a + b + \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], 2\right] - (1-i) \right. \\
 & a \text{EllipticPi}\left[\frac{(1+i)\left(a-i\left(b+\sqrt{a^2+b^2}\right)\right)}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], \right. \\
 & \left. \left. 2\right] \sqrt{-\frac{1+i \tan\left[\frac{1}{2}(e+fx)\right]}{i+\tan\left[\frac{1}{2}(e+fx)\right]}} \left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2} \right. \\
 & \left. \left. \left( \frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\sec\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \right) \right) \\
 & \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\tan\left[\frac{1}{2}(e+fx)\right]\right)^2}} \sqrt{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 21 b^3 \left( a + b - \sqrt{a^2 + b^2} \right) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1+\tan\left[\frac{1}{2}(e+fx)\right]}\right)}}{i+\tan\left[\frac{1}{2}(e+fx)\right]}}{\sqrt{2}}\right], 2\right] - (1-i) \right.
 \end{aligned}$$

$$\begin{aligned}
 & a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], \right. \\
 & \left. 2 \right] \sqrt{-\frac{2 + 2i \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2} \\
 & \left( \frac{\operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2} - \frac{\operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^3} \right) \sqrt{ \\
 & \left( 4 \left( -a - b + \sqrt{a^2 + b^2} \right) \left( -i a - b + \sqrt{a^2 + b^2} \right) \sqrt{\frac{-1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{\left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2}} \right. \\
 & \left. \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2} \right) - \\
 & \left( 21 b^4 \left( \left( a + b - \sqrt{a^2 + b^2} \right) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], 2 \right) - (1-i) \right. \right. \\
 & \left. \left. a \operatorname{EllipticPi} \left[ \frac{(1+i) \left( a + i \left( -b + \sqrt{a^2 + b^2} \right) \right)}{a + b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)}}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}}{\sqrt{2}} \right], \right. \right. \\
 & \left. \left. 2 \right] \sqrt{-\frac{2 + 2i \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]} \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right)^2} \right) \right)
 \end{aligned}$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \sqrt{\phantom{x}}$$

$$\left( 4 \sqrt{a^2 + b^2} \left(-a - b + \sqrt{a^2 + b^2}\right) \left(-i a - b + \sqrt{a^2 + b^2}\right) \right.$$

$$\left. \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) +$$

$$\left( 21 b^3 \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], 2\right] - (1 - i) \right.$$

$$\left. a \operatorname{EllipticPi}\left[\frac{(1+i)\left(a - i\left(b + \sqrt{a^2 + b^2}\right)\right)}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(1+i)\left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}\right)}}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}}\right], \right.$$

$$\left. 2\right] \sqrt{-\frac{2 + 2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2$$

$$\left( \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} - \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^3} \right) \sqrt{\phantom{x}}$$

$$\left( 4 \left(i a + b + \sqrt{a^2 + b^2}\right) \left(a + b + \sqrt{a^2 + b^2}\right) \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right)$$



$$\begin{aligned}
 & \sqrt{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2} + \\
 & \left( 21b^3 \sqrt{-\frac{2 + 2i \tan\left[\frac{1}{2}(e + fx)\right]}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \left(i + \tan\left[\frac{1}{2}(e + fx)\right]\right)^2 \sqrt{\frac{-1 + \tan\left[\frac{1}{2}(e + fx)\right]^2}{\left(i + \tan\left[\frac{1}{2}(e + fx)\right]\right)^2}} \right. \\
 & \left. \left( \left( (a + b - \sqrt{a^2 + b^2}) \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \sec\left[\frac{1}{2}(e + fx)\right]^2}{i + \tan\left[\frac{1}{2}(e + fx)\right]} - \left(\frac{1}{2} + \frac{i}{2}\right) \sec\left[\frac{1}{2}(e + fx)\right]^2 \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)\right) \right) \right) / \left(i + \tan\left[\frac{1}{2}(e + fx)\right]\right)^2 \right) \right) / \\
 & \left( 2\sqrt{2} \sqrt{\frac{(1+i)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \sqrt{1 - \frac{(1+i)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left(\frac{1}{2} + \frac{i}{2}\right)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \right) - \\
 & \left( \left(\frac{1}{2} - \frac{i}{2}\right) a \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \sec\left[\frac{1}{2}(e + fx)\right]^2}{i + \tan\left[\frac{1}{2}(e + fx)\right]} - \left(\frac{1}{2} + \frac{i}{2}\right) \sec\left[\frac{1}{2}(e + fx)\right]^2 \right. \right. \\
 & \left. \left. \left. \left. \left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)\right) \right) \right) / \left(i + \tan\left[\frac{1}{2}(e + fx)\right]\right)^2 \right) \right) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \sqrt{1 - \frac{(1+i)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \right. \\
 & \left. \sqrt{1 - \frac{\left(\frac{1}{2} + \frac{i}{2}\right)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)}{i + \tan\left[\frac{1}{2}(e + fx)\right]}} \left(1 - \left(i\left(a + i\left(-b + \sqrt{a^2 + b^2}\right)\right)\left(1 + \tan\left[\frac{1}{2}(e + fx)\right]\right)\right) \right) \right) \right) / \\
 & \left. \left. \left. \left. \left( (a + b - \sqrt{a^2 + b^2}) \left( i + \tan\left[\frac{1}{2}(e + fx)\right] \right) \right) \right) \right) \right) \right) / \\
 & \left( 2\left(-a - b + \sqrt{a^2 + b^2}\right)\left(-i a - b + \sqrt{a^2 + b^2}\right) \sqrt{1 + \tan\left[\frac{1}{2}(e + fx)\right]^2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 21 b^4 \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right. \\
 & \left( \left( (a+b-\sqrt{a^2+b^2}) \left( \frac{\left(\frac{1}{2}+\frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} - \left(\frac{1}{2}+\frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. (1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]) \right) \right) \right) / \left( i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \right) \Bigg) / \\
 & \left( 2\sqrt{2} \sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1-\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \left. \sqrt{1-\frac{\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right) - \\
 & \left( \left(\frac{1}{2}-\frac{i}{2}\right) a \left( \frac{\left(\frac{1}{2}+\frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} - \left(\frac{1}{2}+\frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left. (1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]) \right) \right) / \left( i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \right) \Bigg) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1-\frac{(1+i)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \left. \sqrt{1-\frac{\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(1-\left(i\left(a+i\left(-b+\sqrt{a^2+b^2}\right)\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right) \right) \right. \\
 & \left. \left. \left. \frac{1}{2}(e+fx)\right) \right) \right) / \left( (a+b-\sqrt{a^2+b^2}) \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \right) \Bigg) \Bigg) / \\
 & \left( 2\sqrt{a^2+b^2} \left(-a-b+\sqrt{a^2+b^2}\right) \left(-i a-b+\sqrt{a^2+b^2}\right) \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 21 b^4 \sqrt{-\frac{1+i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2 \sqrt{\frac{-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left(i+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2}} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( (a+b+\sqrt{a^2+b^2}) \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} - \left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \right) \right) / \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \right) / \\
 & \left( 2\sqrt{2} \sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1 - \frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \quad \left. \sqrt{1 - \frac{\left(\frac{1}{2} + \frac{i}{2}\right)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right) - \\
 & \left( \left(\frac{1}{2} - \frac{i}{2}\right) a \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} - \left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left. \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \right) \right) / \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \right) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \sqrt{1 - \frac{(1+i)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right. \\
 & \quad \left. \sqrt{1 - \frac{\left(\frac{1}{2} + \frac{i}{2}\right)(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right])}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \right) \left( 1 - \left( i \left( a - i \left( b + \sqrt{a^2+b^2} \right) \right) \left( 1 + \operatorname{Tan}\left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \frac{1}{2}(e+fx) \right] \right) \right) \right) / \left( \left( a + b + \sqrt{a^2+b^2} \right) \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \right) / \\
 & \left( \sqrt{2} \sqrt{a^2+b^2} \left( i a + b + \sqrt{a^2+b^2} \right) \left( a + b + \sqrt{a^2+b^2} \right) \sqrt{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right) + \\
 & \left( 21 b^3 \sqrt{-\frac{2+2i \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}} \left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\frac{-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{\left( i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right)^2}} \right. \\
 & \quad \left. \left( \left( a + b + \sqrt{a^2+b^2} \right) \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{i + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]} - \left(\frac{1}{2} + \frac{i}{2}\right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) / \left( \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right) - \right. \\
 & \left. \left( \left( \frac{1}{2} - \frac{i}{2} \right) a \left( \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]} - \left( \left( \frac{1}{2} + \frac{i}{2} \right) \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right. \right. \right. \\
 & \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) / \left( \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) \Bigg) / \\
 & \left( \sqrt{2} \sqrt{\frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \sqrt{1 - \frac{(1+i) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{\left( \frac{1}{2} + \frac{i}{2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right)}{i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}} \left( 1 - \left( i \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) \left( 1 + \operatorname{Tan} \left[ \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left. \frac{1}{2} (e + f x) \right] \right) \right) \right) \right) / \left( \left( a + b + \sqrt{a^2 + b^2} \right) \left( i + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right) \right) \right) \Bigg) / \\
 & \left( 2 \left( i a + b + \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2} \right) \Bigg) \left( a + b \operatorname{Tan} [e + \right. \\
 & \left. f x] \right)^2 \Bigg)
 \end{aligned}$$

Problem 616: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int \frac{1}{(d \operatorname{Sec}[e + f x])^{5/2} (a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 4, 700 leaves, 19 steps):

$$\begin{aligned} & \frac{9 a b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x])^{1/4}}{(a^2 + b^2)^{1/4}}\right] (\operatorname{Sec}[e + f x])^{1/4}}{2 (a^2 + b^2)^{13/4} d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} - \\ & \frac{9 a b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e + f x])^{1/4}}{(a^2 + b^2)^{1/4}}\right] (\operatorname{Sec}[e + f x])^{1/4}}{2 (a^2 + b^2)^{13/4} d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} + \\ & \left( 3 (2 a^4 + 10 a^2 b^2 - 7 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e + f x]], 2\right] (\operatorname{Sec}[e + f x])^{1/4} \right) / \\ & \left( 5 (a^2 + b^2)^3 d^2 f \sqrt{d \operatorname{Sec}[e + f x]} \right) - \frac{3 (2 a^4 + 10 a^2 b^2 - 7 b^4) \operatorname{Tan}[e + f x]}{5 (a^2 + b^2)^3 d^2 f \sqrt{d \operatorname{Sec}[e + f x]}} - \\ & \left( 9 a^2 b^3 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e + f x])^{1/4}], -1\right] \right. \\ & \quad \left. (\operatorname{Sec}[e + f x])^{1/4} \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( 2 (a^2 + b^2)^{7/2} d^2 f \sqrt{d \operatorname{Sec}[e + f x]} \right) + \\ & \left( 9 a^2 b^3 \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e + f x])^{1/4}], -1\right] \right. \\ & \quad \left. (\operatorname{Sec}[e + f x])^{1/4} \sqrt{-\operatorname{Tan}[e + f x]^2} \right) / \left( 2 (a^2 + b^2)^{7/2} d^2 f \sqrt{d \operatorname{Sec}[e + f x]} \right) + \\ & \frac{3 b (2 a^4 + 10 a^2 b^2 - 7 b^4) \operatorname{Sec}[e + f x]^2}{5 (a^2 + b^2)^3 d^2 f \sqrt{d \operatorname{Sec}[e + f x]} (a + b \operatorname{Tan}[e + f x])} + \\ & \frac{2 \operatorname{Cos}[e + f x]^2 (b + a \operatorname{Tan}[e + f x])}{5 (a^2 + b^2) d^2 f \sqrt{d \operatorname{Sec}[e + f x]} (a + b \operatorname{Tan}[e + f x])} - \\ & \frac{2 (b (2 a^2 - 7 b^2) - 3 a (a^2 + 4 b^2) \operatorname{Tan}[e + f x])}{5 (a^2 + b^2)^2 d^2 f \sqrt{d \operatorname{Sec}[e + f x]} (a + b \operatorname{Tan}[e + f x])} \end{aligned}$$

Result (type 4, 34 806 leaves): Display of huge result suppressed!

Problem 617: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e + f x])^{7/2}}{(a + b \operatorname{Tan}[e + f x])^3} dx$$

Optimal (type 4, 583 leaves, 18 steps):

$$\begin{aligned}
& \frac{3 (a^2 + 2 b^2) d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+fx])^{3/2}}{8 b^{5/2} (a^2 + b^2)^{5/4} f (\operatorname{Sec}[e+fx]^2)^{3/4}} - \\
& \frac{3 (a^2 + 2 b^2) d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+fx])^{3/2}}{8 b^{5/2} (a^2 + b^2)^{5/4} f (\operatorname{Sec}[e+fx]^2)^{3/4}} + \\
& \frac{3 a d^2 \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] (d \operatorname{Sec}[e+fx])^{3/2}}{4 b^2 (a^2 + b^2) f (\operatorname{Sec}[e+fx]^2)^{3/4}} - \\
& \frac{3 a d^2 \operatorname{Cos}[e+fx] (d \operatorname{Sec}[e+fx])^{3/2} \operatorname{Sin}[e+fx]}{4 b^2 (a^2 + b^2) f} - \\
& \left( 3 a (a^2 + 2 b^2) d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx]^2)^{1/4}], -1\right] \right. \\
& \quad \left. (d \operatorname{Sec}[e+fx])^{3/2} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8 b^3 (a^2 + b^2)^{3/2} f (\operatorname{Sec}[e+fx]^2)^{3/4} \right) + \\
& \left( 3 a (a^2 + 2 b^2) d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2 + b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx]^2)^{1/4}], -1\right] \right. \\
& \quad \left. (d \operatorname{Sec}[e+fx])^{3/2} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8 b^3 (a^2 + b^2)^{3/2} f (\operatorname{Sec}[e+fx]^2)^{3/4} \right) - \\
& \frac{d^2 (d \operatorname{Sec}[e+fx])^{3/2}}{2 b f (a + b \operatorname{Tan}[e+fx])^2} + \frac{3 a d^2 (d \operatorname{Sec}[e+fx])^{3/2}}{4 b (a^2 + b^2) f (a + b \operatorname{Tan}[e+fx])}
\end{aligned}$$

Result (type 4, 31478 leaves): Display of huge result suppressed!

**Problem 618:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e+fx])^{5/2}}{(a + b \operatorname{Tan}[e+fx])^3} dx$$

Optimal (type 4, 532 leaves, 18 steps):

$$\begin{aligned}
 & \frac{(a^2 - 2b^2) d^2 \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+fx]}}{8b^{3/2} (a^2+b^2)^{7/4} f (\operatorname{Sec}[e+fx]^2)^{1/4}} + \\
 & \frac{(a^2 - 2b^2) d^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+fx]}}{8b^{3/2} (a^2+b^2)^{7/4} f (\operatorname{Sec}[e+fx]^2)^{1/4}} + \\
 & \frac{a d^2 \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] \sqrt{d \operatorname{Sec}[e+fx]}}{4b^2 (a^2+b^2) f (\operatorname{Sec}[e+fx]^2)^{1/4}} - \\
 & \left( a (a^2 - 2b^2) d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+fx]} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8b^2 (a^2+b^2)^2 f (\operatorname{Sec}[e+fx]^2)^{1/4} \right) - \\
 & \left( a (a^2 - 2b^2) d^2 \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+fx]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+fx]} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8b^2 (a^2+b^2)^2 f (\operatorname{Sec}[e+fx]^2)^{1/4} \right) - \\
 & \frac{d^2 \sqrt{d \operatorname{Sec}[e+fx]}}{2bf (a+b \operatorname{Tan}[e+fx])^2} + \frac{a d^2 \sqrt{d \operatorname{Sec}[e+fx]}}{4b (a^2+b^2) f (a+b \operatorname{Tan}[e+fx])}
 \end{aligned}$$

Result (type 4, 21475 leaves): Display of huge result suppressed!

**Problem 619: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e+fx])^{3/2}}{(a+b \operatorname{Tan}[e+fx])^3} dx$$

Optimal (type 4, 566 leaves, 18 steps):

$$\begin{aligned}
 & \frac{(3 a^2 - 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{8 \sqrt{b} (a^2+b^2)^{9/4} f (\operatorname{Sec}[e+f x]^2)^{3/4}} - \\
 & \frac{(3 a^2 - 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (d \operatorname{Sec}[e+f x])^{3/2}}{8 \sqrt{b} (a^2+b^2)^{9/4} f (\operatorname{Sec}[e+f x]^2)^{3/4}} - \\
 & \frac{5 a \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (d \operatorname{Sec}[e+f x])^{3/2}}{4 (a^2+b^2)^2 f (\operatorname{Sec}[e+f x]^2)^{3/4}} + \\
 & \frac{5 a \operatorname{Cos}[e+f x] (d \operatorname{Sec}[e+f x])^{3/2} \operatorname{Sin}[e+f x]}{4 (a^2+b^2)^2 f} - \\
 & \left( a (3 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 b (a^2+b^2)^{5/2} f (\operatorname{Sec}[e+f x]^2)^{3/4} \right) + \\
 & \left( a (3 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{3/2} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 b (a^2+b^2)^{5/2} f (\operatorname{Sec}[e+f x]^2)^{3/4} \right) - \\
 & \frac{b (d \operatorname{Sec}[e+f x])^{3/2}}{2 (a^2+b^2) f (a+b \operatorname{Tan}[e+f x])^2} - \frac{5 a b (d \operatorname{Sec}[e+f x])^{3/2}}{4 (a^2+b^2)^2 f (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 31542 leaves): Display of huge result suppressed!

**Problem 620: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{d \operatorname{Sec}[e+f x]}}{(a+b \operatorname{Tan}[e+f x])^3} dx$$

Optimal (type 4, 515 leaves, 18 steps):



$$\begin{aligned}
 & \frac{3 \sqrt{b} (5 a^2 - 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{8 (a^2+b^2)^{11/4} f (\operatorname{Sec}[e+f x]^2)^{1/4}} - \\
 & \frac{3 \sqrt{b} (5 a^2 - 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] \sqrt{d \operatorname{Sec}[e+f x]}}{8 (a^2+b^2)^{11/4} f (\operatorname{Sec}[e+f x]^2)^{1/4}} - \\
 & \frac{7 a \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] \sqrt{d \operatorname{Sec}[e+f x]}}{4 (a^2+b^2)^2 f (\operatorname{Sec}[e+f x]^2)^{1/4}} + \\
 & \left(3 a (5 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+f x]} \sqrt{-\operatorname{Tan}[e+f x]^2}\right) / \left(8 (a^2+b^2)^3 f (\operatorname{Sec}[e+f x]^2)^{1/4}\right) + \\
 & \left(3 a (5 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
 & \quad \left. \sqrt{d \operatorname{Sec}[e+f x]} \sqrt{-\operatorname{Tan}[e+f x]^2}\right) / \left(8 (a^2+b^2)^3 f (\operatorname{Sec}[e+f x]^2)^{1/4}\right) - \\
 & \frac{b \sqrt{d \operatorname{Sec}[e+f x]}}{2 (a^2+b^2) f (a+b \operatorname{Tan}[e+f x])^2} - \frac{7 a b \sqrt{d \operatorname{Sec}[e+f x]}}{4 (a^2+b^2)^2 f (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 41235 leaves): Display of huge result suppressed!

**Problem 621: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])^3} dx$$

Optimal (type 4, 664 leaves, 19 steps):

$$\begin{aligned}
& \frac{5 b^{3/2} (7 a^2 - 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{1/4}}{8 (a^2+b^2)^{13/4} f \sqrt{d \operatorname{Sec}[e+f x]}} - \\
& \frac{5 b^{3/2} (7 a^2 - 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{1/4}}{8 (a^2+b^2)^{13/4} f \sqrt{d \operatorname{Sec}[e+f x]}} + \\
& \left( a (8 a^2 - 37 b^2) \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (\operatorname{Sec}[e+f x]^2)^{1/4} \right) / \\
& \left( 4 (a^2+b^2)^3 f \sqrt{d \operatorname{Sec}[e+f x]} \right) - \frac{a (8 a^2 - 37 b^2) \operatorname{Tan}[e+f x]}{4 (a^2+b^2)^3 f \sqrt{d \operatorname{Sec}[e+f x]}} - \\
& \left( 5 a b (7 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
& \left. (\operatorname{Sec}[e+f x]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 (a^2+b^2)^{7/2} f \sqrt{d \operatorname{Sec}[e+f x]} \right) + \\
& \left( 5 a b (7 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[(\operatorname{Sec}[e+f x]^2)^{1/4}\right], -1\right] \right. \\
& \left. (\operatorname{Sec}[e+f x]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 (a^2+b^2)^{7/2} f \sqrt{d \operatorname{Sec}[e+f x]} \right) + \\
& \frac{b (4 a^2 - 5 b^2) \operatorname{Sec}[e+f x]^2}{2 (a^2+b^2)^2 f \sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])^2} + \\
& \frac{2 (b+a \operatorname{Tan}[e+f x])}{(a^2+b^2) f \sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])^2} + \\
& \frac{a b (8 a^2 - 37 b^2) \operatorname{Sec}[e+f x]^2}{4 (a^2+b^2)^3 f \sqrt{d \operatorname{Sec}[e+f x]} (a+b \operatorname{Tan}[e+f x])}
\end{aligned}$$

Result (type 4, 32867 leaves): Display of huge result suppressed!

**Problem 622: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])^3} dx$$

Optimal (type 4, 620 leaves, 19 steps):

$$\begin{aligned}
 & - \frac{7 b^{5/2} (9 a^2 - 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{3/4}}{8 (a^2+b^2)^{15/4} f (d \operatorname{Sec}[e+f x])^{3/2}} - \\
 & \frac{7 b^{5/2} (9 a^2 - 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+f x]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+f x]^2)^{3/4}}{8 (a^2+b^2)^{15/4} f (d \operatorname{Sec}[e+f x])^{3/2}} + \\
 & \left( a (8 a^2 - 69 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+f x]], 2\right] (\operatorname{Sec}[e+f x]^2)^{3/4} \right) / \\
 & \left( 12 (a^2+b^2)^3 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \left( 7 a b^2 (9 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+f x]^2)^{3/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 (a^2+b^2)^4 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \left( 7 a b^2 (9 a^2 - 2 b^2) \operatorname{Cot}[e+f x] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+f x]^2)^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+f x]^2)^{3/4} \sqrt{-\operatorname{Tan}[e+f x]^2} \right) / \left( 8 (a^2+b^2)^4 f (d \operatorname{Sec}[e+f x])^{3/2} \right) + \\
 & \frac{b (4 a^2 - 7 b^2) \operatorname{Sec}[e+f x]^2}{6 (a^2+b^2)^2 f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])^2} + \\
 & \frac{2 (b+a \operatorname{Tan}[e+f x])}{3 (a^2+b^2) f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])^2} + \\
 & \frac{a b (8 a^2 - 69 b^2) \operatorname{Sec}[e+f x]^2}{12 (a^2+b^2)^3 f (d \operatorname{Sec}[e+f x])^{3/2} (a+b \operatorname{Tan}[e+f x])}
 \end{aligned}$$

Result (type 4, 42324 leaves): Display of huge result suppressed!

**Problem 623: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e+f x])^{5/2} (a+b \operatorname{Tan}[e+f x])^3} dx$$

Optimal (type 4, 814 leaves, 20 steps):

$$\begin{aligned}
 & \frac{9 b^{7/2} (11 a^2 - 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{1/4}}{8 (a^2+b^2)^{17/4} d^2 f \sqrt{d \operatorname{Sec}[e+fx]}} - \\
 & \frac{9 b^{7/2} (11 a^2 - 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} (\operatorname{Sec}[e+fx]^2)^{1/4}}{(a^2+b^2)^{1/4}}\right] (\operatorname{Sec}[e+fx]^2)^{1/4}}{8 (a^2+b^2)^{17/4} d^2 f \sqrt{d \operatorname{Sec}[e+fx]}} + \\
 & \left( 3 a (8 a^4 + 64 a^2 b^2 - 139 b^4) \operatorname{EllipticE}\left[\frac{1}{2} \operatorname{ArcTan}[\operatorname{Tan}[e+fx]], 2\right] (\operatorname{Sec}[e+fx]^2)^{1/4} \right) / \\
 & \left( 20 (a^2+b^2)^4 d^2 f \sqrt{d \operatorname{Sec}[e+fx]} \right) - \frac{3 a (8 a^4 + 64 a^2 b^2 - 139 b^4) \operatorname{Tan}[e+fx]}{20 (a^2+b^2)^4 d^2 f \sqrt{d \operatorname{Sec}[e+fx]}} - \\
 & \left( 9 a b^3 (11 a^2 - 2 b^2) \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[-\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx]^2)^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+fx]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8 (a^2+b^2)^{9/2} d^2 f \sqrt{d \operatorname{Sec}[e+fx]} \right) + \\
 & \left( 9 a b^3 (11 a^2 - 2 b^2) \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{b}{\sqrt{a^2+b^2}}, \operatorname{ArcSin}[(\operatorname{Sec}[e+fx]^2)^{1/4}], -1\right] \right. \\
 & \left. (\operatorname{Sec}[e+fx]^2)^{1/4} \sqrt{-\operatorname{Tan}[e+fx]^2} \right) / \left( 8 (a^2+b^2)^{9/2} d^2 f \sqrt{d \operatorname{Sec}[e+fx]} \right) + \\
 & \frac{3 b (4 a^4 + 28 a^2 b^2 - 15 b^4) \operatorname{Sec}[e+fx]^2}{10 (a^2+b^2)^3 d^2 f \sqrt{d \operatorname{Sec}[e+fx]} (a+b \operatorname{Tan}[e+fx])^2} + \\
 & \frac{2 \operatorname{Cos}[e+fx]^2 (b+a \operatorname{Tan}[e+fx])}{5 (a^2+b^2) d^2 f \sqrt{d \operatorname{Sec}[e+fx]} (a+b \operatorname{Tan}[e+fx])^2} + \\
 & \frac{3 a b (8 a^4 + 64 a^2 b^2 - 139 b^4) \operatorname{Sec}[e+fx]^2}{20 (a^2+b^2)^4 d^2 f \sqrt{d \operatorname{Sec}[e+fx]} (a+b \operatorname{Tan}[e+fx])} - \\
 & \frac{2 (b (4 a^2 - 9 b^2) - a (3 a^2 + 16 b^2) \operatorname{Tan}[e+fx])}{5 (a^2+b^2)^2 d^2 f \sqrt{d \operatorname{Sec}[e+fx]} (a+b \operatorname{Tan}[e+fx])^2}
 \end{aligned}$$

Result (type 4, 34358 leaves): Display of huge result suppressed!

**Problem 626: Mathematica result simpler than optimal antiderivative, IF it can be verified!**

$$\int \frac{a+b \operatorname{Tan}[e+fx]}{(d \operatorname{Sec}[e+fx])^{1/3}} dx$$

Optimal (type 5, 76 leaves, 3 steps):

$$\frac{3 b}{f (d \operatorname{Sec}[e+fx])^{1/3}} - \frac{3 a d \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \operatorname{Cos}[e+fx]^2\right] \operatorname{Sin}[e+fx]}{4 f (d \operatorname{Sec}[e+fx])^{4/3} \sqrt{\operatorname{Sin}[e+fx]^2}}$$

Result (type 4, 2147 leaves):

$$\begin{aligned}
 & \left( \sqrt{1 - \cos[e + f x]^2} \right. \\
 & \left. \left( (-1)^{1/3} + \sec[e + f x]^{2/3} + \sqrt{3} \sec[e + f x]^{2/3} \right)^6 \sec[e + f x]^{1/3} (-1 + \sec[e + f x]^2)^2 \right. \\
 & \left. \left( -\frac{3b}{\sec[e + f x]^{1/3}} + 3a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{2/3} - \left( 6a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x] \right. \right. \right. \\
 & \left. \left. \left( (-1)^{1/3} \left( -6 \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} + (1 - \sqrt{3}) \sec[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right) + \right. \right. \right. \\
 & \left. \left. \left( 3 - \sqrt{3} \right) \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} + (1 - \sqrt{3}) \sec[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right) \right. \\
 & \left. \left. \left( (-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3} \right)^2 \sqrt{\frac{\left( (-1)^{1/3} + \sec[e + f x]^{2/3} \right) \sec[e + f x]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3} \right)^2}} \right. \right. \\
 & \left. \left. \sqrt{\frac{\left( (-1)^{2/3} - (-1)^{1/3} \sec[e + f x]^{2/3} + \sec[e + f x]^{4/3} \right)}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3} \right)^2}} \right) / \left( 4 \times 3^{3/4} \sec[e + f x]^{1/3} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec[e + f x]^2} \right) + \frac{(1 + \sqrt{3}) \sec[e + f x]^{1/3} \sqrt{-1 + \sec[e + f x]^2}}{2 \left( (-1)^{1/3} + (1 + \sqrt{3}) \sec[e + f x]^{2/3} \right)} \right) / \\
 & \left. \left. \left( \sqrt{-1 + \sec[e + f x]^2} \right) \right) (a + b \tan[e + f x]) \right) / \left( f (d \sec[e + f x])^{1/3} \right. \\
 & \left. \left( a \sin[e + f x] - 6 (-1)^{2/3} a \sec[e + f x]^{2/3} \sin[e + f x] - \right. \right. \\
 & 6 (-1)^{2/3} \sqrt{3} a \sec[e + f x]^{2/3} \sin[e + f x] - \\
 & 60 (-1)^{1/3} a \sec[e + f x]^{4/3} \sin[e + f x] - \\
 & 30 (-1)^{1/3} \sqrt{3} a \sec[e + f x]^{4/3} \sin[e + f x] - \\
 & 6 (-1)^{2/3} b \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} \sin[e + f x] - \\
 & 6 (-1)^{2/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} \sin[e + f x] - \\
 & 60 (-1)^{1/3} b \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{7/3} \sin[e + f x] - \\
 & 30 (-1)^{1/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{7/3} \sin[e + f x] + \\
 & 432 (-1)^{2/3} a \sec[e + f x]^{8/3} \sin[e + f x] + \\
 & 252 (-1)^{2/3} \sqrt{3} a \sec[e + f x]^{8/3} \sin[e + f x] + \\
 & 576 (-1)^{1/3} a \sec[e + f x]^{10/3} \sin[e + f x] + \\
 & \left. \left. 324 (-1)^{1/3} \sqrt{3} a \sec[e + f x]^{10/3} \sin[e + f x] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 432 (-1)^{2/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \\
& 252 (-1)^{2/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \\
& 576 (-1)^{1/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{13/3} \operatorname{Sin}[e + f x] + \\
& 324 (-1)^{1/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{13/3} \operatorname{Sin}[e + f x] - \\
& 846 (-1)^{2/3} a \operatorname{Sec}[e + f x]^{14/3} \operatorname{Sin}[e + f x] - 486 (-1)^{2/3} \sqrt{3} a \operatorname{Sec}[e + f x]^{14/3} \operatorname{Sin}[e + f x] - \\
& 972 (-1)^{1/3} a \operatorname{Sec}[e + f x]^{16/3} \operatorname{Sin}[e + f x] - 558 (-1)^{1/3} \sqrt{3} a \operatorname{Sec}[e + f x]^{16/3} \operatorname{Sin}[e + f x] - \\
& 846 (-1)^{2/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{17/3} \operatorname{Sin}[e + f x] - \\
& 486 (-1)^{2/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{17/3} \operatorname{Sin}[e + f x] - \\
& 972 (-1)^{1/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{19/3} \operatorname{Sin}[e + f x] - \\
& 558 (-1)^{1/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{19/3} \operatorname{Sin}[e + f x] + \\
& 420 (-1)^{2/3} a \operatorname{Sec}[e + f x]^{20/3} \operatorname{Sin}[e + f x] + 240 (-1)^{2/3} \sqrt{3} a \operatorname{Sec}[e + f x]^{20/3} \operatorname{Sin}[e + f x] + \\
& 456 (-1)^{1/3} a \operatorname{Sec}[e + f x]^{22/3} \operatorname{Sin}[e + f x] + 264 (-1)^{1/3} \sqrt{3} a \operatorname{Sec}[e + f x]^{22/3} \operatorname{Sin}[e + f x] + \\
& 420 (-1)^{2/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{23/3} \operatorname{Sin}[e + f x] + \\
& 240 (-1)^{2/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{23/3} \operatorname{Sin}[e + f x] + \\
& 456 (-1)^{1/3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{25/3} \operatorname{Sin}[e + f x] + \\
& 264 (-1)^{1/3} \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^{25/3} \operatorname{Sin}[e + f x] + \\
& b \sqrt{1 - \cos[e + f x]^2} \operatorname{Tan}[e + f x] - 202 a \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x] - \\
& 120 \sqrt{3} a \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x] - 202 b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] - \\
& 120 \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + 609 a \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] + \\
& 360 \sqrt{3} a \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] + 609 b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^4 \operatorname{Tan}[e + f x] + \\
& 360 \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^4 \operatorname{Tan}[e + f x] - 616 a \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] - \\
& 360 \sqrt{3} a \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] - 616 b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^6 \operatorname{Tan}[e + f x] - \\
& 360 \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^6 \operatorname{Tan}[e + f x] + 208 a \operatorname{Sec}[e + f x]^7 \operatorname{Tan}[e + f x] + \\
& 120 \sqrt{3} a \operatorname{Sec}[e + f x]^7 \operatorname{Tan}[e + f x] + 208 b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^8 \operatorname{Tan}[e + f x] + \\
& 120 \sqrt{3} b \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^8 \operatorname{Tan}[e + f x] \Big)
\end{aligned}$$

**Problem 630: Mathematica result simpler than optimal antiderivative, IF it can be verified!**

$$\int \frac{(a + b \operatorname{Tan}[e + f x])^2}{(d \operatorname{Sec}[e + f x])^{1/3}} dx$$

Optimal (type 5, 119 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{15 a b}{2 f (d \operatorname{Sec}[e+f x])^{1/3}} - \\
 & \left( 3 (2 a^2 - 3 b^2) d \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \operatorname{Cos}[e+f x]^2\right] \operatorname{Sin}[e+f x] \right) / \\
 & \left( 8 f (d \operatorname{Sec}[e+f x])^{4/3} \sqrt{\operatorname{Sin}[e+f x]^2} \right) + \frac{3 b (a+b \operatorname{Tan}[e+f x])}{2 f (d \operatorname{Sec}[e+f x])^{1/3}}
 \end{aligned}$$

Result (type 4, 4052 leaves):

$$\begin{aligned}
 & \frac{3 b^2 \operatorname{Cos}[e+f x] \operatorname{Sin}[e+f x] (a+b \operatorname{Tan}[e+f x])^2}{2 f (d \operatorname{Sec}[e+f x])^{1/3} (a \operatorname{Cos}[e+f x] + b \operatorname{Sin}[e+f x])^2} + \\
 & \left( 3 \left( -4 a b \operatorname{Sec}[e+f x] + (2 a^2 - 3 b^2) \sqrt{1 - \operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^2 - \right. \right. \\
 & \quad \frac{1}{6 \sqrt{1 - \operatorname{Cos}[e+f x]^2} \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3} \right)} (2 a^2 - 3 b^2) \\
 & \quad \left. \left( (-1)^{1/3} 3^{1/4} \left( -6 \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] - \right. \right. \right. \\
 & \quad \left. \left. (-3 + \sqrt{3}) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \right) \\
 & \quad \left. \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3} \right)^3 \sqrt{\frac{\left( (-1)^{1/3} + \operatorname{Sec}[e+f x]^{2/3} \right) \operatorname{Sec}[e+f x]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3} \right)^2}} \right. \\
 & \quad \left. \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e+f x]^{2/3} + \operatorname{Sec}[e+f x]^{4/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3} \right)^2}} + \right. \\
 & \quad \left. \left. 6 (1 + \sqrt{3}) \operatorname{Sec}[e+f x]^{2/3} (-1 + \operatorname{Sec}[e+f x]^2) \right) \right) \\
 & (2 a^2 \operatorname{Cos}[e+f x] - 3 b^2 \operatorname{Cos}[e+f x] + 4 a b \operatorname{Sin}[e+f x]) \\
 & \left. \left. \left. (a+b \operatorname{Tan}[e+f x])^2 \right) / 2 \right) \right) \\
 & f \\
 & \operatorname{Sec}[e+f x]^{7/3}
 \end{aligned}$$

$$\begin{aligned}
 & (d \operatorname{Sec}[e + f x])^{1/3} \\
 & (a \operatorname{Cos}[e + f x] + b \operatorname{Sin}[e + f x])^2 \\
 & \left( -\frac{1}{\operatorname{Sec}[e + f x]^{1/3}} 4 \left( -4 a b \operatorname{Sec}[e + f x] + (2 a^2 - 3 b^2) \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^2 - \right. \right. \\
 & \quad \left. \left. \left( 1 / \left( 6 \sqrt{1 - \operatorname{Cos}[e + f x]^2} \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3} \right) \right) \right) (2 a^2 - 3 b^2) \right. \right. \\
 & \quad \left. \left. \left( (-1)^{1/3} 3^{1/4} \left( -6 \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}} \right], \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] - (-3 + \sqrt{3}) \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right) \right) \left( (-1)^{1/3} + \right. \right. \\
 & \quad \left. \left. (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3} \right)^3 \sqrt{\frac{\left( (-1)^{1/3} + \operatorname{Sec}[e + f x]^{2/3} \right) \operatorname{Sec}[e + f x]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3} \right)^2}} \right. \\
 & \quad \left. \sqrt{\left( \left( (-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e + f x]^{2/3} + \operatorname{Sec}[e + f x]^{4/3} \right) / \right. \right. \\
 & \quad \left. \left. \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3} \right)^2 \right) + 6 (1 + \sqrt{3}) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) \left. \right) \operatorname{Sin}[e + f x] + \frac{1}{\operatorname{Sec}[e + f x]^{4/3}} \\
 & 3 \left( 1 / \left( 6 (1 - \operatorname{Cos}[e + f x]^2)^{3/2} \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3} \right) \right) \right) (2 a^2 - 3 b^2) \operatorname{Cos}[ \\
 & e + f x] \left( (-1)^{1/3} 3^{1/4} \left( -6 \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + f x]^{2/3}} \right], \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] - (-3 + \sqrt{3}) \operatorname{EllipticF} \left[ \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \text{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \left( (-1)^{1/3} + \right. \\
 & \left. (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^3 \sqrt{\frac{\left( (-1)^{1/3} + \text{Sec}[e + f x]^{2/3} \right) \text{Sec}[e + f x]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^2}} \\
 & \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \text{Sec}[e + f x]^{2/3} + \text{Sec}[e + f x]^{4/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^2}} + \\
 & \left. 6 (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} (-1 + \text{Sec}[e + f x]^2) \right) \text{Sin}[e + f x] + \\
 & \left( \frac{1}{9 \sqrt{1 - \text{Cos}[e + f x]^2}} \left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^2 \right) \\
 & (1 + \sqrt{3}) (2 a^2 - 3 b^2) \text{Sec}[e + f x]^{5/3} \\
 & \left( (-1)^{1/3} 3^{1/4} \left( -6 \text{EllipticE} \left[ \text{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}} \right], \right. \right. \right. \\
 & \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] - (-3 + \sqrt{3}) \text{EllipticF} \left[ \right. \right. \\
 & \left. \left. \text{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right) \left( (-1)^{1/3} + \right. \\
 & \left. (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^3 \sqrt{\frac{\left( (-1)^{1/3} + \text{Sec}[e + f x]^{2/3} \right) \text{Sec}[e + f x]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^2}} \\
 & \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \text{Sec}[e + f x]^{2/3} + \text{Sec}[e + f x]^{4/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)^2}} + \\
 & \left. 6 (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} (-1 + \text{Sec}[e + f x]^2) \right) \text{Sin}[e + f x] - \\
 & \frac{1}{6 \sqrt{1 - \text{Cos}[e + f x]^2} \left( (-1)^{1/3} + (1 + \sqrt{3}) \text{Sec}[e + f x]^{2/3} \right)}
 \end{aligned}$$

$$\begin{aligned}
 & (2a^2 - 3b^2) \left( 12(1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{11/3} \operatorname{Sin}[e + fx] + 2(-1)^{1/3} 3^{1/4} (1 + \sqrt{3}) \right. \\
 & \left. \left( -6 \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] - \right. \right. \\
 & \left. \left. (-3 + \sqrt{3}) \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] \right) \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^2 \right. \\
 & \sqrt{\frac{\left( (-1)^{1/3} + \operatorname{Sec}[e + fx]^{2/3} \right) \operatorname{Sec}[e + fx]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^2}} \operatorname{Sec}[e + fx]^{5/3}} \\
 & \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e + fx]^{2/3} + \operatorname{Sec}[e + fx]^{4/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^2}} \operatorname{Sin}[e + fx] + } \\
 & 4(1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{5/3} (-1 + \operatorname{Sec}[e + fx]^2) \operatorname{Sin}[e + fx] + \\
 & \frac{1}{2 \sqrt{\frac{(-1)^{1/3} + \operatorname{Sec}[e + fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}}}} (-1)^{1/3} 3^{1/4} \left( -6 \operatorname{EllipticE} \left[ \right. \right. \\
 & \left. \left. \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] - (-3 + \sqrt{3}) \right. \right. \\
 & \left. \left. \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right) \right) \\
 & \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^3 \sqrt{\left( \left( (-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e + fx]^{2/3} + \operatorname{Sec}[e + fx]^{4/3} \right) / \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^2 \right)} \\
 & \left( 2 \left( (-1)^{1/3} + \operatorname{Sec}[e + fx]^{2/3} \right) \operatorname{Sec}[e + fx]^{5/3} \operatorname{Sin}[e + fx] \right) / \left( 3 \left( (-1)^{1/3} + \right. \right. \\
 & \left. \left. (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^2 \right) - 4(1 + \sqrt{3}) \left( (-1)^{1/3} + \operatorname{Sec}[e + fx]^{2/3} \right) \\
 & \left. \operatorname{Sec}[e + fx]^{7/3} \operatorname{Sin}[e + fx] \right) / \left( 3 \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e + fx]^{2/3} \right)^3 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2 \operatorname{Sec}[e+fx]^{7/3} \operatorname{Sin}[e+fx]}{3 \left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2} \Bigg) + (-1)^{1/3} 3^{1/4} \left( (-1)^{1/3} + \right. \\
 & \left. (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^3 \sqrt{\frac{\left( (-1)^{1/3} + \operatorname{Sec}[e+fx]^{2/3} \right) \operatorname{Sec}[e+fx]^{2/3}}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}} \\
 & \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e+fx]^{2/3} + \operatorname{Sec}[e+fx]^{4/3}}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}} \left( \left( (-3+\sqrt{3}) \right. \right. \\
 & \left. \left. - \left( (2(1+\sqrt{3}) \left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right) \operatorname{Sec}[e+fx]^{5/3} \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sin}[e+fx] \right) / \left( 3 \left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2 \right) \right) - \right. \\
 & \left. \left. \frac{2(-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{5/3} \operatorname{Sin}[e+fx]}{3 \left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)} \right) \right) / \\
 & \left( \sqrt{\left( 1 - \frac{1}{4} (2+\sqrt{3}) \left( 1 - \frac{\left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2} \right) \right)} \right) \\
 & \sqrt{\frac{\left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}} + \\
 & \left( 6 \sqrt{\left( 1 - \frac{1}{4} (2+\sqrt{3}) \left( 1 - \frac{\left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2} \right) \right)} \right) \\
 & \left( - \left( (2(1+\sqrt{3}) \left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right) \operatorname{Sec}[e+fx]^{5/3} \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sin}[e+fx] \right) / \left( 3 \left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2 \right) \right) - \right. \\
 & \left. \left. \frac{2(-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{5/3} \operatorname{Sin}[e+fx]}{3 \left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)} \right) \right) / \\
 & \left( \sqrt{\frac{\left( (-1)^{1/3} - (-1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}{\left( (-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2 \sqrt{\frac{(-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e+fx]^{2/3} + \operatorname{Sec}[e+fx]^{4/3}}{((-1)^{1/3} + (1+\sqrt{3}) \operatorname{Sec}[e+fx]^{2/3})^2}}} (-1)^{1/3} 3^{1/4} \\
 & \left( -6 \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] - \right. \\
 & \quad \left. (-3 + \sqrt{3}) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{(-1)^{1/3} - (-1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3}}{(-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3}}\right], \right. \right. \\
 & \quad \left. \left. \frac{1}{4} (2 + \sqrt{3})\right] \right) \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^3 \\
 & \sqrt{\frac{\left( (-1)^{1/3} + \operatorname{Sec}[e+fx]^{2/3} \right) \operatorname{Sec}[e+fx]^{2/3}}{\left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2}} \left( - \left( 4 (1 + \sqrt{3}) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+fx]^{5/3} \left( (-1)^{2/3} - (-1)^{1/3} \operatorname{Sec}[e+fx]^{2/3} + \operatorname{Sec}[e+fx]^{4/3} \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sin}[e+fx] \right) / \left( 3 \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^3 \right) \right) + \\
 & \quad \left( -\frac{2}{3} (-1)^{1/3} \operatorname{Sec}[e+fx]^{5/3} \operatorname{Sin}[e+fx] + \frac{4}{3} \operatorname{Sec}[e+fx]^{7/3} \operatorname{Sin}[e+fx] \right) / \\
 & \quad \left. \left( (-1)^{1/3} + (1 + \sqrt{3}) \operatorname{Sec}[e+fx]^{2/3} \right)^2 \right) + \\
 & \left. \left. \left. \left. \left. \frac{(2a^2 - 3b^2) \operatorname{Tan}[e+fx]}{\sqrt{1 - \operatorname{Cos}[e+fx]^2}} - 4ab \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx] + 2(2a^2 - 3b^2) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \right. \right. \right. \right. \right.
 \end{aligned}$$

**Problem 632: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(d \operatorname{Sec}[e+fx])^{5/3}}{a + b \operatorname{Tan}[e+fx]} dx$$

Optimal (type 6, 552 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2b^{1/3}(\operatorname{Sec}[e+fx]^2)^{1/6}}{\sqrt{3}(a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{5/3}}{2b^{2/3}(a^2+b^2)^{1/6}f(\operatorname{Sec}[e+fx]^2)^{5/6}} + \\
 & \frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2b^{1/3}(\operatorname{Sec}[e+fx]^2)^{1/6}}{\sqrt{3}(a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{5/3}}{2b^{2/3}(a^2+b^2)^{1/6}f(\operatorname{Sec}[e+fx]^2)^{5/6}} - \\
 & \frac{\operatorname{ArcTanh}\left[\frac{b^{1/3}(\operatorname{Sec}[e+fx]^2)^{1/6}}{(a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{5/3}}{b^{2/3}(a^2+b^2)^{1/6}f(\operatorname{Sec}[e+fx]^2)^{5/6}} + \\
 & \left(\operatorname{Log}\left[(a^2+b^2)^{1/3} - b^{1/3}(a^2+b^2)^{1/6}(\operatorname{Sec}[e+fx]^2)^{1/6} + b^{2/3}(\operatorname{Sec}[e+fx]^2)^{1/3}\right] (d \operatorname{Sec}[e+fx])^{5/3}\right) / \\
 & \left(4b^{2/3}(a^2+b^2)^{1/6}f(\operatorname{Sec}[e+fx]^2)^{5/6}\right) - \\
 & \left(\operatorname{Log}\left[(a^2+b^2)^{1/3} + b^{1/3}(a^2+b^2)^{1/6}(\operatorname{Sec}[e+fx]^2)^{1/6} + b^{2/3}(\operatorname{Sec}[e+fx]^2)^{1/3}\right] (d \operatorname{Sec}[e+fx])^{5/3}\right) / \\
 & \left(4b^{2/3}(a^2+b^2)^{1/6}f(\operatorname{Sec}[e+fx]^2)^{5/6}\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, 1, \frac{1}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e+fx]^2}{a^2}, -\operatorname{Tan}[e+fx]^2\right] (d \operatorname{Sec}[e+fx])^{5/3} \operatorname{Tan}[e+fx]\right) / \\
 & \left(a f (\operatorname{Sec}[e+fx]^2)^{5/6}\right)
 \end{aligned}$$

Result (type 6, 276 leaves):

$$\begin{aligned}
 & - \left( \left( 24 d^2 \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{6}, \frac{1}{6}, \frac{4}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] (a+b \operatorname{Tan}[e+fx]) \right) / \left( b f \right. \right. \\
 & \left. \left. (d \operatorname{Sec}[e+fx])^{1/3} \left( (a+ib) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{1}{6}, \frac{7}{6}, \frac{7}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] + \right. \right. \right. \\
 & \left. \left. (a-ib) \operatorname{AppellF1}\left[\frac{4}{3}, \frac{7}{6}, \frac{1}{6}, \frac{7}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] + \right. \right. \\
 & \left. \left. \left. 8 \operatorname{AppellF1}\left[\frac{1}{3}, \frac{1}{6}, \frac{1}{6}, \frac{4}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] (a+b \operatorname{Tan}[e+fx]) \right) \right) \right)
 \end{aligned}$$

**Problem 633: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(d \operatorname{Sec}[e+fx])^{1/3}}{a+b \operatorname{Tan}[e+fx]} dx$$

Optimal (type 6, 552 leaves, 16 steps):

$$\frac{\sqrt{3} b^{2/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2b^{1/3} (\operatorname{Sec}[e+fx]^2)^{1/6}}{\sqrt{3} (a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{1/3}}{2 (a^2+b^2)^{5/6} f (\operatorname{Sec}[e+fx]^2)^{1/6}} -$$

$$\frac{\sqrt{3} b^{2/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2b^{1/3} (\operatorname{Sec}[e+fx]^2)^{1/6}}{\sqrt{3} (a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{1/3}}{2 (a^2+b^2)^{5/6} f (\operatorname{Sec}[e+fx]^2)^{1/6}} -$$

$$\frac{b^{2/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e+fx]^2)^{1/6}}{(a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+fx])^{1/3}}{(a^2+b^2)^{5/6} f (\operatorname{Sec}[e+fx]^2)^{1/6}} +$$

$$\left(b^{2/3} \operatorname{Log}\left[(a^2+b^2)^{1/3} - b^{1/3} (a^2+b^2)^{1/6} (\operatorname{Sec}[e+fx]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e+fx]^2)^{1/3}\right] (d \operatorname{Sec}[e+fx])^{1/3}\right) / \left(4 (a^2+b^2)^{5/6} f (\operatorname{Sec}[e+fx]^2)^{1/6}\right) -$$

$$\left(b^{2/3} \operatorname{Log}\left[(a^2+b^2)^{1/3} + b^{1/3} (a^2+b^2)^{1/6} (\operatorname{Sec}[e+fx]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e+fx]^2)^{1/3}\right] (d \operatorname{Sec}[e+fx])^{1/3}\right) / \left(4 (a^2+b^2)^{5/6} f (\operatorname{Sec}[e+fx]^2)^{1/6}\right) +$$

$$\left(\operatorname{AppellF1}\left[\frac{1}{2}, 1, \frac{5}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e+fx]^2}{a^2}, -\operatorname{Tan}[e+fx]^2\right] (d \operatorname{Sec}[e+fx])^{1/3} \operatorname{Tan}[e+fx]\right) / \left(a f (\operatorname{Sec}[e+fx]^2)^{1/6}\right)$$

Result (type 6, 280 leaves):

$$-\left(\left(48 d^2 \operatorname{AppellF1}\left[\frac{5}{3}, \frac{5}{6}, \frac{5}{6}, \frac{8}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] (a+b \operatorname{Tan}[e+fx])\right) / \left(5 b f (d \operatorname{Sec}[e+fx])^{5/3}\right) + \right.$$

$$\left(5 (a+ib) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{5}{6}, \frac{11}{6}, \frac{11}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] + \right.$$

$$\left.5 (a-ib) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{11}{6}, \frac{5}{6}, \frac{11}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] + \right.$$

$$\left.16 \operatorname{AppellF1}\left[\frac{5}{3}, \frac{5}{6}, \frac{5}{6}, \frac{8}{3}, \frac{a-ib}{a+b \operatorname{Tan}[e+fx]}, \frac{a+ib}{a+b \operatorname{Tan}[e+fx]}\right] (a+b \operatorname{Tan}[e+fx])\right) \Bigg)$$

**Problem 634: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{1}{(d \operatorname{Sec}[e+fx])^{1/3} (a+b \operatorname{Tan}[e+fx])} dx$$

Optimal (type 6, 579 leaves, 17 steps):

$$\begin{aligned}
 & \frac{3b}{(a^2 + b^2) f (d \operatorname{Sec}[e + f x])^{1/3}} - \frac{\sqrt{3} b^{4/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{2 (a^2 + b^2)^{7/6} f (d \operatorname{Sec}[e + f x])^{1/3}} + \\
 & \frac{\sqrt{3} b^{4/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{2 (a^2 + b^2)^{7/6} f (d \operatorname{Sec}[e + f x])^{1/3}} - \\
 & \frac{b^{4/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{7/6} f (d \operatorname{Sec}[e + f x])^{1/3}} + \\
 & \left( b^{4/3} \operatorname{Log}\left[\left(a^2 + b^2\right)^{1/3} - b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{1/6} \right) / \left( 4 (a^2 + b^2)^{7/6} f (d \operatorname{Sec}[e + f x])^{1/3} \right) - \\
 & \left( b^{4/3} \operatorname{Log}\left[\left(a^2 + b^2\right)^{1/3} + b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{1/6} \right) / \left( 4 (a^2 + b^2)^{7/6} f (d \operatorname{Sec}[e + f x])^{1/3} \right) + \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1, \frac{7}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2\right] (\operatorname{Sec}[e + f x]^2)^{1/6} \operatorname{Tan}[e + f x] \right) / \\
 & \left( a f (d \operatorname{Sec}[e + f x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 285 leaves):

$$\begin{aligned}
 & - \left( \left( 60 d \operatorname{AppellF1}\left[\frac{7}{3}, \frac{7}{6}, \frac{7}{6}, \frac{10}{3}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \right. \right. \\
 & \quad \left. \left. (a \operatorname{Cos}[e + f x] + b \operatorname{Sin}[e + f x]) \right) \right) / \left( 7 b f (d \operatorname{Sec}[e + f x])^{4/3} \right) \\
 & \left( 7 (a + i b) \operatorname{AppellF1}\left[\frac{10}{3}, \frac{7}{6}, \frac{13}{6}, \frac{13}{3}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] + \right. \\
 & \quad \left. 7 (a - i b) \operatorname{AppellF1}\left[\frac{10}{3}, \frac{13}{6}, \frac{7}{6}, \frac{13}{3}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] + \right. \\
 & \quad \left. \left. 20 \operatorname{AppellF1}\left[\frac{7}{3}, \frac{7}{6}, \frac{7}{6}, \frac{10}{3}, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] (a + b \operatorname{Tan}[e + f x]) \right) \right)
 \end{aligned}$$

**Problem 635: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e + f x])^{5/3} (a + b \operatorname{Tan}[e + f x])} dx$$

Optimal (type 6, 581 leaves, 17 steps):

$$\frac{3 b}{5 (a^2 + b^2) f (d \operatorname{Sec}[e + f x])^{5/3}} + \frac{\sqrt{3} b^{8/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{2 (a^2 + b^2)^{11/6} f (d \operatorname{Sec}[e + f x])^{5/3}} -$$

$$\frac{\sqrt{3} b^{8/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{2 (a^2 + b^2)^{11/6} f (d \operatorname{Sec}[e + f x])^{5/3}} -$$

$$\frac{b^{8/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{(a^2 + b^2)^{11/6} f (d \operatorname{Sec}[e + f x])^{5/3}} +$$

$$\left( b^{8/3} \operatorname{Log}\left[ (a^2 + b^2)^{1/3} - b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3} \right] \right. \\ \left. (\operatorname{Sec}[e + f x]^2)^{5/6} \right) / \left( 4 (a^2 + b^2)^{11/6} f (d \operatorname{Sec}[e + f x])^{5/3} \right) -$$

$$\left( b^{8/3} \operatorname{Log}\left[ (a^2 + b^2)^{1/3} + b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3} \right] \right. \\ \left. (\operatorname{Sec}[e + f x]^2)^{5/6} \right) / \left( 4 (a^2 + b^2)^{11/6} f (d \operatorname{Sec}[e + f x])^{5/3} \right) +$$

$$\left( \operatorname{AppellF1}\left[ \frac{1}{2}, 1, \frac{11}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2 \right] (\operatorname{Sec}[e + f x]^2)^{5/6} \operatorname{Tan}[e + f x] \right) /$$

$$\left( a f (d \operatorname{Sec}[e + f x])^{5/3} \right)$$

Result (type 6, 18391 leaves):

$$\left( \frac{3 \left( b + a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x] \right)}{5 (a^2 + b^2) \operatorname{Sec}[e + f x]^{5/3}} \right) +$$

$$3 \left( \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan}\left[ \frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \right. \\ \left. \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) \right) /$$

$$\left( 6 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) +$$

$$\left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan}\left[ \frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\ \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) /$$

$$\left( 6 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) +$$

$$\left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan}\left[ \frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\ \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) /$$



$$\begin{aligned}
 & \left( 3 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \log \left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \sec[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \sec[e + f x]^{2/3} \right] \sec[e + f x]^2 \right. \\
 & \quad \left. \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \right) / \left( 4 \sqrt{3} \right. \\
 & \quad \left. (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \log \left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \sec[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \sec[e + f x]^{2/3} \right] \sec[e + f x]^2 \right. \\
 & \quad \left. \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \right) / \left( 4 \sqrt{3} \right. \\
 & \quad \left. (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) - \\
 & \left( 14 a^3 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \left. \sec[e + f x]^{10/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right. \\
 & \quad \left. \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \right) / \\
 & \left( 5 (-1 + \sec[e + f x]^2) \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \right) \right. \\
 & \quad \left. \left( -a^2 + b^2 (-1 + \sec[e + f x]^2) \right) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + \right. \right. \\
 & \quad \left. \left. b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) - \\
 & \left( 49 a b^2 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \sec[e + f x]^{10/3} \right. \\
 & \quad \left. \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right. \\
 & \quad \left. \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \right) / \\
 & \left( 5 (-1 + \sec[e + f x]^2) \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \right) \right. \\
 & \quad \left. \left( -a^2 + b^2 (-1 + \sec[e + f x]^2) \right) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + \right. \right. \\
 & \quad \left. \left. b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) -
 \end{aligned}$$



$$\begin{aligned}
 & \left( 9 (a^2 + b^2)^2 \left( 1 + \frac{(\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3})^2}{(a^2 + b^2)^{1/3}} \right) \right. \\
 & \quad \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( b^3 \operatorname{Sec}[e + f x]^{10/3} \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \right. \right. \\
 & \quad \left. \left. \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \operatorname{Sin}[e + f x] \right) / \\
 & \left( 9 (a^2 + b^2)^2 \left( 1 + \frac{(-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3}}{(a^2 + b^2)^{1/3}} \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( 28 a^3 b^2 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^{19/3} \right. \\
 & \quad \left. \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \right. \right. \\
 & \quad \left. \left. \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \operatorname{Sin}[e + f x] \right) / \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \\
 & \quad \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left. \right) + \\
 & \left( 98 a b^4 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^{19/3} \right. \\
 & \quad \left. \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \right. \right. \\
 & \quad \left. \left. \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \operatorname{Sin}[e + f x] \right) / \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. b \operatorname{Sec}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \right) - \right. \\
 & \left( 52 a b^4 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \operatorname{Sec}[e+fx]^{25/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \left( -b + b \operatorname{Sec}[e+fx]^2 + a \operatorname{Sec}[e+fx] \right. \\
 & \quad \left. \left. \left. \left. \left. \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \operatorname{Sin}[e+fx] \right) \right) \right] \left. \right) / \left( 35 (-1 + \operatorname{Sec}[e+fx]^2)^2 \right. \\
 & \quad \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+fx]^2 \right) \\
 & \quad \left. \left. \left. \left. \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e+fx]^2))^2 \left( a \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. b \operatorname{Sec}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \right) \right) \right) + \right. \\
 & \left( 28 a^3 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \operatorname{Sec}[e+fx]^{19/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \left( -b + b \operatorname{Sec}[e+fx]^2 + a \operatorname{Sec}[e+fx] \right. \\
 & \quad \left. \left. \left. \left. \left. \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \operatorname{Sin}[e+fx] \right) \right) \right] \left. \right) / \left( 5 (-1 + \operatorname{Sec}[e+fx]^2)^2 \right) \\
 & \quad \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+fx]^2 \right) \\
 & \quad \left. \left. \left. \left. \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e+fx]^2)) \left( a \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. b \operatorname{Sec}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \right) \right) \right) + \right. \\
 & \left( 98 a b^2 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \operatorname{Sec}[e+fx]^{19/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \left( -b + b \operatorname{Sec}[e+fx]^2 + a \operatorname{Sec}[e+fx] \right. \\
 & \quad \left. \left. \left. \left. \left. \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \operatorname{Sin}[e+fx] \right) \right) \right] \left. \right) / \left( 5 (-1 + \operatorname{Sec}[e+fx]^2)^2 \right) \\
 & \quad \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2 + b^2) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \text{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \text{Sec}[e+fx]^2 \right) \right. \\
 & \left. \left( -a^2 + b^2 (-1 + \text{Sec}[e+fx]^2) \right) \left( a \sqrt{1 - \text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 + \right. \right. \\
 & \left. \left. b \text{Sec}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2) \right) \right) - \\
 & \left( 28 a^3 \text{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \text{Sec}[e+fx]^{13/3} \right. \\
 & \left. \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \left( -b + b \text{Sec}[e+fx]^2 + a \text{Sec}[e+fx] \right. \right. \\
 & \left. \left. \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \right) \text{Sin}[e+fx] \right) / \left( 3 (-1 + \text{Sec}[e+fx]^2) \right) \\
 & \left( 7 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \text{Sec}[e+fx]^2 \right) \\
 & \left. \left( -a^2 + b^2 (-1 + \text{Sec}[e+fx]^2) \right) \left( a \sqrt{1 - \text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 + \right. \right. \\
 & \left. \left. b \text{Sec}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2) \right) \right) \right) - \\
 & \left( 98 a b^2 \text{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \\
 & \left. \text{Sec}[e+fx]^{13/3} \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \right. \\
 & \left. \left( -b + b \text{Sec}[e+fx]^2 + a \text{Sec}[e+fx] \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \right) \right. \\
 & \left. \text{Sin}[e+fx] \right) / \left( 3 (-1 + \text{Sec}[e+fx]^2) \right) \\
 & \left( 7 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \text{Sec}[e+fx]^2 \right) \\
 & \left. \left( -a^2 + b^2 (-1 + \text{Sec}[e+fx]^2) \right) \left( a \sqrt{1 - \text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 + \right. \right. \\
 & \left. \left. b \text{Sec}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2) \right) \right) \right) - \\
 & \left( 52 a b^2 \text{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \\
 & \left. \text{Sec}[e+fx]^{25/3} \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \right. \\
 & \left. \left( -b + b \text{Sec}[e+fx]^2 + a \text{Sec}[e+fx] \sqrt{\text{Cos}[e+fx]^2 (-1 + \text{Sec}[e+fx]^2)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sin[e + f x] \right) / \left( 35 (-1 + \sec[e + f x]^2)^2 \right. \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \right) \\
 & (-a^2 + b^2 (-1 + \sec[e + f x]^2)) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + \right. \\
 & \quad \left. b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \left. \right) + \\
 & \left( 416 a b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \left. \sec[e + f x]^{19/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right. \\
 & \left. (-b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)}) \right) \\
 & \left. \sin[e + f x] \right) / \left( 105 (-1 + \sec[e + f x]^2) \right. \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \right) \\
 & (-a^2 + b^2 (-1 + \sec[e + f x]^2)) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + \right. \\
 & \quad \left. b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \left. \right) - \left( (-1)^{5/6} b^{8/3} \sec[e + f x]^2 \right. \\
 & \left. (-b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)}) \right) \\
 & \left( -\frac{(-1)^{1/6} b^{1/3} (a^2 + b^2)^{1/6} \sec[e + f x]^{4/3} \sin[e + f x]}{\sqrt{3}} + \right. \\
 & \quad \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \sec[e + f x]^{5/3} \sin[e + f x] \right) \left. \right) / \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \sec[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \sec[e + f x]^{2/3} \right) \right. \\
 & \left. \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^3 + b \sec[e + f x]^2 (-1 + \sec[e + f x]^2) \right) \right) \left. \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \sec[e + f x]^2 (-b + b \sec[e + f x]^2 + a \sec[e + f x] \right. \\
 & \quad \left. \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)}) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{(-1)^{1/6} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{4/3} \operatorname{Sin}[e + f x]}{\sqrt{3}} + \right. \\
 & \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{5/3} \operatorname{Sin}[e + f x] \right) / \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right) \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \operatorname{Tan}[e + f x] \right) / \left( 3 (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \operatorname{Tan}[e + f x] \right) / \left( 3 (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( 2 (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \operatorname{Tan}[e + f x] \right) / \left( 3 (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{Log} \left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \operatorname{Tan}[e + f x] \right) / \left( 2 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{Log} \left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \operatorname{Tan}[e + f x] \Big/ \left( 2 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( 7 a^3 \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \operatorname{Sec}[e + f x]^{10/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \left( -2 \operatorname{Cos}[e + f x] (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] + 2 \operatorname{Tan}[e + f x] \right) \right) \Big/ \\
 & \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right. \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \right. \\
 & \left. \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) \Big/ \\
 & \left( 49 a b^2 \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \operatorname{Sec}[e + f x]^{10/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \left( -2 \operatorname{Cos}[e + f x] (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] + 2 \operatorname{Tan}[e + f x] \right) \right) \Big/ \\
 & \left( 10 (-1 + \operatorname{Sec}[e + f x]^2) \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right. \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \right. \\
 & \left. \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) \Big/ + \\
 & \left( 13 a b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \operatorname{Sec}[e + f x]^{16/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left( -2 \cos [e+f x] (-1+\sec [e+f x]^2) \sin [e+f x]+2 \tan [e+f x] \right) \right) / \\
 & \left( 35 (-1+\sec [e+f x]^2) \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right. \\
 & \left( 13 \left( a^2+b^2 \right) \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right]+ \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right]+ \left( a^2+b^2 \right) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \right) \sec [e+f x]^2 \right) \\
 & \left. \left( -a^2+b^2 (-1+\sec [e+f x]^2) \right) \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^3+ \right. \right. \\
 & \left. \left. b \sec [e+f x]^2 (-1+\sec [e+f x]^2) \right) \right) \left. \right) - \\
 & \left( 14 a^3 \sec [e+f x]^{10/3} \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right. \\
 & \left( -b+b \sec [e+f x]^2+a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \\
 & \left( \frac{1}{7 \left( a^2+b^2 \right)} 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \sec [e+f x]^2 \right. \\
 & \left. \tan [e+f x]+ \frac{1}{7} \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \right. \\
 & \left. \left. \sec [e+f x]^2 \tan [e+f x] \right) \right) / \left( 5 (-1+\sec [e+f x]^2) \right) \\
 & \left( 7 \left( a^2+b^2 \right) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right]+ \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right]+ \left( a^2+b^2 \right) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \right) \sec [e+f x]^2 \right) \\
 & \left. \left( -a^2+b^2 (-1+\sec [e+f x]^2) \right) \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^3+ \right. \right. \\
 & \left. \left. b \sec [e+f x]^2 (-1+\sec [e+f x]^2) \right) \right) \left. \right) - \\
 & \left( 49 a b^2 \sec [e+f x]^{10/3} \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right. \\
 & \left( -b+b \sec [e+f x]^2+a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \\
 & \left( \frac{1}{7 \left( a^2+b^2 \right)} 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \sec [e+f x]^2 \right. \\
 & \left. \tan [e+f x]+ \frac{1}{7} \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2}\right] \right. \\
 & \left. \left. \sec [e+f x]^2 \tan [e+f x] \right) \right) / \left( 5 (-1+\sec [e+f x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \\
 & \quad \quad \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \Big) \\
 & \quad \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \\
 & \quad \quad \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \Big) + \\
 & \left( 26 a b^2 \operatorname{Sec}[e + f x]^{16/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right. \\
 & \quad \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \quad \left( \frac{1}{13 (a^2 + b^2)} 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \quad \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \right. \\
 & \quad \quad \quad \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \Big) \Big) / \left( 35 (-1 + \operatorname{Sec}[e + f x]^2) \right. \\
 & \quad \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \\
 & \quad \quad \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \Big) \\
 & \quad \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \\
 & \quad \quad \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \Big) - \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \quad \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \quad \left( \frac{a \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + 3 a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] + \right. \\
 & \quad \quad \left. 2 b \operatorname{Sec}[e + f x]^4 \operatorname{Tan}[e + f x] + 2 b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Tan}[e + f x] \right) \Big) \Big) / \\
 & \left( 6 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( -1 + \sec [e + f x]^2 \right)^2 \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \sec [e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \sec [e + f x]^2 \right. \\
 & \left( -b + b \sec [e + f x]^2 + a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \\
 & \left( \frac{a \sec [e + f x] \tan [e + f x]}{\sqrt{1 - \cos [e + f x]^2}} + 3 a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^3 \tan [e + f x] + \right. \\
 & \left. \left. 2 b \sec [e + f x]^4 \tan [e + f x] + 2 b \sec [e + f x]^2 (-1 + \sec [e + f x]^2) \tan [e + f x] \right) \right) / \\
 & \left( 6 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^3 + b \sec [e + f x]^2 \right. \right. \\
 & \left. \left. (-1 + \sec [e + f x]^2) \right)^2 \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{ArcTan} \left[ \frac{(-1)^{1/6} b^{1/3} \sec [e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \sec [e + f x]^2 \right. \\
 & \left( -b + b \sec [e + f x]^2 + a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \\
 & \left( \frac{a \sec [e + f x] \tan [e + f x]}{\sqrt{1 - \cos [e + f x]^2}} + 3 a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^3 \tan [e + f x] + \right. \\
 & \left. \left. 2 b \sec [e + f x]^4 \tan [e + f x] + 2 b \sec [e + f x]^2 (-1 + \sec [e + f x]^2) \tan [e + f x] \right) \right) / \\
 & \left( 3 (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^3 + b \sec [e + f x]^2 \right. \right. \\
 & \left. \left. (-1 + \sec [e + f x]^2) \right)^2 \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{Log} \left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \sec [e + f x]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \sec [e + f x]^{2/3} \right] \sec [e + f x]^2 \right. \\
 & \left( -b + b \sec [e + f x]^2 + a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \\
 & \left( \frac{a \sec [e + f x] \tan [e + f x]}{\sqrt{1 - \cos [e + f x]^2}} + 3 a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^3 \tan [e + f x] + \right. \\
 & \left. \left. 2 b \sec [e + f x]^4 \tan [e + f x] + 2 b \sec [e + f x]^2 (-1 + \sec [e + f x]^2) \tan [e + f x] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos [e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 \right. \right. \\
 & \quad \left. \left. (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \operatorname{Log} \left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \quad (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sec}[e + f x]^2 \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\cos [e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) \\
 & \left( \frac{a \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x]}{\sqrt{1 - \cos [e + f x]^2}} + 3 a \sqrt{1 - \cos [e + f x]^2} \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] + \right. \\
 & \quad \left. 2 b \operatorname{Sec}[e + f x]^4 \operatorname{Tan}[e + f x] + 2 b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Tan}[e + f x] \right) \Bigg) / \\
 & \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \left( a \sqrt{1 - \cos [e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 \right. \right. \\
 & \quad \left. \left. (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) + \\
 & \left( 14 a^3 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^{10/3} \right. \\
 & \quad \sqrt{\cos [e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\cos [e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) \\
 & \left( \frac{a \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x]}{\sqrt{1 - \cos [e + f x]^2}} + 3 a \sqrt{1 - \cos [e + f x]^2} \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] + \right. \\
 & \quad \left. 2 b \operatorname{Sec}[e + f x]^4 \operatorname{Tan}[e + f x] + 2 b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Tan}[e + f x] \right) \Bigg) / \\
 & \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) \\
 & \left( a \sqrt{1 - \cos [e + f x]^2} \operatorname{Sec}[e + f x]^3 + b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \Bigg) + \\
 & \left( 49 a^2 b^2 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Sec}[e + f x]^{10/3} \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \\
 & \left( -b + b \text{Sec}[e + f x]^2 + a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{a \text{Sec}[e + f x] \text{Tan}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} + 3 a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 \text{Tan}[e + f x] + \right. \\
 & \left. 2 b \text{Sec}[e + f x]^4 \text{Tan}[e + f x] + 2 b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \text{Tan}[e + f x] \right) \Bigg) / \\
 & \left( 5 (-1 + \text{Sec}[e + f x]^2) \left( 7 (a^2 + b^2) \text{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \text{Sec}[e + f x]^2 (-a^2 + b^2 (-1 + \text{Sec}[e + f x]^2)) \right) \\
 & \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( 26 a b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \left. \begin{aligned}
 & \text{Sec}[e + f x]^{16/3} \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \\
 & \left( -b + b \text{Sec}[e + f x]^2 + a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{a \text{Sec}[e + f x] \text{Tan}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} + 3 a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 \text{Tan}[e + f x] + \right. \\
 & \left. 2 b \text{Sec}[e + f x]^4 \text{Tan}[e + f x] + 2 b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \text{Tan}[e + f x] \right) \Bigg) / \\
 & \left( 35 (-1 + \text{Sec}[e + f x]^2) \left( 13 (a^2 + b^2) \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \text{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \text{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \text{Sec}[e + f x]^2 (-a^2 + b^2 (-1 + \text{Sec}[e + f x]^2)) \right) \\
 & \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right)^2 \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \text{ArcTan}\left[\frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \text{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \right)
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}[e + f x]^2 \left( 2 b \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \right. \\
 & \quad \left. a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \text{Tan}[e + f x] + \right. \\
 & \quad \left. (a \text{Sec}[e + f x] (-2 \text{Cos}[e + f x] (-1 + \text{Sec}[e + f x]^2) \text{Sin}[e + f x] + 2 \text{Tan}[e + f x])) \right) / \\
 & \quad \left( 2 \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \Bigg) / \left( 6 (a^2 + b^2)^{11/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \text{ArcTan} \left[ \frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \text{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \right. \\
 & \quad \text{Sec}[e + f x]^2 \left( 2 b \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \right. \\
 & \quad \left. a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \text{Tan}[e + f x] + \right. \\
 & \quad \left. (a \text{Sec}[e + f x] (-2 \text{Cos}[e + f x] (-1 + \text{Sec}[e + f x]^2) \text{Sin}[e + f x] + 2 \text{Tan}[e + f x])) \right) / \\
 & \quad \left( 2 \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \Bigg) / \left( 6 (a^2 + b^2)^{11/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \text{ArcTan} \left[ \frac{(-1)^{1/6} b^{1/3} \text{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \text{Sec}[e + f x]^2 \right. \\
 & \quad \left( 2 b \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right. \\
 & \quad \left. \text{Tan}[e + f x] + (a \text{Sec}[e + f x] (-2 \text{Cos}[e + f x] (-1 + \text{Sec}[e + f x]^2) \text{Sin}[e + f x] + \right. \\
 & \quad \left. 2 \text{Tan}[e + f x])) \right) / \left( 2 \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \Bigg) / \left( 3 (a^2 + b^2)^{11/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{5/6} b^{8/3} \text{Log} \left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \text{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \text{Sec}[e + f x]^{2/3} \right] \text{Sec}[e + f x]^2 \left( 2 b \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \right. \right. \\
 & \quad \left. \left. a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \text{Tan}[e + f x] + \right. \right. \\
 & \quad \left. \left. (a \text{Sec}[e + f x] (-2 \text{Cos}[e + f x] (-1 + \text{Sec}[e + f x]^2) \text{Sin}[e + f x] + 2 \text{Tan}[e + f x])) \right) \right) / \\
 & \quad \left( 2 \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \Bigg) / \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{5/6} b^{8/3} \text{Log} \left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \text{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \text{Sec}[e + f x]^{2/3} \right] \text{Sec}[e + f x]^2 \left( 2 b \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \right. \right. \\
 & \quad \left. \left. a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \text{Tan}[e + f x] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sec[e+fx] \left( -2 \cos[e+fx] \left( -1 + \sec[e+fx]^2 \right) \sin[e+fx] + 2 \tan[e+fx] \right) \right) / \\
 & \left( 2 \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \right) \Bigg) / \left( 4 \sqrt{3} (a^2 + b^2)^{11/6} \right. \\
 & \left. \left( a \sqrt{1 - \cos[e+fx]^2} \sec[e+fx]^3 + b \sec[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right) \right) \right) - \\
 & \left( 14 a^3 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] \sec[e+fx]^{10/3} \right. \\
 & \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \left( 2 b \sec[e+fx]^2 \tan[e+fx] + \right. \\
 & \left. a \sec[e+fx] \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \tan[e+fx] + \right. \\
 & \left. \left. \left( a \sec[e+fx] \left( -2 \cos[e+fx] \left( -1 + \sec[e+fx]^2 \right) \sin[e+fx] + 2 \tan[e+fx] \right) \right) \right) \right) / \\
 & \left( 2 \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \right) \Bigg) / \left( 5 \left( -1 + \sec[e+fx]^2 \right) \right) \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] + \right. \\
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \\
 & \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] \right) \sec[e+fx]^2 \right) \\
 & \left( -a^2 + b^2 \left( -1 + \sec[e+fx]^2 \right) \right) \left( a \sqrt{1 - \cos[e+fx]^2} \sec[e+fx]^3 + \right. \\
 & \left. b \sec[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right) \right) \Bigg) - \\
 & \left( 49 a b^2 \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] \sec[e+fx]^{10/3} \right. \\
 & \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \left( 2 b \sec[e+fx]^2 \tan[e+fx] + \right. \\
 & \left. a \sec[e+fx] \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \tan[e+fx] + \right. \\
 & \left. \left. \left( a \sec[e+fx] \left( -2 \cos[e+fx] \left( -1 + \sec[e+fx]^2 \right) \sin[e+fx] + 2 \tan[e+fx] \right) \right) \right) \right) / \\
 & \left( 2 \sqrt{\cos[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right)} \right) \Bigg) / \left( 5 \left( -1 + \sec[e+fx]^2 \right) \right) \\
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] + \right. \\
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \\
 & \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \sec[e+fx]^2, \frac{b^2 \sec[e+fx]^2}{a^2 + b^2} \right] \right) \sec[e+fx]^2 \right) \\
 & \left( -a^2 + b^2 \left( -1 + \sec[e+fx]^2 \right) \right) \left( a \sqrt{1 - \cos[e+fx]^2} \sec[e+fx]^3 + \right. \\
 & \left. b \sec[e+fx]^2 \left( -1 + \sec[e+fx]^2 \right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 26 a b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^{16/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \left( 2 b \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \right. \\
 & \quad a \operatorname{Sec}[e+f x] \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \operatorname{Tan}[e+f x] + \\
 & \quad \left. \left. \left( a \operatorname{Sec}[e+f x] (-2 \operatorname{Cos}[e+f x] (-1+\operatorname{Sec}[e+f x]^2) \operatorname{Sin}[e+f x] + 2 \operatorname{Tan}[e+f x]) \right) \right) \right) / \\
 & \quad \left( 2 \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right) \Bigg) / \left( 35 (-1+\operatorname{Sec}[e+f x]^2) \right) \\
 & \left( 13 (a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] + (a^2+b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \right) \operatorname{Sec}[e+f x]^2 \right) \\
 & \quad \left. (-a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2)) \left( a \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^3 + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \right) \Bigg) + \\
 & \left( 14 a^3 \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^{10/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e+f x]^2 + a \operatorname{Sec}[e+f x] \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right) \right) \\
 & \quad \left( 6 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] + \right. \right. \\
 & \quad \left. \left. (a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \right) \right) \\
 & \quad \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + 7 (a^2+b^2) \left( \frac{1}{7 (a^2+b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \right. \right. \\
 & \quad \left. \left. \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{1}{7} \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Bigg) + \\
 & \quad 3 \operatorname{Sec}[e+f x]^2 \left( 2 b^2 \left( \frac{1}{13 (a^2+b^2)} 28 b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 3, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{7}{13} \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Bigg) + (a^2+b^2) \\
 & \quad \left( \frac{1}{13 (a^2+b^2)} 14 b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \right)
 \end{aligned}$$



$$\begin{aligned} & \left( \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \frac{21}{13} \operatorname{AppellF1}\left[\frac{13}{6}, \frac{5}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \\ & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] \right) \bigg/ \left( 5(-1+\operatorname{Sec}[e+fx]^2) \right. \\ & \left. \left( 7(a^2+b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + 3 \right. \right. \\ & \quad \left. \left( 2b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + (a^2+b^2) \right. \right. \\ & \quad \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \right)^2 \right. \\ & \left. (-a^2+b^2(-1+\operatorname{Sec}[e+fx]^2)) \left( a\sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \right. \right. \\ & \quad \left. \left. b \operatorname{Sec}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2) \right) \right) \bigg) + \\ & \left( 49ab^2 \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \right. \\ & \quad \operatorname{Sec}[e+fx]^{10/3} \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \\ & \quad \left. \left( -b+b \operatorname{Sec}[e+fx]^2 + a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \right) \right. \\ & \quad \left. \left( 6 \left( 2b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \right. \\ & \quad \left. \left. (a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \right. \\ & \quad \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + 7(a^2+b^2) \left( \frac{1}{7(a^2+b^2)} 2b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \right. \right. \\ & \quad \left. \left. \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \frac{1}{7} \operatorname{AppellF1}\left[\right. \right. \\ & \quad \left. \left. \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] \right) + \\ & \quad 3 \operatorname{Sec}[e+fx]^2 \left( 2b^2 \left( \frac{1}{13(a^2+b^2)} 28b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 3, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \right. \\ & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \frac{7}{13} \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \right. \right. \\ & \quad \left. \left. \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] \right) + (a^2+b^2) \right. \\ & \quad \left. \left( \frac{1}{13(a^2+b^2)} 14b^2 \operatorname{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \right. \right. \\ & \quad \left. \left. \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \frac{21}{13} \operatorname{AppellF1}\left[\frac{13}{6}, \frac{5}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \right. \\ & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] \right) \bigg) \bigg/ \left( 5(-1+\operatorname{Sec}[e+fx]^2) \right) \end{aligned}$$

$$\begin{aligned}
 & \left( 7 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right. \\
 & \quad \quad \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \Big)^2 \\
 & \quad \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 + \right. \\
 & \quad \quad \left. b \operatorname{Sec}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \Big) - \\
 & \left( 26 a b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \operatorname{Sec}[e + f x]^{16/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) \\
 & \quad \left( 6 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \right. \\
 & \quad 13 (a^2 + b^2) \left( \frac{1}{13 (a^2 + b^2)} 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) + \\
 & \quad 3 \operatorname{Sec}[e + f x]^2 \left( 2 b^2 \left( \frac{1}{19 (a^2 + b^2)} 52 b^2 \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{1}{2}, 3, \frac{25}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{13}{19} \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{3}{2}, 2, \frac{25}{6}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) + (a^2 + b^2) \\
 & \quad \left( \frac{1}{19 (a^2 + b^2)} 26 b^2 \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{3}{2}, 2, \frac{25}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \quad \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{39}{19} \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{5}{2}, 1, \frac{25}{6}, \operatorname{Sec}[e + f x]^2, \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \Big) \Big) / \left( 35 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \right. \\
 & \quad \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \right) \right)
 \end{aligned}$$

$$\text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \left( -a^2 + b^2 (-1 + \text{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 + b \text{Sec}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2) \right) \right)^2$$

Problem 636: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(d \text{Sec}[e + f x])^{5/3}}{(a + b \text{Tan}[e + f x])^2} dx$$

Optimal (type 6, 687 leaves, 18 steps):

$$\begin{aligned} & \frac{a \text{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2 b^{1/3} (\text{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (d \text{Sec}[e + f x])^{5/3}}{2 \sqrt{3} b^{2/3} (a^2 + b^2)^{7/6} f (\text{Sec}[e + f x]^2)^{5/6}} + \\ & \frac{a \text{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2 b^{1/3} (\text{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (d \text{Sec}[e + f x])^{5/3}}{2 \sqrt{3} b^{2/3} (a^2 + b^2)^{7/6} f (\text{Sec}[e + f x]^2)^{5/6}} - \\ & \frac{a \text{ArcTanh}\left[\frac{b^{1/3} (\text{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{1/6}}\right] (d \text{Sec}[e + f x])^{5/3}}{3 b^{2/3} (a^2 + b^2)^{7/6} f (\text{Sec}[e + f x]^2)^{5/6}} + \\ & \left( a \text{Log}\left[(a^2 + b^2)^{1/3} - b^{1/3} (a^2 + b^2)^{1/6} (\text{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\text{Sec}[e + f x]^2)^{1/3}\right] \right. \\ & \quad \left. (d \text{Sec}[e + f x])^{5/3} \right) / \left( 12 b^{2/3} (a^2 + b^2)^{7/6} f (\text{Sec}[e + f x]^2)^{5/6} \right) - \\ & \left( a \text{Log}\left[(a^2 + b^2)^{1/3} + b^{1/3} (a^2 + b^2)^{1/6} (\text{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\text{Sec}[e + f x]^2)^{1/3}\right] \right. \\ & \quad \left. (d \text{Sec}[e + f x])^{5/3} \right) / \left( 12 b^{2/3} (a^2 + b^2)^{7/6} f (\text{Sec}[e + f x]^2)^{5/6} \right) + \\ & \left( \text{AppellF1}\left[\frac{1}{2}, 2, \frac{1}{6}, \frac{3}{2}, \frac{b^2 \text{Tan}[e + f x]^2}{a^2}, -\text{Tan}[e + f x]^2\right] (d \text{Sec}[e + f x])^{5/3} \text{Tan}[e + f x] \right) / \\ & \quad \left( a^2 f (\text{Sec}[e + f x]^2)^{5/6} \right) + \\ & \left( b^2 \text{AppellF1}\left[\frac{3}{2}, 2, \frac{1}{6}, \frac{5}{2}, \frac{b^2 \text{Tan}[e + f x]^2}{a^2}, -\text{Tan}[e + f x]^2\right] (d \text{Sec}[e + f x])^{5/3} \text{Tan}[e + f x]^3 \right) / \\ & \quad \left( 3 a^4 f (\text{Sec}[e + f x]^2)^{5/6} \right) - \frac{a b (d \text{Sec}[e + f x])^{5/3}}{(a^2 + b^2) f (a^2 - b^2 \text{Tan}[e + f x]^2)} \end{aligned}$$

Result (type 6, 19462 leaves):

$$\left( \text{Sec}[e + f x] (d \text{Sec}[e + f x])^{5/3} (a \text{Cos}[e + f x] + b \text{Sin}[e + f x])^2 \left( \frac{b \text{Cos}[e + f x]}{a (a - i b) (a + i b)} + \right. \right.$$

$$\begin{aligned}
 & \left( \frac{\sin[e+fx]}{(a-ib)(a+ib)} - \frac{b}{(a-ib)(a+ib)(a\cos[e+fx]+b\sin[e+fx])} \right) \Big/ \\
 & \left( f(a+b\tan[e+fx])^2 - \left( 4 \operatorname{AppellF1} \left[ \frac{1}{3}, \frac{1}{6}, \frac{1}{6}, \frac{4}{3}, \frac{a-ib}{a+b\tan[e+fx]}, \frac{a+ib}{a+b\tan[e+fx]} \right] \right. \right. \\
 & \left. \left. (d\sec[e+fx])^{5/3} (a\cos[e+fx]+b\sin[e+fx])^2 \right) \Big/ \left( abf(a+b\tan[e+fx]) \right. \right. \\
 & \left. \left. \left( (a+ib) \operatorname{AppellF1} \left[ \frac{4}{3}, \frac{1}{6}, \frac{7}{6}, \frac{7}{3}, \frac{a-ib}{a+b\tan[e+fx]}, \frac{a+ib}{a+b\tan[e+fx]} \right] + \right. \right. \\
 & \left. \left. (a-ib) \operatorname{AppellF1} \left[ \frac{4}{3}, \frac{7}{6}, \frac{1}{6}, \frac{7}{3}, \frac{a-ib}{a+b\tan[e+fx]}, \frac{a+ib}{a+b\tan[e+fx]} \right] + \right. \right. \\
 & \left. \left. 8 \operatorname{AppellF1} \left[ \frac{1}{3}, \frac{1}{6}, \frac{1}{6}, \frac{4}{3}, \frac{a-ib}{a+b\tan[e+fx]}, \frac{a+ib}{a+b\tan[e+fx]} \right] (a+b\tan[e+fx]) \right) \right) - \\
 & \left( \sec[e+fx] (d\sec[e+fx])^{5/3} \left( \frac{6(b+a\sqrt{1-\cos[e+fx]^2}) \sec[e+fx]}{(a^2+b^2)\sec[e+fx]^{1/3}} + \right. \right. \\
 & \left. \left. \left( (-1)^{1/6} (-a^2+b^2) \operatorname{ArcTan} \left[ \frac{-\sqrt{3}(a^2+b^2)^{1/6} + 2(-1)^{1/6} b^{1/3} \sec[e+fx]^{1/3}}{(a^2+b^2)^{1/6}} \right] \sec[e+fx]^{2/3} \right. \right. \\
 & \left. \left. \left( -b+b\sec[e+fx]^2 + a\sec[e+fx] \sqrt{\cos[e+fx]^2(-1+\sec[e+fx]^2)} \right) \right) \Big/ \right. \\
 & \left. \left( 2b^{2/3}(a^2+b^2)^{7/6} \left( a\sqrt{1-\cos[e+fx]^2} \sec[e+fx]^{5/3} + \right. \right. \right. \\
 & \left. \left. \left. b\sec[e+fx]^{2/3}(-1+\sec[e+fx]^2) \right) \right) + \right. \\
 & \left. \left( (-1)^{1/6} (-a^2+b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{3}(a^2+b^2)^{1/6} + 2(-1)^{1/6} b^{1/3} \sec[e+fx]^{1/3}}{(a^2+b^2)^{1/6}} \right] \sec[e+fx]^{2/3} \right. \right. \\
 & \left. \left. \left( -b+b\sec[e+fx]^2 + a\sec[e+fx] \sqrt{\cos[e+fx]^2(-1+\sec[e+fx]^2)} \right) \right) \Big/ \right. \\
 & \left. \left( 2b^{2/3}(a^2+b^2)^{7/6} \left( a\sqrt{1-\cos[e+fx]^2} \sec[e+fx]^{5/3} + \right. \right. \right. \\
 & \left. \left. \left. b\sec[e+fx]^{2/3}(-1+\sec[e+fx]^2) \right) \right) + \right. \\
 & \left. \left( (-1)^{1/6} (-a^2+b^2) \operatorname{ArcTan} \left[ \frac{(-1)^{1/6} b^{1/3} \sec[e+fx]^{1/3}}{(a^2+b^2)^{1/6}} \right] \sec[e+fx]^{2/3} \left( -b+b\sec[e+fx]^2 + \right. \right. \right. \\
 & \left. \left. \left. a\sec[e+fx] \sqrt{\cos[e+fx]^2(-1+\sec[e+fx]^2)} \right) \right) \Big/ \left( b^{2/3}(a^2+b^2)^{7/6} \right. \right. \\
 & \left. \left. \left( a\sqrt{1-\cos[e+fx]^2} \sec[e+fx]^{5/3} + b\sec[e+fx]^{2/3}(-1+\sec[e+fx]^2) \right) \right) + \right. \\
 & \left. \left( (-1)^{1/6} \sqrt{3} (-a^2+b^2) \operatorname{Log} \left[ (a^2+b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \sec[e+fx]^{1/3} + \right. \right. \right. \\
 & \left. \left. \left. (-1)^{1/3} b^{2/3} \sec[e+fx]^{2/3} \right] \sec[e+fx]^{2/3} \left( -b+b\sec[e+fx]^2 + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \Big) \Big/ \left( 4 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + b \operatorname{Sec}[e+fx]^{2/3} (-1+\operatorname{Sec}[e+fx]^2) \right) \right) - \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2+b^2) \operatorname{Log}\left[ (a^2+b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+fx]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{2/3} \right] \operatorname{Sec}[e+fx]^{2/3} \left( -b + b \operatorname{Sec}[e+fx]^2 + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \right) \right) \Big/ \left( 4 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + b \operatorname{Sec}[e+fx]^{2/3} (-1+\operatorname{Sec}[e+fx]^2) \right) \right) + \\
 & \left( 33 a^3 \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^{10/3} \right. \\
 & \left. \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \left( -b + b \operatorname{Sec}[e+fx]^2 + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \right) \right) \Big/ \left( (-1+\operatorname{Sec}[e+fx]^2) \right. \\
 & \left. \left( 11 (a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \\
 & \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a^2+b^2) \operatorname{AppellF1}\left[\frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \operatorname{Sec}[e+fx]^2 \right) \right. \\
 & \left. \left. (-a^2+b^2 (-1+\operatorname{Sec}[e+fx]^2)) \left( a \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + \right. \right. \right. \\
 & \left. \left. \left. b \operatorname{Sec}[e+fx]^{2/3} (-1+\operatorname{Sec}[e+fx]^2) \right) \right) \right) + \\
 & \left( 99 a b^2 \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^{10/3} \right. \\
 & \left. \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \left( -b + b \operatorname{Sec}[e+fx]^2 + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1+\operatorname{Sec}[e+fx]^2)} \right) \right) \Big/ \left( 5 (-1+\operatorname{Sec}[e+fx]^2) \right. \\
 & \left. \left( 11 (a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \\
 & \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a^2+b^2) \operatorname{AppellF1}\left[\frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \operatorname{Sec}[e+fx]^2 \right) \right. \\
 & \left. \left. (-a^2+b^2 (-1+\operatorname{Sec}[e+fx]^2)) \left( a \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + \right. \right. \right. \\
 & \left. \left. \left. b \operatorname{Sec}[e+fx]^{2/3} (-1+\operatorname{Sec}[e+fx]^2) \right) \right) \right) - \\
 & \left( 204 a b^2 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] \operatorname{Sec}[e+fx]^{16/3} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \left( -b+b \sec [e+f x]^2 + \right. \right. \right. \\
 & \left. \left. \left. a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \right) \right) / \left( 11 (-1+\sec [e+f x]^2) \right. \\
 & \left( 17 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] \right) \sec [e+f x]^2 \right) \\
 & \left. \left. \left. (-a^2+b^2 (-1+\sec [e+f x]^2)) \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + \right. \right. \right. \right. \\
 & \left. \left. \left. b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) \right) \right) \\
 & (\cos [e+f x] - \sin [e+f x]) (\cos [e+f x] + \sin [e+f x]) \\
 & \left. \left. \left. (a \cos [e+f x] + b \sin [e+f x]) \right) \right) \right) / \left( 6 \right. \\
 & a \\
 & f \\
 & (a+b \tan [e+f x])^2 \\
 & \left( -\frac{1}{a^2+b^2} 2 \sec [e+f x]^{2/3} \left( b+a \sqrt{1-\cos [e+f x]^2} \sec [e+f x] \right) \sin [e+f x] + \right. \\
 & \left( (-1)^{1/6} (-a^2+b^2) \operatorname{ArcTan} \left[ \frac{-\sqrt{3} (a^2+b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \sec [e+f x]^{1/3}}{(a^2+b^2)^{1/6}} \right] \sec [e+f x]^{5/3} \right. \\
 & \left. \left. \left. \left( -b+b \sec [e+f x]^2 + a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \right) \right) \right) \\
 & \left. \left. \left. \sin [e+f x] \right) \right) \right) / \left( 3 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left. \left. \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) \right) \right) + \\
 & \left( (-1)^{1/6} (-a^2+b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{3} (a^2+b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \sec [e+f x]^{1/3}}{(a^2+b^2)^{1/6}} \right] \right. \\
 & \left. \left. \left. \sec [e+f x]^{5/3} \left( -b+b \sec [e+f x]^2 + a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \right) \right) \right) \\
 & \left. \left. \left. \sin [e+f x] \right) \right) \right) / \left( 3 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left. \left. \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan} \left[ \frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^{5/3} \right. \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) / \left( 3 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{Log} \left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^{5/3} \right. \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) / \left( 2 \sqrt{3} b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{Log} \left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^{5/3} \right. \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) / \left( 2 \sqrt{3} b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \quad \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( 66 a^3 b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \operatorname{Sec}[e + f x]^{19/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) / \left( (-1 + \operatorname{Sec}[e + f x]^2) \right. \\
 & \quad \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \quad \left. \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( 198 a b^4 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e + f x]^{19/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \operatorname{Sin}[e + f x] \Big/ \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \right. \\
 & \left. \left( 11 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \\
 & \quad \left. \left. (a^2 + b^2) \operatorname{AppellF1}\left[\frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2))^2 \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( 408 a b^4 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right. \\
 & \quad \operatorname{Sec}[e + f x]^{25/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) \Big/ \left( 11 (-1 + \operatorname{Sec}[e + f x]^2) \right. \\
 & \quad \left. \left( 17 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \\
 & \quad \left. \left. (a^2 + b^2) \operatorname{AppellF1}\left[\frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \quad \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2))^2 \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( 66 a^3 \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \operatorname{Sec}[e + f x]^{19/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \quad \left. \operatorname{Sin}[e + f x] \right) \Big/ \left( (-1 + \operatorname{Sec}[e + f x]^2)^2 \right. \\
 & \quad \left. \left( 11 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \\
 & \quad \left. \left. (a^2 + b^2) \operatorname{AppellF1}\left[\frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -a^2 + b^2 (-1 + \sec[e + f x]^2) \right) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \\
 & \quad \left. b \sec[e + f x]^{2/3} (-1 + \sec[e + f x]^2) \right) - \\
 & \left( 198 a b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \sec[e + f x]^{19/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \\
 & \quad \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \\
 & \quad \left. \sin[e + f x] \right) / \left( 5 (-1 + \sec[e + f x]^2)^2 \right) \\
 & \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \Big) \\
 & \left( -a^2 + b^2 (-1 + \sec[e + f x]^2) \right) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \\
 & \quad \left. b \sec[e + f x]^{2/3} (-1 + \sec[e + f x]^2) \right) \Big) + \\
 & \left( 110 a^3 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \sec[e + f x]^{13/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \\
 & \quad \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right) \\
 & \quad \left. \sin[e + f x] \right) / \left( (-1 + \sec[e + f x]^2) \right) \\
 & \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \Big) \\
 & \left( -a^2 + b^2 (-1 + \sec[e + f x]^2) \right) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \\
 & \quad \left. b \sec[e + f x]^{2/3} (-1 + \sec[e + f x]^2) \right) \Big) + \\
 & \left( 66 a b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \sec[e + f x]^{13/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \\
 & \quad \left( -b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \right)
 \end{aligned}$$

$$\begin{aligned}
& \sin[e + f x] \Big/ \left( (-1 + \sec[e + f x])^2 \right) \\
& \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \\
& \left. (-a^2 + b^2 (-1 + \sec[e + f x]^2)) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \right. \\
& \quad \left. \left. b \sec[e + f x]^{2/3} (-1 + \sec[e + f x]^2) \right) \right) + \\
& \left( 408 a b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
& \quad \sec[e + f x]^{25/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \\
& \quad \left. (-b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)}) \right) \\
& \sin[e + f x] \Big/ \left( 11 (-1 + \sec[e + f x])^2 \right) \\
& \left( 17 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \\
& \left. (-a^2 + b^2 (-1 + \sec[e + f x]^2)) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \right. \\
& \quad \left. \left. b \sec[e + f x]^{2/3} (-1 + \sec[e + f x]^2) \right) \right) - \\
& \left( 1088 a b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right. \\
& \quad \sec[e + f x]^{19/3} \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)} \\
& \quad \left. (-b + b \sec[e + f x]^2 + a \sec[e + f x] \sqrt{\cos[e + f x]^2 (-1 + \sec[e + f x]^2)}) \right) \\
& \sin[e + f x] \Big/ \left( 11 (-1 + \sec[e + f x])^2 \right) \\
& \left( 17 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] + \right. \\
& \quad \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \sec[e + f x]^2, \frac{b^2 \sec[e + f x]^2}{a^2 + b^2} \right] \right) \sec[e + f x]^2 \\
& \left. (-a^2 + b^2 (-1 + \sec[e + f x]^2)) \left( a \sqrt{1 - \cos[e + f x]^2} \sec[e + f x]^{5/3} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) + \left( (-1)^{1/6} \sqrt{3} (-a^2 + b^2) \operatorname{Sec}[e + f x]^{2/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left( -\frac{(-1)^{1/6} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{4/3} \operatorname{Sin}[e + f x]}{\sqrt{3}} + \right. \\
 & \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{5/3} \operatorname{Sin}[e + f x] \right) \right) / \left( 4 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right) \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2 + b^2) \operatorname{Sec}[e + f x]^{2/3} \left( -b + b \operatorname{Sec}[e + f x]^2 + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left( \frac{(-1)^{1/6} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{4/3} \operatorname{Sin}[e + f x]}{\sqrt{3}} + \right. \\
 & \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{5/3} \operatorname{Sin}[e + f x] \right) \right) / \left( 4 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right) \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan} \left[ \frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \right. \\
 & \operatorname{Sec}[e + f x]^{2/3} \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + \right. \\
 & 2 b \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \left. \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \right) / \left( 2 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \right. \\
 & \left. \operatorname{Sec}[e + f x]^{2/3} \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + \right. \\
 & 2 b \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \\
 & \left. \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) / \left( 2 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan}\left[ \frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}} \right] \operatorname{Sec}[e + f x]^{2/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + \right. \right. \\
 & \left. \left. 2 b \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \right. \right. \\
 & \left. \left. \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \right) / \left( b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2 + b^2) \operatorname{Log}\left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^{2/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right. \\
 & \left. \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + \right. \right. \\
 & \left. \left. 2 b \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \right. \right. \\
 & \left. \left. \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \right) / \left( 4 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) + \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2 + b^2) \operatorname{Log}\left[ (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3} \right] \operatorname{Sec}[e + f x]^{2/3} \right. \\
 & \left. \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + \right. \\
 & 2 b \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \\
 & \left. \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \Bigg/ \left( 4 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \right) - \\
 & \left( 33 a^3 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \operatorname{Sec}[e + f x]^{10/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + 2 b \right. \\
 & \left. \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \Bigg) \Bigg/ \\
 & \left( (-1 + \operatorname{Sec}[e + f x]^2) \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \Bigg) - \\
 & \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right)^2 \Bigg) - \\
 & \left( 99 a b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \operatorname{Sec}[e + f x]^{10/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{a \operatorname{Sec}[e + f x]^{2/3} \operatorname{Sin}[e + f x]}{\sqrt{1 - \operatorname{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{8/3} \operatorname{Sin}[e + f x] + 2 b \right. \\
 & \left. \operatorname{Sec}[e + f x]^{11/3} \operatorname{Sin}[e + f x] + \frac{2}{3} b \operatorname{Sec}[e + f x]^{5/3} (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] \right) \Bigg) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 (-1 + \text{Sec}[e + f x]^2) \left( 11 (a^2 + b^2) \text{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \text{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \text{AppellF1}\left[\frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \text{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \text{Sec}[e + f x]^2 \left( -a^2 + b^2 (-1 + \text{Sec}[e + f x]^2) \right) \\
 & \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^{5/3} + b \text{Sec}[e + f x]^{2/3} (-1 + \text{Sec}[e + f x]^2) \right)^2 \right) + \\
 & \left( 204 a b^2 \text{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \text{Sec}[e + f x]^{16/3} \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \\
 & \quad \left( -b + b \text{Sec}[e + f x]^2 + a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \\
 & \quad \left( \frac{a \text{Sec}[e + f x]^{2/3} \text{Sin}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} + \frac{5}{3} a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^{8/3} \text{Sin}[e + f x] + 2 b \right. \\
 & \quad \left. \left. \left. \text{Sec}[e + f x]^{11/3} \text{Sin}[e + f x] + \frac{2}{3} b \text{Sec}[e + f x]^{5/3} (-1 + \text{Sec}[e + f x]^2) \text{Sin}[e + f x] \right) \right) \right) / \\
 & \left( 11 (-1 + \text{Sec}[e + f x]^2) \left( 17 (a^2 + b^2) \text{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + 3 \left( 2 b^2 \text{AppellF1}\left[\frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \text{Sec}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \text{AppellF1}\left[\frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \text{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \text{Sec}[e + f x]^2 \left( -a^2 + b^2 (-1 + \text{Sec}[e + f x]^2) \right) \\
 & \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^{5/3} + b \text{Sec}[e + f x]^{2/3} (-1 + \text{Sec}[e + f x]^2) \right)^2 \right) + \\
 & \left( (-1)^{1/3} (-a^2 + b^2) \text{Sec}[e + f x] \left( -b + b \text{Sec}[e + f x]^2 + \right. \right. \\
 & \quad \left. \left. a \text{Sec}[e + f x] \sqrt{\text{Cos}[e + f x]^2 (-1 + \text{Sec}[e + f x]^2)} \right) \text{Tan}[e + f x] \right) / \\
 & \left( 3 b^{1/3} (a^2 + b^2)^{4/3} \left( 1 + \frac{(-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \text{Sec}[e + f x]^{1/3})^2}{(a^2 + b^2)^{1/3}} \right) \right) \\
 & \left. \left( a \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^{5/3} + b \text{Sec}[e + f x]^{2/3} (-1 + \text{Sec}[e + f x]^2) \right) \right) + \\
 & \left( (-1)^{1/3} (-a^2 + b^2) \text{Sec}[e + f x] \left( -b + b \text{Sec}[e + f x]^2 + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \tan [e + f x] \right) / \right. \\
 & \left( 3 b^{1/3} (a^2 + b^2)^{4/3} \left( 1 + \frac{(\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \sec [e + f x]^{1/3})^2}{(a^2 + b^2)^{1/3}} \right) \right. \\
 & \left. \left( a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^{5/3} + b \sec [e + f x]^{2/3} (-1 + \sec [e + f x]^2) \right) \right) + \\
 & \left( (-1)^{1/3} (-a^2 + b^2) \sec [e + f x] \left( -b + b \sec [e + f x]^2 + \right. \right. \\
 & \left. \left. a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \tan [e + f x] \right) / \right. \\
 & \left( 3 b^{1/3} (a^2 + b^2)^{4/3} \left( 1 + \frac{(-1)^{1/3} b^{2/3} \sec [e + f x]^{2/3}}{(a^2 + b^2)^{1/3}} \right) \right. \\
 & \left. \left( a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^{5/3} + b \sec [e + f x]^{2/3} (-1 + \sec [e + f x]^2) \right) \right) + \\
 & \left( 33 a^3 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] \sec [e + f x]^{10/3} \right. \\
 & \left( -b + b \sec [e + f x]^2 + a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \\
 & \left. (-2 \cos [e + f x] (-1 + \sec [e + f x]^2) \sin [e + f x] + 2 \tan [e + f x]) \right) / \\
 & \left( 2 (-1 + \sec [e + f x]^2) \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right. \\
 & \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] \right) \sec [e + f x]^2 \right) \\
 & \left. (-a^2 + b^2 (-1 + \sec [e + f x]^2)) \left( a \sqrt{1 - \cos [e + f x]^2} \sec [e + f x]^{5/3} + \right. \right. \\
 & \left. \left. b \sec [e + f x]^{2/3} (-1 + \sec [e + f x]^2) \right) \right) + \\
 & \left( 99 a b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] \sec [e + f x]^{10/3} \right. \\
 & \left( -b + b \sec [e + f x]^2 + a \sec [e + f x] \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right) \\
 & \left. (-2 \cos [e + f x] (-1 + \sec [e + f x]^2) \sin [e + f x] + 2 \tan [e + f x]) \right) / \\
 & \left( 10 (-1 + \sec [e + f x]^2) \sqrt{\cos [e + f x]^2 (-1 + \sec [e + f x]^2)} \right. \\
 & \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e + f x]^2, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
& \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+f x]^2 \\
& \left( -a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \left( a \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^{5/3} + \right. \\
& \quad \left. b \operatorname{Sec}[e+f x]^{2/3} (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) - \\
& \left( 102 a b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^{16/3} \right. \\
& \quad \left( -b+b \operatorname{Sec}[e+f x]^2+a \operatorname{Sec}[e+f x] \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right) \\
& \quad \left. (-2 \operatorname{Cos}[e+f x] (-1+\operatorname{Sec}[e+f x]^2) \operatorname{Sin}[e+f x]+2 \operatorname{Tan}[e+f x]) \right) \Big) / \\
& \left( 11 (-1+\operatorname{Sec}[e+f x]^2) \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right. \\
& \quad \left( 17 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
& \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
& \quad \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+f x]^2 \Big) \\
& \quad \left. (-a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \left( a \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^{5/3} + \right. \\
& \quad \left. b \operatorname{Sec}[e+f x]^{2/3} (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) + \\
& \left( 6 \left( \frac{a \operatorname{Sin}[e+f x]}{\sqrt{1-\operatorname{Cos}[e+f x]^2}} + a \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x] \operatorname{Tan}[e+f x] \right) \right) / \\
& \quad \left( (a^2+b^2) \operatorname{Sec}[e+f x]^{1/3} \right) + \\
& \left( 33 a^3 \operatorname{Sec}[e+f x]^{10/3} \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right. \\
& \quad \left( -b+b \operatorname{Sec}[e+f x]^2+a \operatorname{Sec}[e+f x] \sqrt{\operatorname{Cos}[e+f x]^2 (-1+\operatorname{Sec}[e+f x]^2)} \right) \\
& \quad \left( \frac{1}{11 (a^2+b^2)} 10 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right. \\
& \quad \quad \left. \operatorname{Tan}[e+f x] + \frac{5}{11} \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
& \quad \quad \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Big) / \left( (-1+\operatorname{Sec}[e+f x]^2) \right. \\
& \quad \left( 11 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
& \quad \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left. \left( (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \right) \right. \\
 & \left. \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) + \\
 & \left( 99 a b^2 \operatorname{Sec}[e + f x]^{10/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right. \\
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{1}{11 (a^2 + b^2)} 10 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \operatorname{Tan}[e + f x] + \frac{5}{11} \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \right) / \left( 5 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 11 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left. \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) - \\
 & \left( 204 a b^2 \operatorname{Sec}[e + f x]^{16/3} \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right. \\
 & \left( -b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \\
 & \left( \frac{1}{17 (a^2 + b^2)} 22 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \right. \\
 & \left. \operatorname{Tan}[e + f x] + \frac{11}{17} \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \right) / \left( 11 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 17 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \left. \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \right) \\
 & \left. \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. b \operatorname{Sec}[e+fx]^{2/3} (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \right) + \right. \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan}\left[\frac{-\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e+fx]^{1/3}}{(a^2 + b^2)^{1/6}}\right] \right. \\
 & \left. \operatorname{Sec}[e+fx]^{2/3} \left( 2b \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. (a \operatorname{Sec}[e+fx] (-2 \operatorname{Cos}[e+fx] (-1 + \operatorname{Sec}[e+fx]^2) \operatorname{Sin}[e+fx] + 2 \operatorname{Tan}[e+fx])) \right) \right) / \\
 & \left. \left( 2 \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \right) \left. \right) / \left( 2 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + b \operatorname{Sec}[e+fx]^{2/3} (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \left. \right) + \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan}\left[\frac{\sqrt{3} (a^2 + b^2)^{1/6} + 2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e+fx]^{1/3}}{(a^2 + b^2)^{1/6}}\right] \right. \\
 & \left. \operatorname{Sec}[e+fx]^{2/3} \left( 2b \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. (a \operatorname{Sec}[e+fx] (-2 \operatorname{Cos}[e+fx] (-1 + \operatorname{Sec}[e+fx]^2) \operatorname{Sin}[e+fx] + 2 \operatorname{Tan}[e+fx])) \right) \right) / \\
 & \left. \left( 2 \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \right) \left. \right) / \left( 2 b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + b \operatorname{Sec}[e+fx]^{2/3} (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \left. \right) + \\
 & \left( (-1)^{1/6} (-a^2 + b^2) \operatorname{ArcTan}\left[\frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e+fx]^{1/3}}{(a^2 + b^2)^{1/6}}\right] \operatorname{Sec}[e+fx]^{2/3} \right. \\
 & \left. \left( 2b \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. (a \operatorname{Sec}[e+fx] (-2 \operatorname{Cos}[e+fx] (-1 + \operatorname{Sec}[e+fx]^2) \operatorname{Sin}[e+fx] + 2 \operatorname{Tan}[e+fx])) \right) \right) / \\
 & \left. \left( 2 \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \right) \right) \left. \right) / \left( b^{2/3} (a^2 + b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{5/3} + b \operatorname{Sec}[e+fx]^{2/3} (-1 + \operatorname{Sec}[e+fx]^2) \right) \right) \left. \right) + \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2 + b^2) \operatorname{Log}\left[ (a^2 + b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e+fx]^{1/3} + \right. \right. \\
 & \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{2/3} \right] \operatorname{Sec}[e+fx]^{2/3} \left( 2b \operatorname{Sec}[e+fx]^2 \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. a \operatorname{Sec}[e+fx] \sqrt{\operatorname{Cos}[e+fx]^2 (-1 + \operatorname{Sec}[e+fx]^2)} \operatorname{Tan}[e+fx] + \right. \right. \\
 & \left. \left. (a \operatorname{Sec}[e+fx] (-2 \operatorname{Cos}[e+fx] (-1 + \operatorname{Sec}[e+fx]^2) \operatorname{Sin}[e+fx] + 2 \operatorname{Tan}[e+fx])) \right) \right) \left. \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \Bigg) \Bigg/ \left( 4 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) - \\
 & \left( (-1)^{1/6} \sqrt{3} (-a^2+b^2) \log \left[ (a^2+b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \sec [e+f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \sec [e+f x]^{2/3} \right] \sec [e+f x]^{2/3} \left( 2 b \sec [e+f x]^2 \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. (a \sec [e+f x] (-2 \cos [e+f x] (-1+\sec [e+f x]^2) \sin [e+f x] + 2 \tan [e+f x])) \right) \right) \Bigg/ \\
 & \left( 2 \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \Bigg) \Bigg/ \left( 4 b^{2/3} (a^2+b^2)^{7/6} \right. \\
 & \left. \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) + \\
 & \left( 33 a^3 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] \sec [e+f x]^{10/3} \right. \\
 & \quad \left. \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \left( 2 b \sec [e+f x]^2 \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. (a \sec [e+f x] (-2 \cos [e+f x] (-1+\sec [e+f x]^2) \sin [e+f x] + 2 \tan [e+f x])) \right) \right) \Bigg/ \\
 & \left( 2 \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \Bigg) \Bigg/ \left( (-1+\sec [e+f x]^2) \right. \\
 & \left. \left( 11 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] \right) \sec [e+f x]^2 \right) \right) \\
 & \left. \left( -a^2+b^2 (-1+\sec [e+f x]^2) \right) \left( a \sqrt{1-\cos [e+f x]^2} \sec [e+f x]^{5/3} + \right. \right. \\
 & \quad \left. \left. b \sec [e+f x]^{2/3} (-1+\sec [e+f x]^2) \right) \right) \Bigg) + \\
 & \left( 99 a b^2 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] \sec [e+f x]^{10/3} \right. \\
 & \quad \left. \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \left( 2 b \sec [e+f x]^2 \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. a \sec [e+f x] \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \tan [e+f x] + \right. \right. \\
 & \quad \left. \left. (a \sec [e+f x] (-2 \cos [e+f x] (-1+\sec [e+f x]^2) \sin [e+f x] + 2 \tan [e+f x])) \right) \right) \Bigg/ \\
 & \left( 2 \sqrt{\cos [e+f x]^2 (-1+\sec [e+f x]^2)} \right) \Bigg) \Bigg/ \left( 5 (-1+\sec [e+f x]^2) \right. \\
 & \left. \left( 11 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \sec [e+f x]^2, \frac{b^2 \sec [e+f x]^2}{a^2+b^2} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \\
 & \left( -a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2) \right) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \\
 & \quad \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \Big) - \\
 & \left( 204 a b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^{16/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \left( 2 b \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \right. \\
 & \quad \left. a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \operatorname{Tan}[e + f x] + \right. \\
 & \quad \left. (a \operatorname{Sec}[e + f x] (-2 \operatorname{Cos}[e + f x] (-1 + \operatorname{Sec}[e + f x]^2) \operatorname{Sin}[e + f x] + 2 \operatorname{Tan}[e + f x])) \right) / \\
 & \quad \left. \left( 2 \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \right) \right) \Big) / \left( 11 (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 17 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{1}{2}, 2, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{17}{6}, \frac{3}{2}, 1, \frac{23}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \left( a \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^{5/3} + \right. \right. \\
 & \quad \left. \left. b \operatorname{Sec}[e + f x]^{2/3} (-1 + \operatorname{Sec}[e + f x]^2) \right) \right) \Big) - \\
 & \left( 33 a^3 \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^{10/3} \right. \\
 & \quad \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)} \\
 & \quad \left. (-b + b \operatorname{Sec}[e + f x]^2 + a \operatorname{Sec}[e + f x] \sqrt{\operatorname{Cos}[e + f x]^2 (-1 + \operatorname{Sec}[e + f x]^2)}) \right) \\
 & \left( 6 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + (a^2 + b^2) \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{11}{6}, \frac{3}{2}, 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \right. \\
 & \quad 11 (a^2 + b^2) \left( \frac{1}{11 (a^2 + b^2)} 10 b^2 \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 2, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] + \frac{5}{11} \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. 1, \frac{17}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \Big) +
 \end{aligned}$$







$$\begin{aligned}
 & \frac{5 a b^{2/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2 b^{1/3} (\operatorname{Sec}[e+f x]^2)^{1/6}}{\sqrt{3} (a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+f x])^{1/3}}{2 \sqrt{3} (a^2+b^2)^{11/6} f (\operatorname{Sec}[e+f x]^2)^{1/6}} - \\
 & \frac{5 a b^{2/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2 b^{1/3} (\operatorname{Sec}[e+f x]^2)^{1/6}}{\sqrt{3} (a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+f x])^{1/3}}{2 \sqrt{3} (a^2+b^2)^{11/6} f (\operatorname{Sec}[e+f x]^2)^{1/6}} - \\
 & \frac{5 a b^{2/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e+f x]^2)^{1/6}}{(a^2+b^2)^{1/6}}\right] (d \operatorname{Sec}[e+f x])^{1/3}}{3 (a^2+b^2)^{11/6} f (\operatorname{Sec}[e+f x]^2)^{1/6}} + \\
 & \left(5 a b^{2/3} \operatorname{Log}\left[(a^2+b^2)^{1/3} - b^{1/3} (a^2+b^2)^{1/6} (\operatorname{Sec}[e+f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e+f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{1/3}\right) / \left(12 (a^2+b^2)^{11/6} f (\operatorname{Sec}[e+f x]^2)^{1/6}\right) - \\
 & \left(5 a b^{2/3} \operatorname{Log}\left[(a^2+b^2)^{1/3} + b^{1/3} (a^2+b^2)^{1/6} (\operatorname{Sec}[e+f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e+f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (d \operatorname{Sec}[e+f x])^{1/3}\right) / \left(12 (a^2+b^2)^{11/6} f (\operatorname{Sec}[e+f x]^2)^{1/6}\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2, \frac{5}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2}, -\operatorname{Tan}[e+f x]^2\right] (d \operatorname{Sec}[e+f x])^{1/3} \operatorname{Tan}[e+f x]\right) / \\
 & \quad \left(a^2 f (\operatorname{Sec}[e+f x]^2)^{1/6}\right) + \\
 & \left(b^2 \operatorname{AppellF1}\left[\frac{3}{2}, 2, \frac{5}{6}, \frac{5}{2}, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2}, -\operatorname{Tan}[e+f x]^2\right] (d \operatorname{Sec}[e+f x])^{1/3} \operatorname{Tan}[e+f x]^3\right) / \\
 & \quad \left(3 a^4 f (\operatorname{Sec}[e+f x]^2)^{1/6}\right) - \frac{a b (d \operatorname{Sec}[e+f x])^{1/3}}{(a^2+b^2) f (a^2-b^2 \operatorname{Tan}[e+f x]^2)}
 \end{aligned}$$

Result (type 6, 6547 leaves):

$$\begin{aligned}
 & \left( (d \operatorname{Sec}[e+f x])^{1/3} \left( \frac{1}{12 (a-i b) (a+i b) (a^2+b^2)^{5/6}} \right. \right. \\
 & \quad \left. \left. 5 (-1)^{5/6} a b^{2/3} \left( -2 \operatorname{ArcTan}\left[\sqrt{3} - \frac{2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{1/3}}{(a^2+b^2)^{1/6}}\right] + \right. \right. \\
 & \quad \left. \left. 2 \operatorname{ArcTan}\left[\sqrt{3} + \frac{2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{1/3}}{(a^2+b^2)^{1/6}}\right] + 4 \operatorname{ArcTan}\left[\frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{1/3}}{(a^2+b^2)^{1/6}}\right] - \right. \right. \\
 & \quad \left. \left. \sqrt{3} \operatorname{Log}\left[(a^2+b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+f x]^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+f x]^{2/3}\right] + \sqrt{3} \operatorname{Log}\left[(a^2+b^2)^{1/3} + \right. \right. \\
 & \quad \left. \left. (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+f x]^{2/3}\right] \right) + \\
 & \quad \left. 3 \left( - \left( \left( 7 (3 a^2 - 2 b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] \right. \right. \right. \right. \\
 & \quad \left. \left. \sqrt{1 - \operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^{4/3} \right) / \left( 3 (-1 + \operatorname{Sec}[e+f x]^2) \right) \right. \\
 & \quad \left. \left. \left( 7 (a^2+b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] + 3 \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right) \Bigg) + \\
 & \frac{1}{21} b \operatorname{Sec}[e+f x]^{1/3} \left( \frac{-7 a+7 b \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]}{(a^2+b^2) \left( a^2+b^2-b^2 \operatorname{Sec}[e+f x]^2 \right)} - \right. \\
 & \quad \left. \left( 26 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^3 \right) / \left( \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right. \right. \\
 & \quad \left. \left( 13 \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \right) \right) \right) \Bigg) / \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( f \left( a+b \operatorname{Tan}[e+f x] \right)^2 \left( \frac{1}{12 \left( a-i b \right) \left( a+i b \right) \left( a^2+b^2 \right)^{5/6}} \right. \right. \\
 & \quad \left. \left. \begin{aligned} & 5 \\ & (-1)^{5/6} \\ & a \\ & b^{2/3} \end{aligned} \right. \right. \\
 & \quad \left( \frac{4 \left( -1 \right)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{4/3} \operatorname{Sin}[e+f x]}{3 \left( a^2+b^2 \right)^{1/6} \left( 1+\left( \sqrt{3}-\frac{2 \left( -1 \right)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{1/3}}{\left( a^2+b^2 \right)^{1/6}} \right)^2} \right) + \right. \\
 & \quad \frac{4 \left( -1 \right)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{4/3} \operatorname{Sin}[e+f x]}{3 \left( a^2+b^2 \right)^{1/6} \left( 1+\left( \sqrt{3}+\frac{2 \left( -1 \right)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{1/3}}{\left( a^2+b^2 \right)^{1/6}} \right)^2} \right) + \\
 & \quad \frac{4 \left( -1 \right)^{1/6} b^{1/3} \operatorname{Sec}[e+f x]^{4/3} \operatorname{Sin}[e+f x]}{3 \left( a^2+b^2 \right)^{1/6} \left( 1+\frac{\left( -1 \right)^{1/3} b^{2/3} \operatorname{Sec}[e+f x]^{2/3}}{\left( a^2+b^2 \right)^{1/3}} \right)} - \\
 & \quad \left. \left( \sqrt{3} \left( -\frac{\left( -1 \right)^{1/6} b^{1/3} \left( a^2+b^2 \right)^{1/6} \operatorname{Sec}[e+f x]^{4/3} \operatorname{Sin}[e+f x]}{\sqrt{3}} \right) + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{5/3} \operatorname{Sin}[e+fx] \right) \right) / \right. \\
 & \left. \left( (a^2+b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+fx]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{2/3} \right) + \right. \\
 & \left. \left( \sqrt{3} \left( \frac{(-1)^{1/6} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+fx]^{4/3} \operatorname{Sin}[e+fx]}{\sqrt{3}} + \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{5/3} \operatorname{Sin}[e+fx] \right) \right) / \left( (a^2+b^2)^{1/3} + \right. \right. \\
 & \left. \left. \left. (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \operatorname{Sec}[e+fx]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e+fx]^{2/3} \right) \right) + \right. \\
 & 3 \left( \left( 14 b^2 (3 a^2 - 2 b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{13/3} \operatorname{Sin}[e+fx] \right) / \left( 3 (-1 + \operatorname{Sec}[e+fx]^2) \right. \right. \\
 & \left. \left. \left( 7 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \right. \right. \\
 & \left. \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \right. \right. \right. \\
 & \left. \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \right) \right. \\
 & \left. \left. \operatorname{Sec}[e+fx]^2 \right) (-a^2+b^2 (-1 + \operatorname{Sec}[e+fx]^2))^2 \right) + \\
 & \left( 14 (3 a^2 - 2 b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \\
 & \left. \sqrt{1 - \operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^{13/3} \operatorname{Sin}[e+fx] \right) / \left( 3 (-1 + \operatorname{Sec}[e+fx]^2) \right)^2 \\
 & \left( 7 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \right) \\
 & \left. \left. \operatorname{Sec}[e+fx]^2 \right) (-a^2+b^2 (-1 + \operatorname{Sec}[e+fx]^2)) \right) - \\
 & \left( 7 (3 a^2 - 2 b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \\
 & \left. \operatorname{Sec}[e+fx]^{1/3} \operatorname{Sin}[e+fx] \right) / \left( 3 \sqrt{1 - \operatorname{Cos}[e+fx]^2} (-1 + \operatorname{Sec}[e+fx]^2) \right) \\
 & \left( 7 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right) - \\
 & \left( 28 \left( 3 a^2-2 b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
 & \quad \left. \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^{7/3} \operatorname{Sin}[e+f x] \right) / \left( 9 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right. \\
 & \quad \left. \left( 7 \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \left( a^2+b^2 \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+f x]^2 \right) \right) \\
 & \quad \left. \left( -a^2+b^2 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right) + \frac{1}{63} b \operatorname{Sec}[e+f x]^{4/3} \\
 & \left( \frac{-7 a+7 b \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]}{\left( a^2+b^2 \right) \left( a^2+b^2-b^2 \operatorname{Sec}[e+f x]^2 \right)} - \left( 26 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^3 \right) / \left( \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right. \\
 & \quad \left. \left( 13 \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \right) \right) \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \right) \right) \right) \\
 & \operatorname{Sin}[e+f x] - \left( 7 \left( 3 a^2-2 b^2 \right) \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^{4/3} \right. \\
 & \quad \left. \left( \frac{1}{7 \left( a^2+b^2 \right)} 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+f x] + \frac{1}{7} \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \right) / \left( 3 \left( -1+\operatorname{Sec}[e+f x]^2 \right) \right) \\
 & \left( 7 \left( a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \\
 & \quad \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) + \\
 & \left( 7 (3 a^2-2 b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \sqrt{1-\operatorname{Cos}[e+f x]^2} \right. \\
 & \quad \operatorname{Sec}[e+f x]^{4/3} \left( 6 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \\
 & \quad \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \right) \\
 & \quad \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + 7 (a^2+b^2) \left( \frac{1}{7 (a^2+b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \right. \right. \\
 & \quad \left. \left. \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{1}{7} \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) + \\
 & \quad 3 \operatorname{Sec}[e+f x]^2 \left( 2 b^2 \left( \frac{1}{13 (a^2+b^2)} 28 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 3, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) + (a^2+b^2) \\
 & \quad \left( \frac{1}{13 (a^2+b^2)} 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{21}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{5}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Big) \Big) \Big) / \left( 3 (-1+\operatorname{Sec}[e+f x]^2) \right) \\
 & \left( 7 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + 3 \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+f x]^2 \right)^2 \\
 & \quad \left. (-a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) + \frac{1}{21} b \operatorname{Sec}[e+f x]^{1/3} \\
 & \left( \left( 2 b^2 \operatorname{Sec}[e+f x]^2 \left( -7 a+7 b \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x] \right) \operatorname{Tan}[e+f x] \right) \Big) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2) (a^2 + b^2 - b^2 \operatorname{Sec}[e + f x]^2)^2 \right) + \\
 & \left( 52 b^3 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \left. \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] \right) / \left( (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \\
 & \quad \left. \operatorname{Sec}[e + f x]^2 \right) (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2))^2 \Big) + \\
 & \left( 52 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \left. \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] \right) / \left( (-1 + \operatorname{Sec}[e + f x]^2)^2 \right) \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \\
 & \quad \left. \operatorname{Sec}[e + f x]^2 \right) (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \Big) - \\
 & \left( 26 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \operatorname{Sec}[e + f x] \right. \\
 & \quad \left. \operatorname{Tan}[e + f x] \right) / \left( \sqrt{1 - \operatorname{Cos}[e + f x]^2} (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right. \\
 & \quad \left. (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right) \\
 & \quad \left. \operatorname{Sec}[e + f x]^2 \right) (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \Big) - \\
 & \left( 78 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] \right. \\
 & \quad \left. \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] \right) / \left( (-1 + \operatorname{Sec}[e + f x]^2) \right) \\
 & \left( 13 (a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
& \quad \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \\
& \quad \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) + \\
& \left( \frac{7 b \operatorname{Sin}[e+f x]}{\sqrt{1-\operatorname{Cos}[e+f x]^2}} + 7 b \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x] \operatorname{Tan}[e+f x] \right) / \\
& \quad \left( (a^2+b^2) (a^2+b^2-b^2 \operatorname{Sec}[e+f x]^2) \right) - \\
& \left( 26 b \sqrt{1-\operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^3 \left( \frac{1}{13 (a^2+b^2)} 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \right. \right. \right. \\
& \quad \left. \left. \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \right. \right. \\
& \quad \left. \left. \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Big) / \\
& \left( (-1+\operatorname{Sec}[e+f x]^2) \left( 13 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+f x]^2 \left( -a^2+b^2 (-1+\operatorname{Sec}[e+f x]^2) \right) \Big) + \\
& \left( 26 b \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \sqrt{1-\operatorname{Cos}[e+f x]^2} \right. \\
& \quad \left. \operatorname{Sec}[e+f x]^3 \left( 6 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \right. \right. \\
& \quad \left. \left. (a^2+b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right) \right) \\
& \quad \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + 13 (a^2+b^2) \left( \frac{1}{13 (a^2+b^2)} 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \right. \right. \\
& \quad \left. \left. \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] + \right. \\
& \quad \left. \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
& \quad \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) + 3 \operatorname{Sec}[e+f x]^2 \\
& \left( 2 b^2 \left( \left( 52 b^2 \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{1}{2}, 3, \frac{25}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \right. \right. \\
& \quad \left. \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \Big) / (19 (a^2+b^2)) + \frac{13}{19} \operatorname{AppellF1} \left[ \frac{19}{6}, \frac{3}{2}, 2, \right.
\end{aligned}$$



$$\begin{aligned}
 & \frac{7 a b}{(a^2 + b^2)^2 f (d \operatorname{Sec}[e + f x])^{1/3}} - \frac{7 a b^{4/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{2 \sqrt{3} (a^2 + b^2)^{13/6} f (d \operatorname{Sec}[e + f x])^{1/3}} + \\
 & \frac{7 a b^{4/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{2 \sqrt{3} (a^2 + b^2)^{13/6} f (d \operatorname{Sec}[e + f x])^{1/3}} - \\
 & \frac{7 a b^{4/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{1/6}}{3 (a^2 + b^2)^{13/6} f (d \operatorname{Sec}[e + f x])^{1/3}} + \\
 & \left(7 a b^{4/3} \operatorname{Log}\left[(a^2 + b^2)^{1/3} - b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{1/6}\right) / \left(12 (a^2 + b^2)^{13/6} f (d \operatorname{Sec}[e + f x])^{1/3}\right) - \\
 & \left(7 a b^{4/3} \operatorname{Log}\left[(a^2 + b^2)^{1/3} + b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{1/6}\right) / \left(12 (a^2 + b^2)^{13/6} f (d \operatorname{Sec}[e + f x])^{1/3}\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2, \frac{7}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2\right] (\operatorname{Sec}[e + f x]^2)^{1/6} \operatorname{Tan}[e + f x]\right) / \\
 & \quad \left(a^2 f (d \operatorname{Sec}[e + f x])^{1/3}\right) + \\
 & \left(b^2 \operatorname{AppellF1}\left[\frac{3}{2}, 2, \frac{7}{6}, \frac{5}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2\right] (\operatorname{Sec}[e + f x]^2)^{1/6} \operatorname{Tan}[e + f x]^3\right) / \\
 & \quad \left(3 a^4 f (d \operatorname{Sec}[e + f x])^{1/3}\right) - \frac{a b}{(a^2 + b^2) f (d \operatorname{Sec}[e + f x])^{1/3} (a^2 - b^2 \operatorname{Tan}[e + f x]^2)}
 \end{aligned}$$

Result (type 6, 56289 leaves): Display of huge result suppressed!

**Problem 639: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d \operatorname{Sec}[e + f x])^{5/3} (a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 6, 717 leaves, 19 steps):



$$\begin{aligned}
 & \frac{11 a b}{5 (a^2 + b^2)^2 f (d \operatorname{Sec}[e + f x])^{5/3}} + \frac{11 a b^{8/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} - \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{2 \sqrt{3} (a^2 + b^2)^{17/6} f (d \operatorname{Sec}[e + f x])^{5/3}} - \\
 & \frac{11 a b^{8/3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2 b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{\sqrt{3} (a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{2 \sqrt{3} (a^2 + b^2)^{17/6} f (d \operatorname{Sec}[e + f x])^{5/3}} - \\
 & \frac{11 a b^{8/3} \operatorname{ArcTanh}\left[\frac{b^{1/3} (\operatorname{Sec}[e + f x]^2)^{1/6}}{(a^2 + b^2)^{1/6}}\right] (\operatorname{Sec}[e + f x]^2)^{5/6}}{3 (a^2 + b^2)^{17/6} f (d \operatorname{Sec}[e + f x])^{5/3}} + \\
 & \left(11 a b^{8/3} \operatorname{Log}\left[(a^2 + b^2)^{1/3} - b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{5/6}\right) / \left(12 (a^2 + b^2)^{17/6} f (d \operatorname{Sec}[e + f x])^{5/3}\right) - \\
 & \left(11 a b^{8/3} \operatorname{Log}\left[(a^2 + b^2)^{1/3} + b^{1/3} (a^2 + b^2)^{1/6} (\operatorname{Sec}[e + f x]^2)^{1/6} + b^{2/3} (\operatorname{Sec}[e + f x]^2)^{1/3}\right] \right. \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{5/6}\right) / \left(12 (a^2 + b^2)^{17/6} f (d \operatorname{Sec}[e + f x])^{5/3}\right) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2, \frac{11}{6}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2\right] (\operatorname{Sec}[e + f x]^2)^{5/6} \operatorname{Tan}[e + f x]\right) / \\
 & \quad \left(a^2 f (d \operatorname{Sec}[e + f x])^{5/3}\right) + \\
 & \left(b^2 \operatorname{AppellF1}\left[\frac{3}{2}, 2, \frac{11}{6}, \frac{5}{2}, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2}, -\operatorname{Tan}[e + f x]^2\right] (\operatorname{Sec}[e + f x]^2)^{5/6} \operatorname{Tan}[e + f x]^3\right) / \\
 & \quad \left(3 a^4 f (d \operatorname{Sec}[e + f x])^{5/3}\right) - \frac{a b}{(a^2 + b^2) f (d \operatorname{Sec}[e + f x])^{5/3} (a^2 - b^2 \operatorname{Tan}[e + f x]^2)}
 \end{aligned}$$

Result (type 6, 7441 leaves):

$$\begin{aligned}
 & \left(\frac{1}{12 (a - i b)^2 (a + i b)^2 (a^2 + b^2)^{5/6}}\right. \\
 & \quad 11 (-1)^{5/6} a b^{8/3} \left(-2 \operatorname{ArcTan}\left[\sqrt{3} - \frac{2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}}\right] + \right. \\
 & \quad \left. 2 \operatorname{ArcTan}\left[\sqrt{3} + \frac{2 (-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}}\right] + \right. \\
 & \quad \left. 4 \operatorname{ArcTan}\left[\frac{(-1)^{1/6} b^{1/3} \operatorname{Sec}[e + f x]^{1/3}}{(a^2 + b^2)^{1/6}}\right] - \sqrt{3} \operatorname{Log}\left[(a^2 + b^2)^{1/3} - \right. \right. \\
 & \quad \left. \left. (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3}\right] + \sqrt{3} \operatorname{Log}\left[ \right. \right. \\
 & \quad \left. \left. (a^2 + b^2)^{1/3} + (-1)^{1/6} \sqrt{3} b^{1/3} (a^2 + b^2)^{1/6} \operatorname{Sec}[e + f x]^{1/3} + (-1)^{1/3} b^{2/3} \operatorname{Sec}[e + f x]^{2/3}\right]\right) + \\
 & \quad \frac{1}{35 (a^2 + b^2)^2 \operatorname{Sec}[e + f x]^{5/3}} \left(-\left(\left(49 (6 a^6 + 51 a^4 b^2 + 29 a^2 b^4 - 16 b^6) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \sqrt{1 - \operatorname{Cos}[e + f x]^2} \operatorname{Sec}[e + f x]^3\right)\right) / \\
 & \quad \left(\left(-1 + \operatorname{Sec}[e + f x]^2\right) \left(7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+fx]^2 \left( -a^2+b^2 (-1+\operatorname{Sec}[e+fx]^2) \right) \Big) \Big) + \\
 & \frac{1}{a^2-b^2 (-1+\operatorname{Sec}[e+fx]^2)} \left( 42 a^3 b + 42 a b^3 + 21 a^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx] - \right. \\
 & 21 b^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx] - 77 a b^3 \operatorname{Sec}[e+fx]^2 - \\
 & 21 a^2 b^2 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + 56 b^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \\
 & \left. \left( 26 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^5 \right) / \left( (-1+\operatorname{Sec}[e+fx]^2) \left( 13 (a^2+b^2) \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2+b^2) \operatorname{AppellF1} \left[ \frac{13}{6}, \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+fx]^2 \right) \right) \Big) \Big) / \\
 & \left( f (d \operatorname{Sec}[e+fx])^{5/3} (a+b \operatorname{Tan}[e+fx])^2 \left( -\frac{1}{21 (a^2+b^2)^2 \operatorname{Sec}[e+fx]^{2/3}} \right. \right. \\
 & \left. \left( - \left( \left( 49 (6 a^6 + 51 a^4 b^2 + 29 a^2 b^4 - 16 b^6) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 \right) / \left( (-1+\operatorname{Sec}[e+fx]^2) \right. \right. \right. \\
 & \left. \left( 7 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + \right. \right. \\
 & \left. 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+fx]^2, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2} \right] \right) \operatorname{Sec}[e+fx]^2 \right) \right) \Big) \Big) + \\
 & \frac{1}{a^2-b^2 (-1+\operatorname{Sec}[e+fx]^2)} \\
 & \left( 42 a^3 b + 42 a b^3 + 21 a^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx] - 21 b^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \right. \\
 & \left. \operatorname{Sec}[e+fx] - 77 a b^3 \operatorname{Sec}[e+fx]^2 - 21 a^2 b^2 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \right. \\
 & \left. 56 b^4 \sqrt{1-\operatorname{Cos}[e+fx]^2} \operatorname{Sec}[e+fx]^3 + \left( 26 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \\
 & \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx]^5 \Big/ \left( (-1+\text{Sec}[e+fx]^2) \left( 13(a^2+b^2) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + 3 \left( 2b^2 \text{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + (a^2+b^2) \text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \text{Sec}[e+fx]^2 \right) \right) \Big) \\
 & \text{Sin}[e+fx] + \frac{1}{12(a-ib)^2(a+ib)^2(a^2+b^2)^{5/6}} 11(-1)^{5/6} a b^{8/3} \\
 & \left( \frac{4(-1)^{1/6} b^{1/3} \text{Sec}[e+fx]^{4/3} \text{Sin}[e+fx]}{3(a^2+b^2)^{1/6} \left( 1 + \left( \sqrt{3} - \frac{2(-1)^{1/6} b^{1/3} \text{Sec}[e+fx]^{1/3}}{(a^2+b^2)^{1/6}} \right)^2 \right)} + \right. \\
 & \quad \frac{4(-1)^{1/6} b^{1/3} \text{Sec}[e+fx]^{4/3} \text{Sin}[e+fx]}{3(a^2+b^2)^{1/6} \left( 1 + \left( \sqrt{3} + \frac{2(-1)^{1/6} b^{1/3} \text{Sec}[e+fx]^{1/3}}{(a^2+b^2)^{1/6}} \right)^2 \right)} + \\
 & \quad \frac{4(-1)^{1/6} b^{1/3} \text{Sec}[e+fx]^{4/3} \text{Sin}[e+fx]}{3(a^2+b^2)^{1/6} \left( 1 + \frac{(-1)^{1/3} b^{2/3} \text{Sec}[e+fx]^{2/3}}{(a^2+b^2)^{1/3}} \right)} - \\
 & \quad \left( \sqrt{3} \left( -\frac{(-1)^{1/6} b^{1/3} (a^2+b^2)^{1/6} \text{Sec}[e+fx]^{4/3} \text{Sin}[e+fx]}{\sqrt{3}} + \right. \right. \\
 & \quad \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \text{Sec}[e+fx]^{5/3} \text{Sin}[e+fx] \right) \right) \Big/ \\
 & \quad \left( (a^2+b^2)^{1/3} - (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \text{Sec}[e+fx]^{1/3} + (-1)^{1/3} b^{2/3} \text{Sec}[e+fx]^{2/3} \right) + \\
 & \quad \left( \sqrt{3} \left( \frac{(-1)^{1/6} b^{1/3} (a^2+b^2)^{1/6} \text{Sec}[e+fx]^{4/3} \text{Sin}[e+fx]}{\sqrt{3}} + \right. \right. \\
 & \quad \left. \left. \frac{2}{3} (-1)^{1/3} b^{2/3} \text{Sec}[e+fx]^{5/3} \text{Sin}[e+fx] \right) \right) \Big/ \left( (a^2+b^2)^{1/3} + \right. \\
 & \quad \left. (-1)^{1/6} \sqrt{3} b^{1/3} (a^2+b^2)^{1/6} \text{Sec}[e+fx]^{1/3} + (-1)^{1/3} b^{2/3} \text{Sec}[e+fx]^{2/3} \right) \Big) + \\
 & \frac{1}{35(a^2+b^2)^2 \text{Sec}[e+fx]^{5/3}} \left( \left( 98b^2(6a^6+51a^4b^2+29a^2b^4-16b^6) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] \Big/ \left( (-1 + \operatorname{Sec}[e + f x]^2) \right. \\
 & \left. \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \\
 & \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2))^2 \right) + \left( 98 (6 a^6 + 51 a^4 b^2 + 29 a^2 b^4 - 16 b^6) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right. \\
 & \left. \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^5 \operatorname{Tan}[e + f x] \Big/ \left( (-1 + \operatorname{Sec}[e + f x]^2)^2 \right. \right. \\
 & \left. \left. \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \right) \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \right) - \left( 49 (6 a^6 + 51 a^4 b^2 + 29 a^2 b^4 - 16 b^6) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \operatorname{Sec}[e + f x] \right. \\
 & \left. \operatorname{Tan}[e + f x] \Big/ \left( \sqrt{1 - \cos[e + f x]^2} (-1 + \operatorname{Sec}[e + f x]^2) \right. \right. \\
 & \left. \left. \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \right) \right) \\
 & \left. (-a^2 + b^2 (-1 + \operatorname{Sec}[e + f x]^2)) \right) - \left( 147 (6 a^6 + 51 a^4 b^2 + 29 a^2 b^4 - 16 b^6) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] \right. \\
 & \left. \sqrt{1 - \cos[e + f x]^2} \operatorname{Sec}[e + f x]^3 \operatorname{Tan}[e + f x] \Big/ \left( (-1 + \operatorname{Sec}[e + f x]^2) \right. \right. \\
 & \left. \left. \left( 7 (a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. 3 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \operatorname{Sec}[e + f x]^2, \frac{b^2 \operatorname{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \right. \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \text{Sec}[e+fx]^2 \right) \\
 & \left. (-a^2+b^2(-1+\text{Sec}[e+fx]^2))\right) + \frac{1}{(a^2-b^2(-1+\text{Sec}[e+fx]^2))^2} \\
 & 2b^2 \text{Sec}[e+fx]^2 \left( 42a^3b + 42ab^3 + 21a^4 \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx] - \right. \\
 & 21b^4 \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx] - 77ab^3 \text{Sec}[e+fx]^2 - \\
 & 21a^2b^2 \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 + 56b^4 \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 + \\
 & \left. \left( 26b^2(-3a^4+5a^2b^2+8b^4) \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right. \right. \\
 & \left. \left. \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx]^5 \right) / \left( (-1+\text{Sec}[e+fx]^2) \left( 13(a^2+b^2) \text{AppellF1}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + 3 \left( 2b^2 \text{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 2, \frac{19}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + (a^2+b^2) \text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 1, \right. \right. \right. \\
 & \left. \left. \left. \frac{19}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \text{Sec}[e+fx]^2 \right) \right) \left. \right) \text{Tan}[e+fx] - \\
 & \left( 49(6a^6+51a^4b^2+29a^2b^4-16b^6) \sqrt{1-\text{Cos}[e+fx]^2} \text{Sec}[e+fx]^3 \right. \\
 & \left. \left( \frac{1}{7(a^2+b^2)} 2b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \text{Sec}[e+fx]^2 \right. \right. \\
 & \left. \left. \text{Tan}[e+fx] + \frac{1}{7} \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right. \right. \\
 & \left. \left. \text{Sec}[e+fx]^2 \text{Tan}[e+fx] \right) \right) / \left( (-1+\text{Sec}[e+fx]^2) \right. \\
 & \left( 7(a^2+b^2) \text{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \\
 & 3 \left( 2b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + (a^2+b^2) \right. \\
 & \left. \left. \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \text{Sec}[e+fx]^2 \right) \\
 & \left. (-a^2+b^2(-1+\text{Sec}[e+fx]^2)) \right) + \left( 49(6a^6+51a^4b^2+29a^2b^4-16b^6) \right. \\
 & \text{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \sqrt{1-\text{Cos}[e+fx]^2} \\
 & \text{Sec}[e+fx]^3 \left( 6 \left( 2b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] + \right. \right. \\
 & \left. \left. (a^2+b^2) \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e+fx]^2, \frac{b^2 \text{Sec}[e+fx]^2}{a^2+b^2}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + 7 (a^2 + b^2) \left( \frac{1}{7 (a^2 + b^2)} 2 b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \right. \right. \\
 & \quad \left. \left. \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{1}{7} \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \\
 & 3 \text{Sec}[e + f x]^2 \left( 2 b^2 \left( \frac{1}{13 (a^2 + b^2)} 28 b^2 \text{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 3, \frac{19}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{7}{13} \text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \right. \right. \right. \\
 & \quad \left. \left. \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + (a^2 + b^2) \\
 & \quad \left( \frac{1}{13 (a^2 + b^2)} 14 b^2 \text{AppellF1}\left[\frac{13}{6}, \frac{3}{2}, 2, \frac{19}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \right. \\
 & \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{21}{13} \text{AppellF1}\left[\frac{13}{6}, \frac{5}{2}, 1, \frac{19}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) \Bigg) \Bigg) / \left( (-1 + \text{Sec}[e + f x]^2) \right. \\
 & \quad \left. \left( 7 (a^2 + b^2) \text{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] + 3 \right. \right. \\
 & \quad \left. \left( 2 b^2 \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] + (a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{7}{6}, \frac{3}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \right) \text{Sec}[e + f x]^2 \right)^2 \\
 & \quad \left. (-a^2 + b^2 (-1 + \text{Sec}[e + f x]^2)) \right) + \frac{1}{a^2 - b^2 (-1 + \text{Sec}[e + f x]^2)} \\
 & \left( \frac{21 a^4 \text{Sin}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} - \frac{21 b^4 \text{Sin}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} - \frac{21 a^2 b^2 \text{Sec}[e + f x] \text{Tan}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} + \right. \\
 & \quad \frac{56 b^4 \text{Sec}[e + f x] \text{Tan}[e + f x]}{\sqrt{1 - \text{Cos}[e + f x]^2}} + 21 a^4 \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x] \text{Tan}[e + f x] - \\
 & \quad 21 b^4 \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x] \text{Tan}[e + f x] - 154 a b^3 \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \\
 & \quad 63 a^2 b^2 \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 \text{Tan}[e + f x] + \\
 & \quad 168 b^4 \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^3 \text{Tan}[e + f x] - \\
 & \quad \left. \left( 52 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{1 - \text{Cos}[e + f x]^2} \text{Sec}[e + f x]^7 \text{Tan}[e + f x] \right) \Bigg) / \left( (-1 + \text{Sec}[e + f x]^2) \right)^2 \\
 & \quad \left( 13 (a^2 + b^2) \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \text{Sec}[e + f x]^2, \frac{b^2 \text{Sec}[e + f x]^2}{a^2 + b^2}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right) + \\
 & \left( 26 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^3 \operatorname{Tan}[e+f x] \right) / \left( \sqrt{1 - \operatorname{Cos}[e+f x]^2} (-1 + \operatorname{Sec}[e+f x]^2) \right) \\
 & \left( 13 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right) + \\
 & \left( 130 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
 & \quad \left. \sqrt{1 - \operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^5 \operatorname{Tan}[e+f x] \right) / \left( (-1 + \operatorname{Sec}[e+f x]^2) \right) \\
 & \left( 13 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right) + \\
 & \left( 26 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \sqrt{1 - \operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^5 \left( \frac{1}{13 (a^2+b^2)} \right. \right. \\
 & \quad 14 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \\
 & \quad \left. \operatorname{Tan}[e+f x] + \frac{7}{13} \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) / \left( (-1 + \operatorname{Sec}[e+f x]^2) \right) \\
 & \left( 13 (a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + \right. \\
 & \quad 3 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] + (a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{3}{2}, 1, \frac{19}{6}, \operatorname{Sec}[e+f x]^2, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \operatorname{Sec}[e+f x]^2 \right) - \\
 & \left( 26 b^2 (-3 a^4 + 5 a^2 b^2 + 8 b^4) \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \operatorname{Sec}[e+f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2} \right] \sqrt{1 - \operatorname{Cos}[e+f x]^2} \operatorname{Sec}[e+f x]^5 \left( 6 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, \right. \right. \right. \right.
 \end{aligned}$$





$$\frac{a b (2+m) (d \operatorname{Sec}[e+f x])^m}{f m (1+m)} +$$

$$\left( d (b^2 - a^2 (1+m)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-m}{2}, \frac{3-m}{2}, \operatorname{Cos}[e+f x]^2\right] (d \operatorname{Sec}[e+f x])^{-1+m} \right.$$

$$\left. \operatorname{Sin}[e+f x] \right) / \left( f (1-m) (1+m) \sqrt{\operatorname{Sin}[e+f x]^2} \right) + \frac{b (d \operatorname{Sec}[e+f x])^m (a+b \operatorname{Tan}[e+f x])}{f (1+m)}$$

Result (type 6, 14 694 leaves):

$$\left( \operatorname{Sec}[e+f x]^{-2-m} (d \operatorname{Sec}[e+f x])^m \right.$$

$$\left. (a^2 \operatorname{Sec}[e+f x]^m + 2 a b \operatorname{Sec}[e+f x]^{1+m} \operatorname{Sin}[e+f x] + b^2 \operatorname{Sec}[e+f x]^{2+m} \operatorname{Sin}[e+f x]^2) \right.$$

$$\left( \left( 3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \right. \right.$$

$$\left. \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} \right)^{-2+m} \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^{-1+m} \right) / \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^2 \right.$$

$$\left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + 2 \left( (-1+m) \right. \right.$$

$$\left. \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right.$$

$$\left. \left. 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right) -$$

$$\left( 3 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \right.$$

$$\left. \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} \right)^{-2+m} \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^{-1+m} \right) / \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^2 \right.$$

$$\left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + 2 \left( (-1+m) \right. \right.$$

$$\left. \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right.$$

$$\left. \left. 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right) -$$

$$\left( b^2 \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \right.$$

$$\left. \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2} \right)^{-1+m} \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^m \right) / \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right)^2 \right.$$

$$\left. \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right.$$

$$\begin{aligned}
 & (1+m, 1-m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2) + (1+m) \operatorname{AppellF1}[\frac{3}{2}, 2+m, \\
 & m, -m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] \tan[\frac{1}{2}(e+fx)]^2) + \\
 & \left( 2 b^2 \operatorname{AppellF1}[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] \right. \\
 & \left. \tan[\frac{1}{2}(e+fx)] \left( \frac{1}{1-\tan[\frac{1}{2}(e+fx)]^2} \right)^m \left( 1+\tan[\frac{1}{2}(e+fx)]^2 \right)^m \right) / \\
 & \left( \left( -1+\tan[\frac{1}{2}(e+fx)]^2 \right)^2 \left( \operatorname{AppellF1}[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan[\frac{1}{2}(e+fx)]^2, \right. \right. \\
 & \left. \left. -\tan[\frac{1}{2}(e+fx)]^2 \right] + \frac{2}{3} \left( m \operatorname{AppellF1}[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, \right. \right. \\
 & \left. \left. -\tan[\frac{1}{2}(e+fx)]^2 \right] + (2+m) \operatorname{AppellF1}[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2 \right] \right) \tan[\frac{1}{2}(e+fx)]^2) + \\
 & \left( 2 a b \operatorname{AppellF1}[1, m, 1-m, 2, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] \tan[\frac{1}{2}(e+fx)]^2 \right. \\
 & \left. \left( \frac{1}{1-\tan[\frac{1}{2}(e+fx)]^2} \right)^{-2+m} \left( 1+\tan[\frac{1}{2}(e+fx)]^2 \right)^{-1+m} \right) / \left( \left( -1+\tan[\frac{1}{2}(e+fx)]^2 \right)^2 \right. \\
 & \left( 2 \operatorname{AppellF1}[1, m, 1-m, 2, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] + \right. \\
 & \left. \left( (-1+m) \operatorname{AppellF1}[2, m, 2-m, 3, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] + m \operatorname{AppellF1}[ \right. \right. \\
 & \left. \left. 2, 1+m, 1-m, 3, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2 \right] \right) \tan[\frac{1}{2}(e+fx)]^2) + \\
 & \left( 2 a b \operatorname{AppellF1}[1, 1+m, -m, 2, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] \right. \\
 & \left. \tan[\frac{1}{2}(e+fx)]^2 \left( \frac{1}{1-\tan[\frac{1}{2}(e+fx)]^2} \right)^{-1+m} \right. \\
 & \left. \left( 1+\tan[\frac{1}{2}(e+fx)]^2 \right)^m \right) / \left( \left( -1+\tan[\frac{1}{2}(e+fx)]^2 \right)^2 \right. \\
 & \left( 2 \operatorname{AppellF1}[1, 1+m, -m, 2, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] + \right. \\
 & \left. \left( m \operatorname{AppellF1}[2, 1+m, 1-m, 3, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] + \right. \right. \\
 & \left. \left. (1+m) \operatorname{AppellF1}[2, 2+m, -m, 3, \tan[\frac{1}{2}(e+fx)]^2, -\tan[\frac{1}{2}(e+fx)]^2] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
& \text{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[\frac{3}{2}, \right. \\
& \quad \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \\
& \left( 6 b^2 \text{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \right. \\
& \quad \left. \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \right) / \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^3\right) \right. \\
& \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left((-1+m) \right. \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) + \\
& \left( 3 a^2 \text{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \right. \\
& \quad \left. \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \right) / \left(2 \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \right. \\
& \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left((-1+m) \right. \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) - \\
& \left( 3 b^2 \text{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \right. \\
& \quad \left. \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \right) / \left(2 \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \right.
\end{aligned}$$



$$\begin{aligned}
& \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \Bigg/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \right. \right. \\
& \quad \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
& \quad \left. \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) - \\
& \left( 3 b^2 (-2+m) \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-1+m} \right. \\
& \left. \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \Bigg/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \right. \\
& \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) - \\
& \left( b^2 m \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-1+m} \right. \\
& \left. \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \Bigg/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \right. \\
& \left. \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) + \\
& \left( 2 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right.
\end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m} \\
 & \left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^m \Big/ \left(\left(-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^3\right. \\
 & \left(\text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left.(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left.-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \\
 & \left(b^2 \text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m} \\
 & \left. \left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^m \Big/ \left(2\left(-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \right. \\
 & \left(\text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left.(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left.\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) - \left(b^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left.\frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} (1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left.\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \\
 & \left(\frac{1}{1-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m} \left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^m \Big/ \left(\left(-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \\
 & \left(\text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \\
& \left( b^2 (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
& \quad \left. \left( 1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^m \right) / \left( \left( -1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
& \quad \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) + \\
& \left( 2 b^2 m \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
& \quad \left. \left( 1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \right) / \left( \left( -1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
& \quad \left( \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) - \\
& \left( 4 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^m
\end{aligned}$$



$$\begin{aligned}
 & \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^m \Big/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^3 \right. \\
 & \left( \text{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( m \text{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (2+m) \text{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) + \\
 & \left( b^2 \text{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^m \Big/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \right. \\
 & \left. \left( \text{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \frac{2}{3} \left( m \text{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (2+m) \text{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \Big) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) + \left( 2 b^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left( \frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} (2+m) \text{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big) \\
 & \left( \frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^m \Big/ \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
 & \left( \text{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( m \text{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (2+m) \text{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
& \left(2b^2m\operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]^2\left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{1+m} \\
& \left.\left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^m\right)\right/\left(\left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \frac{2}{3}\left(m\operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& (2+m)\operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
& \left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
& \left(2ab(-1+m)\operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]^3\left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \\
& \left.\left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-2+m}\right)\right/\left(\left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \\
& \left(2\operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left.\left((-1+m)\operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m\operatorname{AppellF1}\left[ \right. \right. \right. \\
& \left.\left.\left.2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) - \\
& \left(4ab\operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]^3\left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \\
& \left.\left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m}\right)\right/\left(\left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^3\right)
\end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \left. 2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \left. \right) + \\
 & \left( 2 a b \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \left( \frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-2+m} \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
 & \quad \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \quad \left. \left. 2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \left. \right) + \\
 & \left( 2 a b \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -\frac{1}{2} (1-m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \\
 & \quad \left( \frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-2+m} \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
 & \quad \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \quad \left. \left. 2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \left. \right) + \\
 & \left( 2 a b (-2+m) \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^3 \left( \frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-1+m} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \Big/ \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \\
& \left(2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. \left((-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
& \left(2 a b m \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^3 \left(\frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m}\right) \\
& \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \Big/ \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \\
& \left(2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. \left(m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left.(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - \\
& \left(4 a b \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^3 \left(\frac{1}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m}\right) \\
& \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^m \Big/ \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^3\right) \\
& \left(2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. \left(m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left.(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right) +
\end{aligned}$$

$$\begin{aligned}
 & \left( 2 a b \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+f x)\right]^2}\right)^{-1+m} \\
 & \quad \left.\left(1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^m\right) / \left(\left(-1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^2\right) \right. \\
 & \quad \left(2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left(m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left.(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right]\right) \\
 & \quad \left.\tan\left[\frac{1}{2}(e+f x)\right]^2\right) + \left(2 a b \tan\left[\frac{1}{2}(e+f x)\right]^2 \right. \\
 & \quad \left(\frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right] + \frac{1}{2}(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \right. \\
 & \quad \left.\tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right] \left. \right) \\
 & \quad \left.\left(\frac{1}{1-\tan\left[\frac{1}{2}(e+f x)\right]^2}\right)^{-1+m} \left(1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^m\right) / \left(\left(-1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^2\right) \right. \\
 & \quad \left(2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left(m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left.(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+f x)\right]^2, \right. \right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{2}(e+f x)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+f x)\right]^2\right) + \\
 & \left( 2 a b (-1+m) \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+f x)\right]^2, -\tan\left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \tan\left[\frac{1}{2}(e+f x)\right]^3 \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+f x)\right]^2}\right)^m \\
 & \quad \left.\left(1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^m\right) / \left(\left(-1+\tan\left[\frac{1}{2}(e+f x)\right]^2\right)^2\right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) - \\
 & \left( 3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-2+m} \left( 1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+m} \\
 & \quad \left( 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \\
 & \quad \quad 3 \left( -\frac{1}{3}(1-m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \quad \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \right. \\
 & \quad \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & \quad 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+m) \left( -\frac{3}{5}(2-m) \operatorname{AppellF1}\left[\frac{5}{2}, m, 3-m, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \quad \left. \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + m \left( -\frac{3}{5}(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, \right. \right. \\
 & \quad \quad \left. \left. 2-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \\
 & \left( \left( -1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \right. \\
 & \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + \\
 & \left(3 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \tan\left[\frac{1}{2}(e+fx)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-2+m} \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+m} \\
 & \left. \left(2\left((-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \left. m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \left. 3\left(-\frac{1}{3}(1-m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) + \right. \\
 & \left. 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left((-1+m) \left(-\frac{3}{5}(2-m) \operatorname{AppellF1}\left[\frac{5}{2}, m, 3-m, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \left. \left. \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) + m \left(-\frac{3}{5}(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, \right. \right. \right. \\
 & \left. \left. 2-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right)\right) \Big/ \\
 & \left(\left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2\left((-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( b^2 \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \tan\left[\frac{1}{2}(e+fx)\right] \left( \frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^{-1+m} \left( 1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^m \\
& \quad \left( \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \\
& \quad \quad \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
& \quad \quad \left. \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \quad \quad \left. \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
& \quad \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{2}{3} \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
& \quad \quad \left( m \left( -\frac{3}{5}(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \quad \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \right. \\
& \quad \quad \quad \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \left. \right) \left. \right) + \\
& \quad \quad (1+m) \left( \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
& \quad \quad \quad \left. \frac{3}{5}(2+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3+m, -m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \quad \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \Big/ \left( \left( -1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \\
& \quad \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \frac{2}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
& \quad \quad \left. \left. 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \quad \left( 2 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \quad \tan\left[\frac{1}{2}(e+fx)\right] \left( \frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \left( 1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^m
\end{aligned}$$



$$\begin{aligned}
 & \left( \frac{1}{3} m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \\
 & \quad \frac{2}{3} \left( m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{2}{3} \tan \left[ \frac{1}{2} (e+fx) \right]^2 \\
 & \quad \left( m \left( -\frac{3}{5} (1-m) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+m, 2-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} (2+m) \operatorname{AppellF1} \left[ \frac{5}{2}, 3+m, 1-m, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) + \\
 & \quad (2+m) \left( \frac{3}{5} m \operatorname{AppellF1} \left[ \frac{5}{2}, 3+m, 1-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \\
 & \quad \left. \frac{3}{5} (3+m) \operatorname{AppellF1} \left[ \frac{5}{2}, 4+m, -m, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) \Bigg) / \left( \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 \right) \\
 & \quad \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \frac{2}{3} \left( m \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 2+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 3+m, -m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \Bigg) - \\
 & \quad \left( 2 a b \operatorname{AppellF1} \left[ 1, m, 1-m, 2, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (e+fx) \right]^2} \right)^{-2+m} \right. \\
 & \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-1+m} \right. \\
 & \quad \left. \left( \left( (-1+m) \operatorname{AppellF1} \left[ 2, m, 2-m, 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \right. \\
 & \quad \left. \left. m \operatorname{AppellF1} \left[ 2, 1+m, 1-m, 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 2\left(-\frac{1}{2}(1-m) \text{AppellF1}\left[2, m, 2-m, 3, \right.\right. \\
 & \quad \left.\left.\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left.\frac{1}{2}m \text{AppellF1}\left[2, 1+m, 1-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \left(\left(-1+m\right)\left(-\frac{2}{3}(2-m) \text{AppellF1}\left[3, m, 3-m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{2}{3}m \text{AppellF1}\left[3, 1+m, 2-m, 4, \right.\right. \right. \\
 & \quad \left.\left.\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + \\
 & \quad m\left(-\frac{2}{3}(1-m) \text{AppellF1}\left[3, 1+m, 2-m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
 & \quad \left.\left.-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left.\frac{2}{3}(1+m) \text{AppellF1}\left[3, 2+m, 1-m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right) \Big/ \left(\left(-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2\right)^2 \\
 & \left(2 \text{AppellF1}\left[1, m, 1-m, 2, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \left((-1+m) \right.\right. \\
 & \quad \left.\left.\text{AppellF1}\left[2, m, 2-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[2, \right.\right. \right. \\
 & \quad \left.\left.\left.1+m, 1-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 - \\
 & \left(2ab \text{AppellF1}\left[1, 1+m, -m, 2, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left.\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(\frac{1}{1-\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m} \right. \\
 & \quad \left.\left(1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^m \right. \\
 & \quad \left.\left(\left(m \text{AppellF1}\left[2, 1+m, 1-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \right. \\
 & \quad \left.\left.\left(1+m\right) \text{AppellF1}\left[2, 2+m, -m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left.2\left(\frac{1}{2}m \text{AppellF1}\left[2, 1+m, 1-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{2}(1+m) \text{AppellF1}\left[2, 2+m, -m, 3, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + \\
 & \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( m \left( -\frac{2}{3}(1-m) \text{AppellF1}\left[3, 1+m, 2-m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{3}(1+m) \text{AppellF1}\left[3, 2+m, 1-m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + (1+m) \left( \frac{2}{3} m \text{AppellF1}\left[3, 2+m, 1-m, 4, \right. \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{3}(2+m) \text{AppellF1}\left[3, 3+m, -m, 4, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \\
 & \left( 2 \text{AppellF1}\left[1, 1+m, -m, 2, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( m \text{AppellF1}\left[ \right. \right. \right. \\
 & \quad \left. \left. 2, 1+m, 1-m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + (1+m) \text{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 2+m, -m, 3, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left. \right) \left. \right)
 \end{aligned}$$

**Problem 642: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (d \text{Sec}[e+fx])^m (a+b \text{Tan}[e+fx]) dx$$

Optimal (type 5, 93 leaves, 3 steps):

$$\frac{b (d \text{Sec}[e+fx])^m}{f m} - \frac{\left( a d \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-m}{2}, \frac{3-m}{2}, \text{Cos}[e+fx]^2\right] (d \text{Sec}[e+fx])^{-1+m} \text{Sin}[e+fx] \right)}{\left( f (1-m) \sqrt{\text{Sin}[e+fx]^2} \right)}$$

Result (type 6, 7252 leaves):

$$\left( 2 \text{Sec}[e+fx]^{-1+m} (d \text{Sec}[e+fx])^m (a \text{Sec}[e+fx]^m + b \text{Sec}[e+fx]^{1+m} \text{Sin}[e+fx]) \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right)$$

$$\begin{aligned}
& \left( \frac{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \left( \left( 3 a \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right) / \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \right. \right. \right. \\
& \quad \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \left. 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \quad b \tan\left[\frac{1}{2}(e+fx)\right] \left( \left( \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right) / \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \\
& \quad \left. \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
& \quad \quad \left. \left. m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) - \\
& \quad \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] / \\
& \quad \left( 2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
& \quad \quad \left. \left. 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (1+m) \operatorname{AppellF1}\left[2, \right. \right. \right. \\
& \quad \quad \left. \left. \left. 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \\
& \left. \left( a + b \tan[e+fx] \right) \right) / \left( f \left( a \cos[e+fx] + b \sin[e+fx] \right) \right) \\
& \left( -1 + \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
& \left( -\frac{1}{\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2} 2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \right. \right. \\
& \quad \left. \left( \left( 3 a \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
& \quad \quad \left. \left. \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right) / \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \Big] + 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big] + \\
 & b \tan\left[\frac{1}{2}(e+fx)\right] \left( \left( \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. (-1+\tan\left[\frac{1}{2}(e+fx)\right]^2) \right) \right) / \left( \left( 1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, \right. \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big] - \\
 & \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] / \\
 & \left( 2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left( m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big] + \\
 & \frac{1}{-1+\tan\left[\frac{1}{2}(e+fx)\right]^2} \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
 & \left( \left( 3 a \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. (-1+\tan\left[\frac{1}{2}(e+fx)\right]^2) \right) \right) / \left( \left( 1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, \right. \right. \right. \\
 & \quad \left. \left. 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big] + \\
 & b \tan\left[\frac{1}{2}(e+fx)\right] \left( \left( \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. (-1+\tan\left[\frac{1}{2}(e+fx)\right]^2) \right) \right) / \left( \left( 1+\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, \right. \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \frac{1}{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} 2 \tan\left[\frac{1}{2}(e+fx)\right] \left( \frac{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 - \tan\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
 & \left( - \left( \left( 3 a \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right) \right) / \right. \\
 & \quad \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \quad \left( 3 a \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) / \\
 & \quad \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \quad \left( 3 a \left( -\frac{1}{3} (1-m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \\
 & \quad \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) / \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( (-1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, m, 2-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
& \quad \left. m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (e+fx) \right]^2 \Bigg) + \frac{1}{2} b \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \\
& \left( \left( \operatorname{AppellF1} \left[ 1, m, 1-m, 2, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. (-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2) \right) \Bigg) / \left( \left( 1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \left( 2 \operatorname{AppellF1} \left[ 1, m, 1-m, 2, \right. \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \left( (-1+m) \operatorname{AppellF1} \left[ 2, m, 2-m, \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + m \operatorname{AppellF1} \left[ 2, 1+m, 1-m, \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \Bigg) - \\
& \operatorname{AppellF1} \left[ 1, 1+m, -m, 2, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] / \\
& \left( 2 \operatorname{AppellF1} \left[ 1, 1+m, -m, 2, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
& \quad \left. \left( m \operatorname{AppellF1} \left[ 2, 1+m, 1-m, 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. (1+m) \operatorname{AppellF1} \left[ 2, 2+m, -m, 3, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \Bigg) - \\
& \left( 3 a \operatorname{AppellF1} \left[ \frac{1}{2}, m, 1-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \left. \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right. \\
& \quad \left( 2 \left( (-1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, m, 2-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + 3 \left( -\frac{1}{3} (1-m) \operatorname{AppellF1} \left[ \frac{3}{2}, m, 2-m, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \\
& \quad \left. \frac{1}{3} m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) + 2 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right. \\
& \quad \left( (-1+m) \left( -\frac{3}{5} (2-m) \operatorname{AppellF1} \left[ \frac{5}{2}, m, 3-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + m\left(-\frac{3}{5}(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. 2-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right) \Big/ \\
 & \left(\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+2\left((-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, m, 2-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
 & \left(-\left(\left(\operatorname{AppellF1}\left[1, m, 1-m, 2, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\right) \Big/ \\
 & \left(\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2\left(2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+\left((-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) + \\
 & \left(\operatorname{AppellF1}\left[1, m, 1-m, 2, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) \Big/ \left(\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \\
 & \left(2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \quad \left. \left((-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \right. \\
 & \quad \left. \left. m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + \left(\left(-\frac{1}{2}(1-m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+ \right. \\
 & \quad \left. \frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right\} / \\
& \left( \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left(2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right.\right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left((-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \right.\right.\right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right.\right. \\
& \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \left(\frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{2}(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \right.\right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) / \\
& \left(2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. \left(m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \\
& \quad \left. \left.(1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - \left(\operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \\
& \left( \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \\
& \quad \left. \left. m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 2 \left(-\frac{1}{2}(1-m) \operatorname{AppellF1}\left[2, m, \right.\right.\right. \\
& \quad \left. \left. 2-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right.\right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) + \\
& \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+m) \left(-\frac{2}{3}(2-m) \operatorname{AppellF1}\left[3, m, 3-m, 4, \right.\right.\right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{2}{3} m \operatorname{AppellF1}\left[3, 1+m, 2-m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right.\right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) +
\end{aligned}$$

$$\begin{aligned}
 & m \left( -\frac{2}{3} (1-m) \operatorname{AppellF1}\left[3, 1+m, 2-m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{2}{3} (1+m) \operatorname{AppellF1}\left[3, 2+m, 1-m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 2 \operatorname{AppellF1}\left[1, m, 1-m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( (-1+m) \operatorname{AppellF1}\left[2, m, 2-m, 3, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \left( \left( m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 2 \left( \frac{1}{2} m \operatorname{AppellF1}\left[2, 1+m, 1-m, \right. \right. \\
 & \quad \left. \left. 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{2} (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( m \left( -\frac{2}{3} (1-m) \operatorname{AppellF1}\left[3, 1+m, 2-m, 4, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2} \right. \right. \\
 & \quad \left. \left. (e+fx)\right] + \frac{2}{3} (1+m) \operatorname{AppellF1}\left[3, 2+m, 1-m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & (1+m) \left( \frac{2}{3} m \operatorname{AppellF1}\left[3, 2+m, 1-m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{2}{3} (2+m) \operatorname{AppellF1}\left[3, 3+m, -m, 4, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) /
 \end{aligned}$$

$$\left( 2 \operatorname{AppellF1}\left[1, 1+m, -m, 2, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ \left. \left( m \operatorname{AppellF1}\left[2, 1+m, 1-m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ \left. \left. (1+m) \operatorname{AppellF1}\left[2, 2+m, -m, 3, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right)$$

**Problem 643: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e+fx])^m}{a+b \operatorname{Tan}[e+fx]} dx$$

Optimal (type 6, 141 leaves, 6 steps):

$$\frac{b \operatorname{Hypergeometric2F1}\left[1, \frac{m}{2}, \frac{2+m}{2}, \frac{b^2 \operatorname{Sec}[e+fx]^2}{a^2+b^2}\right] (d \operatorname{Sec}[e+fx])^m}{(a^2+b^2) f m} + \\ \frac{1}{a f} \operatorname{AppellF1}\left[\frac{1}{2}, 1, 1-\frac{m}{2}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e+fx]^2}{a^2}, -\operatorname{Tan}[e+fx]^2\right] \\ (d \operatorname{Sec}[e+fx])^m (\operatorname{Sec}[e+fx]^2)^{-m/2} \operatorname{Tan}[e+fx]$$

Result (type 6, 1158 leaves):

$$\begin{aligned}
 & \left( (d \operatorname{Sec}[e + f x])^m \right. \\
 & \left( b - b (\operatorname{Sec}[e + f x]^2)^{m/2} + a m \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2\right] \operatorname{Tan}[e + f x] + \right. \\
 & \left. b \operatorname{AppellF1}\left[-m, -\frac{m}{2}, -\frac{m}{2}, 1 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \right. \\
 & \left. (\operatorname{Sec}[e + f x]^2)^{m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \right) \Big/ \\
 & \left( f (a + b \operatorname{Tan}[e + f x]) \left( a m \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2\right] \operatorname{Sec}[e + f x]^2 - \right. \right. \\
 & \left. b m (\operatorname{Sec}[e + f x]^2)^{m/2} \operatorname{Tan}[e + f x] + \right. \\
 & \left. b m \operatorname{AppellF1}\left[-m, -\frac{m}{2}, -\frac{m}{2}, 1 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \right. \\
 & \left. (\operatorname{Sec}[e + f x]^2)^{m/2} \operatorname{Tan}[e + f x] \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} + \right. \\
 & \left. b (\operatorname{Sec}[e + f x]^2)^{m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \right. \\
 & \left. \left( - \left( \left( (a - i b) b m^2 \operatorname{AppellF1}\left[1 - m, 1 - \frac{m}{2}, -\frac{m}{2}, 2 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}[e + f x]^2 \right) / \left( 2 (1 - m) (a + b \operatorname{Tan}[e + f x])^2 \right) \right) - \right. \\
 & \left. \left( (a + i b) b m^2 \operatorname{AppellF1}\left[1 - m, -\frac{m}{2}, 1 - \frac{m}{2}, 2 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \right) / \left( 2 (1 - m) (a + b \operatorname{Tan}[e + f x])^2 \right) \right) - \\
 & \frac{1}{2} b m \operatorname{AppellF1}\left[-m, -\frac{m}{2}, -\frac{m}{2}, 1 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \\
 & (\operatorname{Sec}[e + f x]^2)^{m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-1 - \frac{m}{2}} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \\
 & \left( - \frac{b^2 \operatorname{Sec}[e + f x]^2 (-i + \operatorname{Tan}[e + f x])}{(a + b \operatorname{Tan}[e + f x])^2} + \frac{b \operatorname{Sec}[e + f x]^2}{a + b \operatorname{Tan}[e + f x]} \right) - \\
 & \frac{1}{2} b m \operatorname{AppellF1}\left[-m, -\frac{m}{2}, -\frac{m}{2}, 1 - m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]}\right] \\
 & (\operatorname{Sec}[e + f x]^2)^{m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-1 - \frac{m}{2}} \\
 & \left( - \frac{b^2 \operatorname{Sec}[e + f x]^2 (i + \operatorname{Tan}[e + f x])}{(a + b \operatorname{Tan}[e + f x])^2} + \frac{b \operatorname{Sec}[e + f x]^2}{a + b \operatorname{Tan}[e + f x]} \right) + a m \operatorname{Sec}[e + f x]^2 \\
 & \left. \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2\right] + (1 + \operatorname{Tan}[e + f x]^2)^{-1 + \frac{m}{2}} \right) \right) \Big)
 \end{aligned}$$

### Problem 644: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(d \operatorname{Sec}[e + f x])^m}{(a + b \operatorname{Tan}[e + f x])^2} dx$$

Optimal (type 6, 227 leaves, 7 steps):

$$\frac{2 a b \operatorname{Hypergeometric2F1}\left[2, \frac{m}{2}, \frac{2+m}{2}, \frac{b^2 \operatorname{Sec}[e+f x]^2}{a^2+b^2}\right] (d \operatorname{Sec}[e+f x])^m}{(a^2+b^2)^2 f m} + \frac{1}{a^2 f}$$

$$\operatorname{AppellF1}\left[\frac{1}{2}, 2, 1-\frac{m}{2}, \frac{3}{2}, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2}, -\operatorname{Tan}[e+f x]^2\right] (d \operatorname{Sec}[e+f x])^m (\operatorname{Sec}[e+f x]^2)^{-m/2}$$

$$\operatorname{Tan}[e+f x] + \frac{1}{3 a^4 f} b^2 \operatorname{AppellF1}\left[\frac{3}{2}, 2, 1-\frac{m}{2}, \frac{5}{2}, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2}, -\operatorname{Tan}[e+f x]^2\right]$$

$$(d \operatorname{Sec}[e+f x])^m (\operatorname{Sec}[e+f x]^2)^{-m/2} \operatorname{Tan}[e+f x]^3$$

Result (type 6, 356 leaves):

$$\left(2(-4+m) \operatorname{AppellF1}\left[3-m, 1-\frac{m}{2}, 1-\frac{m}{2}, 4-m, \frac{a-i b}{a+b \operatorname{Tan}[e+f x]}, \frac{a+i b}{a+b \operatorname{Tan}[e+f x]}\right]\right. \\ \left.(d \operatorname{Sec}[e+f x])^m (a \operatorname{Cos}[e+f x]+b \operatorname{Sin}[e+f x])^2\right) / \left(b f(-3+m)(a+b \operatorname{Tan}[e+f x])^2\right. \\ \left.\left((-2+m)\left((a+i b) \operatorname{AppellF1}\left[4-m, 1-\frac{m}{2}, 2-\frac{m}{2}, 5-m, \frac{a-i b}{a+b \operatorname{Tan}[e+f x]}, \frac{a+i b}{a+b \operatorname{Tan}[e+f x]}\right]\right)+\right. \\ \left.\left.(a-i b) \operatorname{AppellF1}\left[4-m, 2-\frac{m}{2}, 1-\frac{m}{2}, 5-m, \frac{a-i b}{a+b \operatorname{Tan}[e+f x]}, \frac{a+i b}{a+b \operatorname{Tan}[e+f x]}\right]\right)\right) + \\ \left.2(-4+m) \operatorname{AppellF1}\left[3-m, 1-\frac{m}{2}, 1-\frac{m}{2}, 4-m, \frac{a-i b}{a+b \operatorname{Tan}[e+f x]}, \frac{a+i b}{a+b \operatorname{Tan}[e+f x]}\right]\right) \\ \left.(a+b \operatorname{Tan}[e+f x])\right)$$

### Problem 645: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (d \operatorname{Sec}[e + f x])^m (a + b \operatorname{Tan}[e + f x])^n dx$$

Optimal (type 6, 181 leaves, 3 steps):

$$\left(b \operatorname{AppellF1}\left[1+n, 1-\frac{m}{2}, 1-\frac{m}{2}, 2+n, \frac{a+b \operatorname{Tan}[e+f x]}{a+\sqrt{-b^2}}, \frac{a+b \operatorname{Tan}[e+f x]}{a-\sqrt{-b^2}}\right]\right. \\ \left.(d \operatorname{Sec}[e+f x])^m (a+b \operatorname{Tan}[e+f x])^{1+n} \left(1+\frac{a+b \operatorname{Tan}[e+f x]}{-a+\sqrt{-b^2}}\right)^{-m/2}\right. \\ \left.\left(1-\frac{a+b \operatorname{Tan}[e+f x]}{a+\sqrt{-b^2}}\right)^{-m/2}\right) / \left((a^2+b^2) f(1+n)\right)$$

Result (type 6, 1527 leaves):

$$\begin{aligned}
 & \left( b \operatorname{AppellF1} \left[ 1+n, 1-\frac{m}{2}, 1-\frac{m}{2}, 2+n, \frac{a+b \tan [e+f x]}{a-i b}, \frac{a+b \tan [e+f x]}{a+i b} \right] \right. \\
 & \quad (d \operatorname{Sec}[e+f x])^m (\operatorname{Sec}[e+f x]^2)^{\frac{m+n}{2}} \left( -\frac{b(-i+\tan [e+f x])}{a+i b} \right)^{-m/2} \\
 & \quad \left. \left( -\frac{b(i+\tan [e+f x])}{a-i b} \right)^{-m/2} (a+b \tan [e+f x])^{1+n} \left( \frac{a+b \tan [e+f x]}{\sqrt{\operatorname{Sec}[e+f x]^2}} \right)^n \right) / \\
 & \left( (a^2+b^2) f (1+n) \left( \left( b^2 \operatorname{AppellF1} \left[ 1+n, 1-\frac{m}{2}, 1-\frac{m}{2}, 2+n, \frac{a+b \tan [e+f x]}{a-i b}, \frac{a+b \tan [e+f x]}{a+i b} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. (\operatorname{Sec}[e+f x]^2)^{1+\frac{m+n}{2}} \left( -\frac{b(-i+\tan [e+f x])}{a+i b} \right)^{-m/2} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( -\frac{b(i+\tan [e+f x])}{a-i b} \right)^{-m/2} \left( \frac{a+b \tan [e+f x]}{\sqrt{\operatorname{Sec}[e+f x]^2}} \right)^n \right) \right) / \left( (a^2+b^2) (1+n) \right) + \\
 & \left( b^2 m \operatorname{AppellF1} \left[ 1+n, 1-\frac{m}{2}, 1-\frac{m}{2}, 2+n, \frac{a+b \tan [e+f x]}{a-i b}, \frac{a+b \tan [e+f x]}{a+i b} \right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+f x]^2)^{1+\frac{m+n}{2}} \left( -\frac{b(-i+\tan [e+f x])}{a+i b} \right)^{-m/2} \left( -\frac{b(i+\tan [e+f x])}{a-i b} \right)^{-1-\frac{m}{2}} \right. \\
 & \quad \left. (a+b \tan [e+f x]) \left( \frac{a+b \tan [e+f x]}{\sqrt{\operatorname{Sec}[e+f x]^2}} \right)^n \right) / \left( 2(a-i b) (a^2+b^2) (1+n) \right) + \\
 & \left( b^2 m \operatorname{AppellF1} \left[ 1+n, 1-\frac{m}{2}, 1-\frac{m}{2}, 2+n, \frac{a+b \tan [e+f x]}{a-i b}, \frac{a+b \tan [e+f x]}{a+i b} \right] \right. \\
 & \quad \left. (\operatorname{Sec}[e+f x]^2)^{1+\frac{m+n}{2}} \left( -\frac{b(-i+\tan [e+f x])}{a+i b} \right)^{-1-\frac{m}{2}} \left( -\frac{b(i+\tan [e+f x])}{a-i b} \right)^{-m/2} \right. \\
 & \quad \left. (a+b \tan [e+f x]) \left( \frac{a+b \tan [e+f x]}{\sqrt{\operatorname{Sec}[e+f x]^2}} \right)^n \right) / \left( 2(a+i b) (a^2+b^2) (1+n) \right) + \\
 & \left( b (\operatorname{Sec}[e+f x]^2)^{\frac{m+n}{2}} \left( \left( b \left( 1-\frac{m}{2} \right) (1+n) \operatorname{AppellF1} \left[ 2+n, 1-\frac{m}{2}, 2-\frac{m}{2}, 3+n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a+b \tan [e+f x]}{a-i b}, \frac{a+b \tan [e+f x]}{a+i b} \right] \operatorname{Sec}[e+f x]^2 \right) \right) / \left( (a+i b) (2+n) \right) + \\
 & \quad \left( b \left( 1-\frac{m}{2} \right) (1+n) \operatorname{AppellF1} \left[ 2+n, 2-\frac{m}{2}, 1-\frac{m}{2}, 3+n, \frac{a+b \tan [e+f x]}{a-i b}, \right. \right. \\
 & \quad \left. \left. \frac{a+b \tan [e+f x]}{a+i b} \right] \operatorname{Sec}[e+f x]^2 \right) / \left( (a-i b) (2+n) \right) \Big)
 \end{aligned}$$

$$\left( -\frac{b(-i + \tan[e + fx])}{a + ib} \right)^{-m/2} \left( -\frac{b(i + \tan[e + fx])}{a - ib} \right)^{-m/2} (a + b \tan[e + fx]) \left( \frac{a + b \tan[e + fx]}{\sqrt{\sec[e + fx]^2}} \right)^n \Big/ ((a^2 + b^2)(1 + n)) +$$

$$\left( b(m + n) \operatorname{AppellF1}\left[1 + n, 1 - \frac{m}{2}, 1 - \frac{m}{2}, 2 + n, \frac{a + b \tan[e + fx]}{a - ib}, \frac{a + b \tan[e + fx]}{a + ib}\right] \right. \\ \left. (\sec[e + fx]^2)^{\frac{m+n}{2}} \tan[e + fx] \left( -\frac{b(-i + \tan[e + fx])}{a + ib} \right)^{-m/2} \left( -\frac{b(i + \tan[e + fx])}{a - ib} \right)^{-m/2} \right. \\ \left. (a + b \tan[e + fx]) \left( \frac{a + b \tan[e + fx]}{\sqrt{\sec[e + fx]^2}} \right)^n \right) \Big/ ((a^2 + b^2)(1 + n)) +$$

$$\left( b n \operatorname{AppellF1}\left[1 + n, 1 - \frac{m}{2}, 1 - \frac{m}{2}, 2 + n, \frac{a + b \tan[e + fx]}{a - ib}, \frac{a + b \tan[e + fx]}{a + ib}\right] \right. \\ \left. (\sec[e + fx]^2)^{\frac{m+n}{2}} \left( -\frac{b(-i + \tan[e + fx])}{a + ib} \right)^{-m/2} \right. \\ \left. \left( -\frac{b(i + \tan[e + fx])}{a - ib} \right)^{-m/2} (a + b \tan[e + fx]) \left( \frac{a + b \tan[e + fx]}{\sqrt{\sec[e + fx]^2}} \right)^{-1+n} \right. \\ \left. \left( b \sqrt{\sec[e + fx]^2} - \frac{\tan[e + fx] (a + b \tan[e + fx])}{\sqrt{\sec[e + fx]^2}} \right) \right) \Big/ ((a^2 + b^2)(1 + n)) \Bigg)$$

**Problem 646: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx]^6 (a + b \tan[c + dx])^n dx$$

Optimal (type 3, 161 leaves, 3 steps):

$$\frac{(a^2 + b^2)^2 (a + b \tan[c + dx])^{1+n}}{b^5 d (1 + n)} - \frac{4 a (a^2 + b^2) (a + b \tan[c + dx])^{2+n}}{b^5 d (2 + n)} +$$

$$\frac{2 (3 a^2 + b^2) (a + b \tan[c + dx])^{3+n}}{b^5 d (3 + n)} - \frac{4 a (a + b \tan[c + dx])^{4+n}}{b^5 d (4 + n)} + \frac{(a + b \tan[c + dx])^{5+n}}{b^5 d (5 + n)}$$

Result (type 3, 377 leaves):



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$$\begin{aligned}
 & b^5 d (1+n) (2+n) (3+n) (4+n) (5+n) \\
 & \operatorname{Sec}[c+dx]^4 \left( 9a^4 + 33a^2b^2 + 64b^4 + 18a^2b^2n + 96b^4n + 3a^2b^2n^2 + 52b^4n^2 + 12b^4n^3 + \right. \\
 & \quad \left. b^4n^4 + 2(6a^4 + a^2b^2(20+9n+n^2) + b^4(24+26n+9n^2+n^3)) \cos[2(c+dx)] + \right. \\
 & \quad \left. (3a^4 - a^2b^2(-7+n^2) + b^4(8+6n+n^2)) \cos[4(c+dx)] - \right. \\
 & \quad \left. 6a^3b \sin[2(c+dx)] - 26a^3b^3 \sin[2(c+dx)] - 6a^3bn \sin[2(c+dx)] - \right. \\
 & \quad \left. 40a^3bn \sin[2(c+dx)] - 16a^3b^3n^2 \sin[2(c+dx)] - 2a^3b^3n^3 \sin[2(c+dx)] - \right. \\
 & \quad \left. 3a^3b \sin[4(c+dx)] - 7a^3b^3 \sin[4(c+dx)] - 3a^3bn \sin[4(c+dx)] - \right. \\
 & \quad \left. 9a^3bn \sin[4(c+dx)] - 2a^3b^3n^2 \sin[4(c+dx)] \right) (a+b \operatorname{Tan}[c+dx])^{1+n}
 \end{aligned}$$

Problem 649: Unable to integrate problem.

$$\int \cos[c+dx]^2 (a+b \operatorname{Tan}[c+dx])^n dx$$

Optimal (type 5, 272 leaves, 6 steps):

$$\begin{aligned}
 & - \left( \left( \sqrt{-b^2} \left( 1 + \frac{a^2}{b^2} - n \right) - a n \right) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a+b \operatorname{Tan}[c+dx]}{a-\sqrt{-b^2}} \right] \right. \\
 & \quad \left. (a+b \operatorname{Tan}[c+dx])^{1+n} \right) / \left( 4 \left( 1 + \frac{a^2}{b^2} \right) b \left( a - \sqrt{-b^2} \right) d (1+n) \right) + \\
 & \left( b \left( \sqrt{-b^2} \left( 1 + \frac{a^2}{b^2} - n \right) + a n \right) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a+b \operatorname{Tan}[c+dx]}{a+\sqrt{-b^2}} \right] \right. \\
 & \quad \left. (a+b \operatorname{Tan}[c+dx])^{1+n} \right) / \left( 4 (a^2+b^2) \left( a + \sqrt{-b^2} \right) d (1+n) \right) + \\
 & \frac{\cos[c+dx]^2 (b+a \operatorname{Tan}[c+dx]) (a+b \operatorname{Tan}[c+dx])^{1+n}}{2 (a^2+b^2) d}
 \end{aligned}$$

Result (type 8, 23 leaves):

$$\int \cos[c+dx]^2 (a+b \operatorname{Tan}[c+dx])^n dx$$

Problem 650: Unable to integrate problem.

$$\int \cos[c+dx]^4 (a+b \operatorname{Tan}[c+dx])^n dx$$

Optimal (type 5, 434 leaves, 7 steps):

$$\left( b \left( \frac{a \left( 5 + \frac{3a^2}{b^2} - 2n \right) n}{b^2} - \frac{\sqrt{-b^2} \left( 3a^4 + a^2 b^2 (6 - 2n - n^2) + b^4 (3 - 4n + n^2) \right)}{b^6} \right) \right.$$

$$\left. \text{Hypergeometric2F1} \left[ 1, 1 + n, 2 + n, \frac{a + b \text{Tan}[c + dx]}{a - \sqrt{-b^2}} \right] (a + b \text{Tan}[c + dx])^{1+n} \right) /$$

$$\left( 16 \left( 1 + \frac{a^2}{b^2} \right)^2 (a - \sqrt{-b^2}) d (1 + n) \right) +$$

$$\left( b \left( \frac{a \left( 5 + \frac{3a^2}{b^2} - 2n \right) n}{b^2} + \frac{\sqrt{-b^2} \left( 3a^4 + a^2 b^2 (6 - 2n - n^2) + b^4 (3 - 4n + n^2) \right)}{b^6} \right) \right.$$

$$\left. \text{Hypergeometric2F1} \left[ 1, 1 + n, 2 + n, \frac{a + b \text{Tan}[c + dx]}{a + \sqrt{-b^2}} \right] (a + b \text{Tan}[c + dx])^{1+n} \right) /$$

$$\left( 16 \left( 1 + \frac{a^2}{b^2} \right)^2 (a + \sqrt{-b^2}) d (1 + n) \right) + \frac{\text{Cos}[c + dx]^4 (b + a \text{Tan}[c + dx]) (a + b \text{Tan}[c + dx])^{1+n}}{4 (a^2 + b^2) d} +$$

$$\frac{1}{8 (a^2 + b^2)^2 d} b \text{Cos}[c + dx]^2 (a + b \text{Tan}[c + dx])^{1+n}$$

$$\left( b^2 (3 - n) + a^2 (1 + n) + a b \left( 5 + \frac{3a^2}{b^2} - 2n \right) \text{Tan}[c + dx] \right)$$

Result (type 8, 23 leaves):

$$\int \text{Cos}[c + dx]^4 (a + b \text{Tan}[c + dx])^n dx$$

**Problem 651: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + dx]^3 (a + b \text{Tan}[c + dx])^n dx$$

Optimal (type 6, 159 leaves, 3 steps):

$$\left( \text{AppellF1} \left[ 1 + n, -\frac{1}{2}, -\frac{1}{2}, 2 + n, \frac{a + b \text{Tan}[c + dx]}{a - \sqrt{-b^2}}, \frac{a + b \text{Tan}[c + dx]}{a + \sqrt{-b^2}} \right] \text{Sec}[c + dx] \right.$$

$$\left. (a + b \text{Tan}[c + dx])^{1+n} \right) / \left( b d (1 + n) \sqrt{1 - \frac{a + b \text{Tan}[c + dx]}{a - \sqrt{-b^2}}} \sqrt{1 - \frac{a + b \text{Tan}[c + dx]}{a + \sqrt{-b^2}}} \right)$$

Result (type 6, 323 leaves):

$$\left( 2 (a - i b) (a + i b) (2 + n) \operatorname{AppellF1}\left[1 + n, -\frac{1}{2}, -\frac{1}{2}, 2 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] \right. \\ \left. \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^n \right] / (b d (1 + n) \\ \left( 2 (a^2 + b^2) (2 + n) \operatorname{AppellF1}\left[1 + n, -\frac{1}{2}, -\frac{1}{2}, 2 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] - \right. \\ \left. \left( (a - i b) \operatorname{AppellF1}\left[2 + n, -\frac{1}{2}, \frac{1}{2}, 3 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] + \right. \right. \\ \left. \left. (a + i b) \operatorname{AppellF1}\left[2 + n, \frac{1}{2}, -\frac{1}{2}, 3 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] \right) (a + \right. \\ \left. b \operatorname{Tan}[c + d x]) \right) \left. \right)$$

**Problem 652: Result unnecessarily involves imaginary or complex numbers.**

$$\int \operatorname{Sec}[c + d x] (a + b \operatorname{Tan}[c + d x])^n dx$$

Optimal (type 6, 159 leaves, 3 steps):

$$\frac{1}{b d (1 + n)} \operatorname{AppellF1}\left[1 + n, \frac{1}{2}, \frac{1}{2}, 2 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - \sqrt{-b^2}}, \frac{a + b \operatorname{Tan}[c + d x]}{a + \sqrt{-b^2}}\right] \\ \operatorname{Cos}[c + d x] (a + b \operatorname{Tan}[c + d x])^{1+n} \sqrt{1 - \frac{a + b \operatorname{Tan}[c + d x]}{a - \sqrt{-b^2}}} \sqrt{1 - \frac{a + b \operatorname{Tan}[c + d x]}{a + \sqrt{-b^2}}}$$

Result (type 6, 314 leaves):

$$\left( 2 (a - i b) (a + i b) (2 + n) \operatorname{AppellF1}\left[1 + n, \frac{1}{2}, \frac{1}{2}, 2 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] \right. \\ \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^n \right] / (b d (1 + n) \\ \left( 2 (a^2 + b^2) (2 + n) \operatorname{AppellF1}\left[1 + n, \frac{1}{2}, \frac{1}{2}, 2 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] + \right. \\ \left. \left( (a - i b) \operatorname{AppellF1}\left[2 + n, \frac{1}{2}, \frac{3}{2}, 3 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] + \right. \right. \\ \left. \left. (a + i b) \operatorname{AppellF1}\left[2 + n, \frac{3}{2}, \frac{1}{2}, 3 + n, \frac{a + b \operatorname{Tan}[c + d x]}{a - i b}, \frac{a + b \operatorname{Tan}[c + d x]}{a + i b}\right] \right) (a + \right. \\ \left. b \operatorname{Tan}[c + d x]) \right) \left. \right)$$

**Problem 653: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Tan}[c + d x])^n dx$$

Optimal (type 6, 161 leaves, 3 steps):

$$\frac{1}{b d (1+n)} \text{AppellF1}\left[1+n, \frac{3}{2}, \frac{3}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-\sqrt{-b^2}}, \frac{a+b \tan [c+d x]}{a+\sqrt{-b^2}}\right]$$

$$\cos [c+d x]^3 (a+b \tan [c+d x])^{1+n} \left(1-\frac{a+b \tan [c+d x]}{a-\sqrt{-b^2}}\right)^{3/2} \left(1-\frac{a+b \tan [c+d x]}{a+\sqrt{-b^2}}\right)^{3/2}$$

Result (type 6, 323 leaves):

$$\left(2(a-i b)(a+i b)(2+n) \text{AppellF1}\left[1+n, \frac{3}{2}, \frac{3}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]\right.$$

$$\left. \cos [c+d x]^2 (a \cos [c+d x]+b \sin [c+d x]) (a+b \tan [c+d x])^n\right) / (b d (1+n))$$

$$\left(2\left(a^2+b^2\right)(2+n) \text{AppellF1}\left[1+n, \frac{3}{2}, \frac{3}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]+3\left((a-i b) \text{AppellF1}\left[2+n, \frac{3}{2}, \frac{5}{2}, 3+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]+(a+i b) \text{AppellF1}\left[2+n, \frac{5}{2}, \frac{3}{2}, 3+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]\right)(a+b \tan [c+d x])\right)$$

**Problem 654: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^3 (a+b \tan [c+d x])^n dx$$

Optimal (type 6, 161 leaves, 3 steps):

$$\frac{1}{b d (1+n)} \text{AppellF1}\left[1+n, \frac{5}{2}, \frac{5}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-\sqrt{-b^2}}, \frac{a+b \tan [c+d x]}{a+\sqrt{-b^2}}\right]$$

$$\cos [c+d x]^5 (a+b \tan [c+d x])^{1+n} \left(1-\frac{a+b \tan [c+d x]}{a-\sqrt{-b^2}}\right)^{5/2} \left(1-\frac{a+b \tan [c+d x]}{a+\sqrt{-b^2}}\right)^{5/2}$$

Result (type 6, 323 leaves):

$$\left(2(a-i b)(a+i b)(2+n) \text{AppellF1}\left[1+n, \frac{5}{2}, \frac{5}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]\right.$$

$$\left. \cos [c+d x]^4 (a \cos [c+d x]+b \sin [c+d x]) (a+b \tan [c+d x])^n\right) / (b d (1+n))$$

$$\left(2\left(a^2+b^2\right)(2+n) \text{AppellF1}\left[1+n, \frac{5}{2}, \frac{5}{2}, 2+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]+5\left((a-i b) \text{AppellF1}\left[2+n, \frac{5}{2}, \frac{7}{2}, 3+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]+(a+i b) \text{AppellF1}\left[2+n, \frac{7}{2}, \frac{5}{2}, 3+n, \frac{a+b \tan [c+d x]}{a-i b}, \frac{a+b \tan [c+d x]}{a+i b}\right]\right)(a+b \tan [c+d x])\right)$$

**Problem 656: Result unnecessarily involves higher level functions and more**

than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^{5/2} (a + i a \tan [c + d x]) dx$$

Optimal (type 4, 90 leaves, 5 steps):

$$-\frac{2 i a (e \cos [c + d x])^{5/2}}{5 d} + \frac{6 a (e \cos [c + d x])^{5/2} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d \cos [c + d x]^{5/2}} + \frac{2 a (e \cos [c + d x])^{5/2} \tan [c + d x]}{5 d}$$

Result (type 5, 195 leaves):

$$-\frac{1}{10 d} i a e^2 \sqrt{e \cos [c + d x]} \operatorname{Csc}[c] \left( 6 \cos [c] + 3 \cos [c + 2 d x] + 3 \cos [3 c + 2 d x] - 6 e^{-i(c+2 d x)} \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - 2 e^{-i c} \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i(c+d x)}\right] + 2 i \sin [c] - 4 i \sin [c + 2 d x] - 2 i \sin [3 c + 2 d x] \right) (-i + \tan [c + d x])$$

**Problem 658:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos [c + d x]} (a + i a \tan [c + d x]) dx$$

Optimal (type 4, 60 leaves, 4 steps):

$$-\frac{2 i a \sqrt{e \cos [c + d x]}}{d} + \frac{2 a \sqrt{e \cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{d \sqrt{\cos [c + d x]}}$$

Result (type 5, 162 leaves):

$$-\left( \left( 4 i a e^{2 i c} \sqrt{e \cos [c + d x]} \left( 3 + 3 e^{2 i(c+d x)} - 3 \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - e^{2 i d x} \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i(c+d x)}\right] \right) \right) / (3 d (-1 + e^{2 i c}) (1 + e^{2 i(c+d x)})) \right)$$

**Problem 659:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{a + i a \tan [c + d x]}{\sqrt{e \cos [c + d x]}} dx$$

Optimal (type 4, 60 leaves, 4 steps):

$$\frac{2 i a}{d \sqrt{e \cos [c + d x]}} + \frac{2 a \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{d \sqrt{e \cos [c + d x]}}$$

Result (type 5, 143 leaves):

$$\begin{aligned} & -\frac{1}{d e \sqrt{\operatorname{Csc}[c]^2}} \sqrt{2} a \sqrt{e \cos [c + d x]} (-i + \operatorname{Cot}[c]) \\ & \left( \sqrt{2} \sqrt{\operatorname{Csc}[c]^2 + i \cos [c + d x]} \sqrt{1 + \cos [2 d x - 2 \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \operatorname{Csc}[c] \right. \\ & \quad \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right) \\ & \sin [c] (\cos [d x] - i \sin [d x]) (-i + \tan [c + d x]) \end{aligned}$$

**Problem 660:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{a + i a \tan [c + d x]}{(e \cos [c + d x])^{3/2}} dx$$

Optimal (type 4, 89 leaves, 5 steps):

$$\frac{2 i a}{3 d (e \cos [c + d x])^{3/2}} - \frac{2 a \cos [c + d x]^{3/2} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{d (e \cos [c + d x])^{3/2}} + \frac{2 a \sin [c + d x]}{d e \sqrt{e \cos [c + d x]}}$$

Result (type 5, 203 leaves):

$$\begin{aligned} & \left( a e^{-i(c+3dx)} (1 + e^{2ic}) (-i + \operatorname{Cot}[c]) \left( -3 - e^{2idx} - 5 e^{2i(c+dx)} - \right. \right. \\ & \quad \left. \left. 3 e^{2i(c+2dx)} + 3 (1 + e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \right. \\ & \quad \left. \left. e^{2idx} (1 + e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i(c+dx)}\right] \right) \right) \\ & \tan [c] (-i + \tan [c + d x]) \Big/ \left( 6 d e (-1 + e^{2ic}) \sqrt{e \cos [c + d x]} \right) \end{aligned}$$

**Problem 662:** Result unnecessarily involves higher level functions.

$$\int \frac{a + i a \tan [c + d x]}{(e \cos [c + d x])^{7/2}} dx$$

Optimal (type 4, 130 leaves, 6 steps):

$$\frac{2 i a}{7 d (e \cos [c+d x])^{7/2}} - \frac{6 a \cos [c+d x]^{7/2} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d (e \cos [c+d x])^{7/2}} +$$

$$\frac{2 a \cos [c+d x] \sin [c+d x]}{5 d (e \cos [c+d x])^{7/2}} + \frac{6 a \cos [c+d x]^3 \sin [c+d x]}{5 d (e \cos [c+d x])^{7/2}}$$

Result (type 5, 245 leaves):

$$\left( \cos [c+d x]^{9/2} \right.$$

$$\left( - \left( \left( 2 \sqrt{2} e^{-i d x} \sqrt{1+e^{2 i(c+d x)}} (-i + \cot [c]) \left( 3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \right. \right. \right.$$

$$\left. \left. \left. e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i(c+d x)}\right] \right) \right) \right) /$$

$$\left( 5 \sqrt{e^{-i(c+d x)} (1+e^{2 i(c+d x)})} \right) + \left( (-i + \cot [c]) (63 \cos [c] + 77 \cos [c+2 d x] + \right.$$

$$\left. 7 \cos [3 c+2 d x] + 21 \cos [3 c+4 d x] + 40 i \sin [c]) \right) / (70 \cos [c+d x]^{7/2}) \left. \right)$$

$$\left( \cos [d x] - i \sin [d x] \right) (a + i a \tan [c+d x]) \left. \right) / (2$$

$$d$$

$$(e \cos [c+d x])^{7/2})$$

**Problem 664: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \cos [c+d x])^{5/2}}{(a+i a \tan [c+d x])^2} dx$$

Optimal (type 4, 154 leaves, 6 steps):

$$\frac{42 (e \cos [c+d x])^{5/2} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{65 a^2 d \cos [c+d x]^{5/2}} + \frac{2 \cos [c+d x] (e \cos [c+d x])^{5/2} \sin [c+d x]}{13 a^2 d} +$$

$$\frac{14 (e \cos [c+d x])^{5/2} \tan [c+d x]}{65 a^2 d} + \frac{4 i \cos [c+d x]^2 (e \cos [c+d x])^{5/2}}{13 d (a^2 + i a^2 \tan [c+d x])}$$

Result (type 5, 292 leaves):

$$\begin{aligned}
& - \frac{1}{1040 a^2 d \sqrt{e \cos [c+d x]}} e^3 \operatorname{Csc}[c] \left( \cos [2(c+d x)] - i \sin [2(c+d x)] \right) \\
& \left( 178 \cos [d x] + 158 \cos [2 c+d x] + 169 \cos [2 c+3 d x] + 167 \cos [4 c+3 d x] - 9 \cos [4 c+5 d x] + \right. \\
& \quad 9 \cos [6 c+5 d x] - 336 e^{i(2 c+d x)} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - \\
& \quad 112 e^{2 i c+3 i d x} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \\
& \quad 296 i \sin [d x] + 40 i \sin [2 c+d x] + 204 i \sin [2 c+3 d x] + \\
& \quad \left. 132 i \sin [4 c+3 d x] - 4 i \sin [4 c+5 d x] + 4 i \sin [6 c+5 d x] \right)
\end{aligned}$$

**Problem 666: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{e \cos [c+d x]}}{(a+i a \tan [c+d x])^2} dx$$

Optimal (type 4, 120 leaves, 5 steps):

$$\frac{2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d \sqrt{\cos [c+d x]}} + \frac{2 i \sqrt{e \cos [c+d x]}}{9 d (a+i a \tan [c+d x])^2} + \frac{2 i \sqrt{e \cos [c+d x]}}{9 d (a^2+i a^2 \tan [c+d x])}$$

Result (type 5, 230 leaves):

$$\begin{aligned}
& - \frac{1}{36 a^2 d \sqrt{e \cos [c+d x]}} \\
& e \operatorname{Csc}[c] \left( \cos [2(c+d x)] - i \sin [2(c+d x)] \right) \left( 7 \cos [d x] + 5 \cos [2 c+d x] + 7 \cos [2 c+3 d x] + \right. \\
& \quad 5 \cos [4 c+3 d x] - 12 e^{i(2 c+d x)} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - \\
& \quad 4 e^{2 i c+3 i d x} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \\
& \quad \left. 12 i \sin [d x] + 8 i \sin [2 c+3 d x] + 4 i \sin [4 c+3 d x] \right)
\end{aligned}$$

**Problem 668: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{(e \cos [c+d x])^{3/2} (a+i a \tan [c+d x])^2} dx$$

Optimal (type 4, 92 leaves, 4 steps):

$$\frac{2 \cos [c+d x]^{3/2} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^2 d (e \cos [c+d x])^{3/2}} + \frac{4 i \cos [c+d x]^2}{5 d (e \cos [c+d x])^{3/2} (a^2+i a^2 \tan [c+d x])}$$

Result (type 5, 104 leaves):



$$\left( i e^{-3 i (c+d x)} \left( 1 + e^{2 i (c+d x)} + 2 e^{2 i (c+d x)} \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \right) / \left( 5 a^2 d e \sqrt{e \cos [c+d x]} \right)$$

**Problem 670: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\left( e \cos [c+d x] \right)^{7/2} \left( a + i a \tan [c+d x] \right)^2} dx$$

Optimal (type 4, 122 leaves, 5 steps):

$$\frac{6 \cos [c+d x]^{7/2} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a^2 d \left( e \cos [c+d x] \right)^{7/2}} - \frac{6 \cos [c+d x]^3 \sin [c+d x]}{a^2 d \left( e \cos [c+d x] \right)^{7/2}} + \frac{4 i \cos [c+d x]^2}{d \left( e \cos [c+d x] \right)^{7/2} \left( a^2 + i a^2 \tan [c+d x] \right)}$$

Result (type 5, 103 leaves):

$$\left( 2 i \sqrt{2} e^{-i (c+d x)} \left( -1 + 3 \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \right) / \left( a^2 d e^3 \sqrt{e e^{-i (c+d x)} \left( 1 + e^{2 i (c+d x)} \right)} \right)$$

**Problem 672: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\left( e \cos [c+d x] \right)^{11/2} \left( a + i a \tan [c+d x] \right)^2} dx$$

Optimal (type 4, 164 leaves, 6 steps):

$$-\frac{14 \cos [c+d x]^{11/2} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^2 d \left( e \cos [c+d x] \right)^{11/2}} + \frac{14 \cos [c+d x]^3 \sin [c+d x]}{15 a^2 d \left( e \cos [c+d x] \right)^{11/2}} + \frac{14 \cos [c+d x]^5 \sin [c+d x]}{5 a^2 d \left( e \cos [c+d x] \right)^{11/2}} - \frac{4 i \cos [c+d x]^2}{3 d \left( e \cos [c+d x] \right)^{11/2} \left( a^2 + i a^2 \tan [c+d x] \right)}$$

Result (type 5, 253 leaves):

$$\left( \text{Cos}[c + d x]^{7/2} \text{Csc}[c] (\text{Cos}[2 c] + i \text{Sin}[2 c]) (\text{Cos}[d x] + i \text{Sin}[d x])^2 \right. \\ \left. - \left( \left( 14 \sqrt{2} e^{-i d x} \sqrt{1 + e^{2 i (c+d x)}} \left( 3 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] + \right. \right. \right. \right. \\ \left. \left. \left. e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i (c+d x)}\right]\right) \right) \right) / \left( \sqrt{e^{-i (c+d x)} (1 + e^{2 i (c+d x)})} \right) \right) + \\ \frac{1}{\text{Cos}[c + d x]^{5/2}} (36 \text{Cos}[d x] + 27 \text{Cos}[2 c + d x] + 21 \text{Cos}[2 c + 3 d x] + \\ 20 i \text{Sin}[d x] - 20 i \text{Sin}[2 c + d x]) \left. \right) / \left( 30 d (e \text{Cos}[c + d x])^{11/2} (a + i a \text{Tan}[c + d x])^2 \right)$$

Problem 677: Result is not expressed in closed-form.

$$\int \frac{\sqrt{a + i a \text{Tan}[c + d x]}}{\sqrt{e \text{Cos}[c + d x]}} dx$$

Optimal (type 3, 335 leaves, 10 steps):

$$\frac{i \sqrt{2} \sqrt{a} \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e \text{Cos}[c+d x]} \sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{a} \sqrt{e}}\right]}{d \sqrt{e}} - \\ \frac{i \sqrt{2} \sqrt{a} \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e \text{Cos}[c+d x]} \sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{a} \sqrt{e}}\right]}{d \sqrt{e}} - \frac{1}{\sqrt{2} d \sqrt{e}} \\ i \sqrt{a} \text{Log}\left[a \sqrt{e} - \sqrt{2} \sqrt{a} \sqrt{e \text{Cos}[c+d x]} \sqrt{a+i a \text{Tan}[c+d x]} + \right. \\ \left. \sqrt{e} \text{Cos}[c+d x] (a + i a \text{Tan}[c+d x])\right] + \frac{1}{\sqrt{2} d \sqrt{e}} i \sqrt{a} \text{Log}\left[ \right. \\ \left. a \sqrt{e} + \sqrt{2} \sqrt{a} \sqrt{e \text{Cos}[c+d x]} \sqrt{a+i a \text{Tan}[c+d x]} + \sqrt{e} \text{Cos}[c+d x] (a + i a \text{Tan}[c+d x]) \right]$$

Result (type 7, 111 leaves):

$$- \left( \left( e^{-\frac{1}{2} i (4 c + 3 d x)} (1 + e^{2 i (c+d x)}) \text{RootSum}\left[1 + e^{2 i c} \#1^4 \&, \frac{d x + 2 i \text{Log}\left[e^{\frac{i d x}{2}} - \#1\right]}{\#1} \&\right] \right. \right. \\ \left. \left. \sqrt{a + i a \text{Tan}[c + d x]} \right) / \left( 4 d \sqrt{e \text{Cos}[c + d x]} \right) \right)$$

Problem 678: Result is not expressed in closed-form.

$$\int \frac{\sqrt{a + i a \text{Tan}[c + d x]}}{(e \text{Cos}[c + d x])^{3/2}} dx$$

Optimal (type 3, 524 leaves, 13 steps):

$$\frac{i a}{d (e \cos [c+d x])^{3/2} \sqrt{a+i a \tan [c+d x]}} -$$

$$\frac{i a^{3/2} \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e}}\right] \operatorname{Sec}[c+d x]}{\sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}} +$$

$$\frac{i a^{3/2} \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e}}\right] \operatorname{Sec}[c+d x]}{\sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}} +$$

$$\left(i a^{3/2} \operatorname{Log}\left[a-\frac{\sqrt{2} \sqrt{a} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{e}}+\cos [c+d x](a-i a \tan [c+d x])\right] \operatorname{Sec}[c+d x]\right) / \left(2 \sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}\right) -$$

$$\left(i a^{3/2} \operatorname{Log}\left[a+\frac{\sqrt{2} \sqrt{a} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{e}}+\cos [c+d x](a-i a \tan [c+d x])\right] \operatorname{Sec}[c+d x]\right) / \left(2 \sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}\right)$$

Result (type 7, 135 leaves):

$$\left(e^{-\frac{3}{2} i (2 c+d x)} \left(8 i e^{\frac{1}{2} i (4 c+d x)} - (1+e^{2 i (c+d x)}) \operatorname{RootSum}\left[1+e^{2 i c} \#1^4 \&, \frac{d x+2 i \operatorname{Log}\left[e^{\frac{i d x}{2}}-\#1\right]}{\#1^3} \&\right]\right) \sqrt{a+i a \tan [c+d x]}\right) / \left(8 d e \sqrt{e \cos [c+d x]}\right)$$

**Problem 679: Result is not expressed in closed-form.**

$$\int \frac{\sqrt{a+i a \tan [c+d x]}}{(e \cos [c+d x])^{5/2}} dx$$

Optimal (type 3, 512 leaves, 13 steps):

$$\frac{3 i \sqrt{a} e^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{4 \sqrt{2} d (e \operatorname{Cos}[c+d x])^{5/2} (e \operatorname{Sec}[c+d x])^{5/2}} - \frac{3 i \sqrt{a} e^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{4 \sqrt{2} d (e \operatorname{Cos}[c+d x])^{5/2} (e \operatorname{Sec}[c+d x])^{5/2}} - \left( \frac{3 i \sqrt{a} e^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right]}{\left(8 \sqrt{2} d (e \operatorname{Cos}[c+d x])^{5/2} (e \operatorname{Sec}[c+d x])^{5/2}\right)} + \frac{3 i \sqrt{a} e^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \operatorname{Cos}[c+d x] (a+i a \operatorname{Tan}[c+d x])\right]}{\left(8 \sqrt{2} d (e \operatorname{Cos}[c+d x])^{5/2} (e \operatorname{Sec}[c+d x])^{5/2}\right)} + \frac{i a}{2 d (e \operatorname{Cos}[c+d x])^{5/2} \sqrt{a+i a \operatorname{Tan}[c+d x]}} - \frac{3 i \operatorname{Cos}[c+d x]^2 \sqrt{a+i a \operatorname{Tan}[c+d x]}}{4 d (e \operatorname{Cos}[c+d x])^{5/2}} \right) /$$

Result (type 7, 186 leaves):

$$\left( \sqrt{a+i a \operatorname{Tan}[c+d x]} \left( -\frac{1}{8 \sqrt{2}} 3 e^{-\frac{1}{2} i (8 c+7 d x)} (1+e^{2 i (c+d x)})^3 \sqrt{e^{-i (c+d x)} (1+e^{2 i (c+d x)})} \operatorname{RootSum}\left[1+e^{2 i c} \#1^4 \&, \frac{d x+2 i \operatorname{Log}\left[e^{\frac{i d x}{2}}-\#1\right]}{\#1}\right] \& \right) + 4 \operatorname{Cos}[c+d x]^{5/2} (-i+2 \operatorname{Tan}[c+d x]) \right) / \left( 16 d \sqrt{\operatorname{Cos}[c+d x]} (e \operatorname{Cos}[c+d x])^{5/2} \right)$$

**Problem 680: Result is not expressed in closed-form.**

$$\int \frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{(e \operatorname{Cos}[c+d x])^{7/2}} dx$$

Optimal (type 3, 719 leaves, 15 steps):

$$\begin{aligned}
 & \frac{i a}{3 d (e \cos [c+d x])^{7/2} \sqrt{a+i a \tan [c+d x]}} + \frac{5 i a \cos [c+d x]^2}{8 d (e \cos [c+d x])^{7/2} \sqrt{a+i a \tan [c+d x]}} - \\
 & \left( \frac{5 i a^{3/2} e^{7/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \sec [c+d x]}}\right] \sec [c+d x]}{\sqrt{a} \sqrt{e \sec [c+d x]}} \right) / \\
 & \left( 8 \sqrt{2} d (e \cos [c+d x])^{7/2} (e \sec [c+d x])^{7/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]} \right) + \\
 & \left( \frac{5 i a^{3/2} e^{7/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \sec [c+d x]}}\right] \sec [c+d x]}{\sqrt{a} \sqrt{e \sec [c+d x]}} \right) / \\
 & \left( 8 \sqrt{2} d (e \cos [c+d x])^{7/2} (e \sec [c+d x])^{7/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]} \right) + \\
 & \left( \frac{5 i a^{3/2} e^{7/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a-i a \tan [c+d x]}}{\sqrt{e \sec [c+d x]}} + \cos [c+d x] (a-i a \tan [c+d x])\right]}{\sqrt{e \sec [c+d x]}} \right. \\
 & \left. \sec [c+d x] \right) / \left( 16 \sqrt{2} d (e \cos [c+d x])^{7/2} (e \sec [c+d x])^{7/2} \right. \\
 & \left. \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]} \right) - \left( 5 i a^{3/2} e^{7/2} \right. \\
 & \left. \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a-i a \tan [c+d x]}}{\sqrt{e \sec [c+d x]}} + \cos [c+d x] (a-i a \tan [c+d x])\right] \sec [c+d x] \right) / \\
 & \left( 16 \sqrt{2} d (e \cos [c+d x])^{7/2} (e \sec [c+d x])^{7/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]} \right) - \\
 & \frac{5 i \cos [c+d x]^2 \sqrt{a+i a \tan [c+d x]}}{12 d (e \cos [c+d x])^{7/2}}
 \end{aligned}$$

Result (type 7, 306 leaves):

$$\begin{aligned}
 & \left( e^{-\frac{1}{2} i (4 c+d x)} \sqrt{e \cos [c+d x]} \left( -15 \sqrt{e^{i d x}} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \sqrt{e^{-i (c+d x)} (1+e^{2 i (c+d x)})} \right. \right. \\
 & \left. \left. \operatorname{RootSum}\left[1+e^{2 i c} \#1^4 \&, \frac{d x+2 i \operatorname{Log}\left[e^{\frac{i d x}{2}}-\#1\right]}{\#1^3} \&\right] - \frac{1}{(1+e^{2 i (c+d x)})^3} \right. \right. \\
 & \left. \left. 8 i e^{\frac{1}{2} i (4 c+d x)} \sqrt{e^{i d x}} (-15-42 e^{2 i (c+d x)}+5 e^{4 i (c+d x)}) \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]} \right) \right. \\
 & \left. \sqrt{a+i a \tan [c+d x]} \right) / \left( 96 d e^4 \cos [c+d x]^{5/2} \sec [c+d x]^{5/2} \sqrt{\cos [d x]+i \sin [d x]} \right)
 \end{aligned}$$

**Problem 685: Result is not expressed in closed-form.**

$$\int \frac{1}{(e \cos [c+d x])^{3/2} \sqrt{a+i a \tan [c+d x]}} dx$$

Optimal (type 3, 495 leaves, 11 steps):

$$\begin{aligned}
 & \frac{i \sqrt{2} \sqrt{a} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e}}\right] \operatorname{Sec}[c+d x]}{d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}} + \\
 & \frac{i \sqrt{2} \sqrt{a} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]}}{\sqrt{a} \sqrt{e}}\right] \operatorname{Sec}[c+d x]}{d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}} + \\
 & \left( \frac{i \sqrt{a} \operatorname{Log}\left[a \sqrt{e} - \sqrt{2} \sqrt{a} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]} + \sqrt{e} \cos [c+d x] (a-i a \tan [c+d x])\right] \operatorname{Sec}[c+d x]}{\left(\sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}\right)} - \right. \\
 & \left. \frac{i \sqrt{a} \operatorname{Log}\left[a \sqrt{e} + \sqrt{2} \sqrt{a} \sqrt{e \cos [c+d x]} \sqrt{a-i a \tan [c+d x]} + \sqrt{e} \cos [c+d x] (a-i a \tan [c+d x])\right] \operatorname{Sec}[c+d x]}{\left(\sqrt{2} d e^{3/2} \sqrt{a-i a \tan [c+d x]} \sqrt{a+i a \tan [c+d x]}\right)} \right) /
 \end{aligned}$$

Result (type 7, 100 leaves):

$$\frac{e^{\frac{1}{2} i (-2 c+d x)} \operatorname{RootSum}\left[1 + e^{2 i c} \#1^4 \&, \frac{d x+2 i \operatorname{Log}\left[e^{\frac{i d x}{2}} - \#1\right]}{\#1^3} \&\right]}{2 d e \sqrt{e \cos [c+d x]} \sqrt{a+i a \tan [c+d x]}}$$

**Problem 686: Result is not expressed in closed-form.**

$$\int \frac{1}{\left(e \cos [c+d x]\right)^{5/2} \sqrt{a+i a \tan [c+d x]}} dx$$

Optimal (type 3, 470 leaves, 12 steps):

$$\begin{aligned}
 & \frac{i e^{5/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} \sqrt{a} d \left(e \cos [c+d x]\right)^{5/2} \left(e \operatorname{Sec}[c+d x]\right)^{5/2}} - \frac{i e^{5/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{a} \sqrt{e \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} \sqrt{a} d \left(e \cos [c+d x]\right)^{5/2} \left(e \operatorname{Sec}[c+d x]\right)^{5/2}} - \\
 & \left( \frac{i e^{5/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \cos [c+d x] (a+i a \tan [c+d x])\right]}{\left(2 \sqrt{2} \sqrt{a} d \left(e \cos [c+d x]\right)^{5/2} \left(e \operatorname{Sec}[c+d x]\right)^{5/2}\right)} + \right. \\
 & \left. \frac{i e^{5/2} \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a+i a \tan [c+d x]}}{\sqrt{e \operatorname{Sec}[c+d x]}} + \cos [c+d x] (a+i a \tan [c+d x])\right]}{\left(2 \sqrt{2} \sqrt{a} d \left(e \cos [c+d x]\right)^{5/2} \left(e \operatorname{Sec}[c+d x]\right)^{5/2}\right)} - \frac{i \cos [c+d x]^2 \sqrt{a+i a \tan [c+d x]}}{a d \left(e \cos [c+d x]\right)^{5/2}} \right) /
 \end{aligned}$$

Result (type 7, 136 leaves):

$$\begin{aligned}
 & - \left( \left( \left( \cos\left[\frac{dx}{2}\right] + i \sin\left[\frac{dx}{2}\right] \right) \left( 4 i \cos\left[c + \frac{dx}{2}\right] + \right. \right. \right. \\
 & \quad \left. \left. \cos[c + dx] \operatorname{RootSum}\left[1 + e^{2ic} \#1^4 \&, \frac{dx + 2 i \operatorname{Log}\left[e^{\frac{idx}{2}} - \#1\right]}{\#1} \&\right] - 4 \sin\left[c + \frac{dx}{2}\right] \right) \right) / \\
 & \quad \left. \left( 4 d e \left( e \cos[c + dx] \right)^{3/2} \sqrt{a + i a \tan[c + dx]} \right) \right)
 \end{aligned}$$

**Problem 687: Result is not expressed in closed-form.**

$$\int \frac{1}{\left( e \cos[c + dx] \right)^{7/2} \sqrt{a + i a \tan[c + dx]}} dx$$

Optimal (type 3, 682 leaves, 14 steps):

$$\begin{aligned}
 & \frac{3 i \cos[c + dx]^2}{4 d \left( e \cos[c + dx] \right)^{7/2} \sqrt{a + i a \tan[c + dx]}} - \\
 & \left( 3 i \sqrt{a} e^{7/2} \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx] \right) / \\
 & \left( 4 \sqrt{2} d \left( e \cos[c + dx] \right)^{7/2} \left( e \sec[c + dx] \right)^{7/2} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) + \\
 & \left( 3 i \sqrt{a} e^{7/2} \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{a} \sqrt{e \sec[c + dx]}}\right] \sec[c + dx] \right) / \\
 & \left( 4 \sqrt{2} d \left( e \cos[c + dx] \right)^{7/2} \left( e \sec[c + dx] \right)^{7/2} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) + \\
 & \left( 3 i \sqrt{a} e^{7/2} \operatorname{Log}\left[a - \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right] \right) \\
 & \quad \sec[c + dx] \left) / \left( 8 \sqrt{2} d \left( e \cos[c + dx] \right)^{7/2} \left( e \sec[c + dx] \right)^{7/2} \right. \\
 & \quad \left. \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) - \left( 3 i \sqrt{a} e^{7/2} \right. \\
 & \quad \left. \operatorname{Log}\left[a + \frac{\sqrt{2} \sqrt{a} \sqrt{e} \sqrt{a - i a \tan[c + dx]}}{\sqrt{e \sec[c + dx]}} + \cos[c + dx] (a - i a \tan[c + dx])\right] \sec[c + dx] \right) / \\
 & \left( 8 \sqrt{2} d \left( e \cos[c + dx] \right)^{7/2} \left( e \sec[c + dx] \right)^{7/2} \sqrt{a - i a \tan[c + dx]} \sqrt{a + i a \tan[c + dx]} \right) - \\
 & \frac{i \cos[c + dx]^2 \sqrt{a + i a \tan[c + dx]}}{2 a d \left( e \cos[c + dx] \right)^{7/2}}
 \end{aligned}$$

Result (type 7, 165 leaves):

$$\begin{aligned}
 & - \left( \left( e^{\frac{1}{2} i (-2c+dx)} \left( 8 i e^{\frac{1}{2} i (4c+dx)} (-3 + e^{2i(c+dx)}) + \right. \right. \right. \\
 & \quad \left. \left. \left. 3 (1 + e^{2i(c+dx)})^2 \operatorname{RootSum}\left[1 + e^{2ic} \#1^4 \&, \frac{dx + 2i \operatorname{Log}\left[e^{\frac{idx}{2}} - \#1\right]}{\#1^3} \&\right] \right) \right) \right) / \\
 & \left( 16 d e^3 (1 + e^{2i(c+dx)})^2 \sqrt{e \operatorname{Cos}[c+dx]} \sqrt{a + i a \operatorname{Tan}[c+dx]} \right)
 \end{aligned}$$

**Problem 691: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \operatorname{Cos}[c+dx])^m}{a + i a \operatorname{Tan}[c+dx]} dx$$

Optimal (type 5, 86 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{1}{a d m} i 2^{-1-\frac{m}{2}} (e \operatorname{Cos}[c+dx])^m \\
 & \operatorname{Hypergeometric2F1}\left[-\frac{m}{2}, \frac{4+m}{2}, 1-\frac{m}{2}, \frac{1}{2} (1-i \operatorname{Tan}[c+dx])\right] (1+i \operatorname{Tan}[c+dx])^{m/2}
 \end{aligned}$$

Result (type 5, 201 leaves):

$$\begin{aligned}
 & \left( 2^{-1-m} e^{-i(c+2dx)} (1 + e^{2i(c+dx)})^{-m} (e^{-i(c+dx)} (1 + e^{2i(c+dx)}))^m \operatorname{Cos}[c+dx]^{-1-m} \right. \\
 & \quad (e \operatorname{Cos}[c+dx])^m \left( m \operatorname{Hypergeometric2F1}\left[-1-\frac{m}{2}, -m, -\frac{m}{2}, -e^{2i(c+dx)}\right] + \right. \\
 & \quad \left. e^{2i(c+dx)} (2+m) \operatorname{Hypergeometric2F1}\left[-m, -\frac{m}{2}, 1-\frac{m}{2}, -e^{2i(c+dx)}\right] \right) \\
 & \left. (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx]) \right) / (a d m (2+m) (-i + \operatorname{Tan}[c+dx]))
 \end{aligned}$$

**Problem 692: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \operatorname{Cos}[c+dx])^m}{(a + i a \operatorname{Tan}[c+dx])^2} dx$$

Optimal (type 5, 86 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{1}{a^2 d m} i 2^{-2-\frac{m}{2}} (e \operatorname{Cos}[c+dx])^m \\
 & \operatorname{Hypergeometric2F1}\left[-\frac{m}{2}, \frac{6+m}{2}, 1-\frac{m}{2}, \frac{1}{2} (1-i \operatorname{Tan}[c+dx])\right] (1+i \operatorname{Tan}[c+dx])^{m/2}
 \end{aligned}$$

Result (type 5, 264 leaves):



$$\frac{1}{a^2 d m (2+m) (4+m) (-i + \tan[c+dx])^2} \\
 i 2^{-2-m} e^{-2i(c+dx)} (1 + e^{2i(c+dx)})^{-m} (e^{-i(c+dx)} (1 + e^{2i(c+dx)}))^m \cos[c+dx]^{-2-m} \\
 (e \cos[c+dx])^m \left( m (2+m) \text{Hypergeometric2F1}\left[-2 - \frac{m}{2}, -m, -1 - \frac{m}{2}, -e^{2i(c+dx)}\right] + \right. \\
 \left. e^{2i(c+dx)} (4+m) \left( 2m \text{Hypergeometric2F1}\left[-1 - \frac{m}{2}, -m, -\frac{m}{2}, -e^{2i(c+dx)}\right] + e^{2i(c+dx)} \right. \right. \\
 \left. \left. (2+m) \text{Hypergeometric2F1}\left[-m, -\frac{m}{2}, 1 - \frac{m}{2}, -e^{2i(c+dx)}\right]\right) \right) (\cos[dx] + i \sin[dx])^2$$

**Problem 694: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos[c+dx])^m}{\sqrt{a + i a \tan[c+dx]}} dx$$

Optimal (type 5, 104 leaves, 5 steps):

$$- \left( \left( i 2^{-\frac{1}{2}-\frac{m}{2}} (e \cos[c+dx])^m \text{Hypergeometric2F1}\left[-\frac{m}{2}, \frac{3+m}{2}, 1 - \frac{m}{2}, \frac{1}{2} (1 - i \tan[c+dx])\right] \right) \right. \\
 \left. (1 + i \tan[c+dx])^{\frac{1+m}{2}} \right) / (d m \sqrt{a + i a \tan[c+dx]})$$

Result (type 5, 215 leaves):

$$\left( i 2^{-\frac{1}{2}-m} (1 + e^{2i(c+dx)})^{-\frac{1}{2}-m} (e^{-i(c+dx)} (1 + e^{2i(c+dx)}))^m \cos[c+dx]^{-m} (e \cos[c+dx])^m \right. \\
 \left. \text{Hypergeometric2F1}\left[\frac{1}{2} (-1-m), -\frac{1}{2}-m, \frac{1-m}{2}, -e^{2i(c+dx)}\right] \sqrt{\sec[c+dx]} \right. \\
 \left. \sqrt{\cos[dx] + i \sin[dx]} \right) / \left( d \sqrt{e^{i dx}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} (1+m) \sqrt{a + i a \tan[c+dx]} \right)$$

**Problem 696: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \cos[e+fx])^m (a + b \tan[e+fx])^2 dx$$

Optimal (type 5, 155 leaves, 5 steps):

$$- \frac{a b (2-m) (d \cos[e+fx])^m}{f (1-m) m} + \\
 \left( (b^2 - a^2 (1-m)) \cos[e+fx] (d \cos[e+fx])^m \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \cos[e+fx]^2\right] \right. \\
 \left. \sin[e+fx] \right) / \left( f (1-m) (1+m) \sqrt{\sin[e+fx]^2} \right) + \frac{b (d \cos[e+fx])^m (a + b \tan[e+fx])}{f (1-m)}$$

Result (type 5, 465 leaves):

$$\begin{aligned}
 & - \left( \frac{1}{-2+m} \frac{2^{1-m} e^{2i(e+fx)} (e^{-i(e+fx)} + e^{i(e+fx)})^m (1 + e^{2i(e+fx)})^{-m}}{\text{Hypergeometric2F1}\left[1-m, 1-\frac{m}{2}, 2-\frac{m}{2}, -e^{2i(e+fx)}\right]} - \frac{1}{m} \frac{2^{1-m} (e^{-i(e+fx)} + e^{i(e+fx)})^m}{(1 + e^{2i(e+fx)})^{-m} \text{Hypergeometric2F1}\left[1-m, -\frac{m}{2}, 1-\frac{m}{2}, -e^{2i(e+fx)}\right]} \right) \\
 & \left( (a + b \tan[e + fx])^2 \right) / \left( f (a \cos[e + fx] + b \sin[e + fx])^2 \right) - \\
 & \left( b^2 \cos[e + fx] (d \cos[e + fx])^m \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2}(-1+m), \frac{1+m}{2}, \cos[e + fx]^2\right] \right. \\
 & \left. \sin[e + fx]^3 (a + b \tan[e + fx])^2 \right) / \\
 & \left( f(-1+m) (\sin[e + fx]^2)^{3/2} (a \cos[e + fx] + b \sin[e + fx])^2 \right) - \\
 & \left( a^2 \cos[e + fx]^3 (d \cos[e + fx])^m \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \cos[e + fx]^2\right] \right. \\
 & \left. \sin[e + fx] (a + b \tan[e + fx])^2 \right) / \\
 & \left( f(1+m) \sqrt{\sin[e + fx]^2} (a \cos[e + fx] + b \sin[e + fx])^2 \right)
 \end{aligned}$$

**Problem 697: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \cos[e + fx])^m (a + b \tan[e + fx]) dx$$

Optimal (type 5, 90 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{b (d \cos[e + fx])^m}{f m} - \\
 & \left( a (d \cos[e + fx])^{1+m} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \cos[e + fx]^2\right] \sin[e + fx] \right) / \\
 & \left( d f (1+m) \sqrt{\sin[e + fx]^2} \right)
 \end{aligned}$$

Result (type 5, 297 leaves):

$$\begin{aligned}
 & \frac{1}{f (-2+m) m (1+m) \sqrt{\sin[e+fx]^2} (a \cos[e+fx] + b \sin[e+fx])} \\
 & 2^{-m} (1 + e^{2i(e+fx)})^{-m} \cos[e+fx]^{1-m} (d \cos[e+fx])^m \\
 & \left( -2^m a (1 + e^{2i(e+fx)})^m (-2+m) m \cos[e+fx]^{1+m} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, \cos[e+fx]^2\right] \sin[e+fx] + b (e^{-i(e+fx)} (1 + e^{2i(e+fx)}))^m (1+m) \right. \\
 & \quad \left. (e^{2i(e+fx)} m \operatorname{Hypergeometric2F1}\left[1-m, 1-\frac{m}{2}, 2-\frac{m}{2}, -e^{2i(e+fx)}\right] - (-2+m) \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[1-m, -\frac{m}{2}, 1-\frac{m}{2}, -e^{2i(e+fx)}\right]\right) \sqrt{\sin[e+fx]^2} (a + b \tan[e+fx])
 \end{aligned}$$

**Problem 698: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(d \cos[e+fx])^m}{a + b \tan[e+fx]} dx$$

Optimal (type 6, 140 leaves, 7 steps):

$$\begin{aligned}
 & \frac{b (d \cos[e+fx])^m \operatorname{Hypergeometric2F1}\left[1, -\frac{m}{2}, 1-\frac{m}{2}, \frac{b^2 \sec[e+fx]^2}{a^2+b^2}\right]}{(a^2 + b^2) f m} + \\
 & \frac{1}{a f} \operatorname{AppellF1}\left[\frac{1}{2}, 1, \frac{2+m}{2}, \frac{3}{2}, \frac{b^2 \tan[e+fx]^2}{a^2}, -\tan[e+fx]^2\right] \\
 & (d \cos[e+fx])^m (\sec[e+fx]^2)^{m/2} \tan[e+fx]
 \end{aligned}$$

Result (type 6, 1132 leaves):

$$\begin{aligned}
 & \left( (d \operatorname{Cos}[e + f x])^m \right. \\
 & \left. \left( b \left( -1 + (\operatorname{Sec}[e + f x]^2)^{-m/2} \right) + a m \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 + \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}[e + f x] - b \operatorname{AppellF1} \left[ m, \frac{m}{2}, \frac{m}{2}, 1 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \right. \right. \\
 & \quad \left. \left. (\operatorname{Sec}[e + f x]^2)^{-m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \right) \right) / \\
 & \left( f (a + b \operatorname{Tan}[e + f x]) \left( a m \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 + \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2 \right] \operatorname{Sec}[e + f x]^2 - \right. \right. \\
 & \quad b m (\operatorname{Sec}[e + f x]^2)^{-m/2} \operatorname{Tan}[e + f x] + \\
 & \quad b m \operatorname{AppellF1} \left[ m, \frac{m}{2}, \frac{m}{2}, 1 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{-m/2} \operatorname{Tan}[e + f x] \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} - \right. \\
 & \quad b (\operatorname{Sec}[e + f x]^2)^{-m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \\
 & \quad \left. \left( - \left( \left( (a - i b) b m^2 \operatorname{AppellF1} \left[ 1 + m, 1 + \frac{m}{2}, \frac{m}{2}, 2 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}[e + f x]^2 \right) / \left( 2 (1 + m) (a + b \operatorname{Tan}[e + f x])^2 \right) \right) - \right. \\
 & \quad \left. \left( (a + i b) b m^2 \operatorname{AppellF1} \left[ 1 + m, \frac{m}{2}, 1 + \frac{m}{2}, 2 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e + f x]^2 \right) / \left( 2 (1 + m) (a + b \operatorname{Tan}[e + f x])^2 \right) \right) - \\
 & \quad \frac{1}{2} b m \operatorname{AppellF1} \left[ m, \frac{m}{2}, \frac{m}{2}, 1 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{-m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-1 + \frac{m}{2}} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \right. \\
 & \quad \left. \left( - \frac{b^2 \operatorname{Sec}[e + f x]^2 (-i + \operatorname{Tan}[e + f x])}{(a + b \operatorname{Tan}[e + f x])^2} + \frac{b \operatorname{Sec}[e + f x]^2}{a + b \operatorname{Tan}[e + f x]} \right) - \right. \\
 & \quad \frac{1}{2} b m \operatorname{AppellF1} \left[ m, \frac{m}{2}, \frac{m}{2}, 1 + m, \frac{a - i b}{a + b \operatorname{Tan}[e + f x]}, \frac{a + i b}{a + b \operatorname{Tan}[e + f x]} \right] \\
 & \quad \left. (\operatorname{Sec}[e + f x]^2)^{-m/2} \left( \frac{b (-i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{m/2} \left( \frac{b (i + \operatorname{Tan}[e + f x])}{a + b \operatorname{Tan}[e + f x]} \right)^{-1 + \frac{m}{2}} \right. \\
 & \quad \left. \left( - \frac{b^2 \operatorname{Sec}[e + f x]^2 (i + \operatorname{Tan}[e + f x])}{(a + b \operatorname{Tan}[e + f x])^2} + \frac{b \operatorname{Sec}[e + f x]^2}{a + b \operatorname{Tan}[e + f x]} \right) + a m \operatorname{Sec}[e + f x]^2 \right. \\
 & \quad \left. \left. \left. \left( -\operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 + \frac{m}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2 \right] + (1 + \operatorname{Tan}[e + f x]^2)^{-1 - \frac{m}{2}} \right) \right) \right) \right)
 \end{aligned}$$

**Problem 699: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(d \cos [e + f x])^m}{(a + b \tan [e + f x])^2} dx$$

Optimal (type 6, 227 leaves, 8 steps):

$$\frac{2 a b (d \cos [e + f x])^m \text{Hypergeometric2F1}\left[2, -\frac{m}{2}, 1 - \frac{m}{2}, \frac{b^2 \sec [e + f x]^2}{a^2 + b^2}\right]}{(a^2 + b^2)^2 f m} + \frac{1}{a^2 f}$$

$$\text{AppellF1}\left[\frac{1}{2}, 2, \frac{2+m}{2}, \frac{3}{2}, \frac{b^2 \tan [e + f x]^2}{a^2}, -\tan [e + f x]^2\right] (d \cos [e + f x])^m (\sec [e + f x]^2)^{m/2}$$

$$\tan [e + f x] + \frac{1}{3 a^4 f} b^2 \text{AppellF1}\left[\frac{3}{2}, 2, \frac{2+m}{2}, \frac{5}{2}, \frac{b^2 \tan [e + f x]^2}{a^2}, -\tan [e + f x]^2\right] \\ (d \cos [e + f x])^m (\sec [e + f x]^2)^{m/2} \tan [e + f x]^3$$

Result (type 6, 361 leaves):

$$-\left(\left(2(4+m) \text{AppellF1}\left[3+m, 1+\frac{m}{2}, 1+\frac{m}{2}, 4+m, \frac{a-i b}{a+b \tan [e+f x]}, \frac{a+i b}{a+b \tan [e+f x]}\right] \right. \right. \\ \left. \left. (d \cos [e+f x])^m \sec [e+f x]^2 (a \cos [e+f x] + b \sin [e+f x])^5\right) / (b f (3+m)) \right. \\ \left. \left( (2+m) \left( (a+i b) \text{AppellF1}\left[4+m, 1+\frac{m}{2}, 2+\frac{m}{2}, 5+m, \frac{a-i b}{a+b \tan [e+f x]}, \frac{a+i b}{a+b \tan [e+f x]}\right] \right. \right. \right. \\ \left. \left. \left. (a-i b) \text{AppellF1}\left[4+m, 2+\frac{m}{2}, 1+\frac{m}{2}, 5+m, \frac{a-i b}{a+b \tan [e+f x]}, \frac{a+i b}{a+b \tan [e+f x]}\right] \right) \right) \right. \\ \left. \cos [e+f x] + 2(4+m) \text{AppellF1}\left[3+m, 1+\frac{m}{2}, 1+\frac{m}{2}, 4+m, \frac{a-i b}{a+b \tan [e+f x]}, \frac{a+i b}{a+b \tan [e+f x]}\right] \right) (a \cos [e+f x] + b \sin [e+f x]) (a+b \tan [e+f x])^5 \Bigg)$$

**Problem 700: Result unnecessarily involves imaginary or complex numbers.**

$$\int (d \cos [e + f x])^m (a + b \tan [e + f x])^n dx$$

Optimal (type 6, 187 leaves, 4 steps):

$$\frac{1}{b f (1+n)} \text{AppellF1}\left[1+n, \frac{2+m}{2}, \frac{2+m}{2}, 2+n, \frac{a+b \tan [e+f x]}{a-\sqrt{-b^2}}, \frac{a+b \tan [e+f x]}{a+\sqrt{-b^2}}\right] \cos [e+f x]^2$$

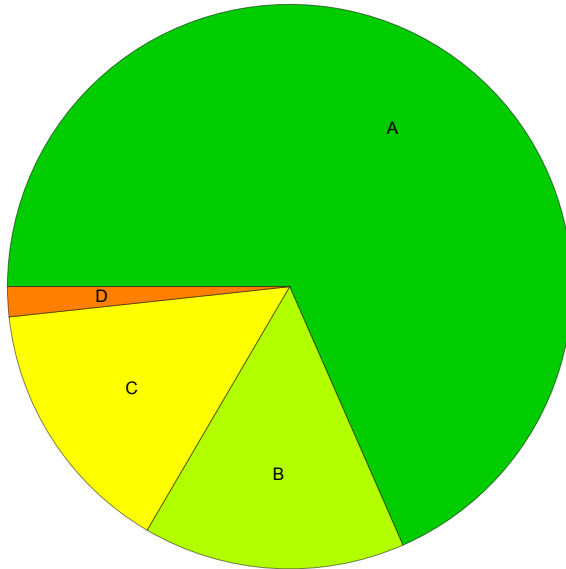
$$(d \cos [e + f x])^m (a + b \tan [e + f x])^{1+n} \left(1 - \frac{a + b \tan [e + f x]}{a - \sqrt{-b^2}}\right)^{\frac{2+m}{2}} \left(1 - \frac{a + b \tan [e + f x]}{a + \sqrt{-b^2}}\right)^{\frac{2+m}{2}}$$

Result (type 6, 365 leaves):

$$\begin{aligned}
 & \left( 2 (a - i b) (a + i b) (2 + n) \right. \\
 & \quad \text{AppellF1} \left[ 1 + n, 1 + \frac{m}{2}, 1 + \frac{m}{2}, 2 + n, \frac{a + b \tan[e + f x]}{a - i b}, \frac{a + b \tan[e + f x]}{a + i b} \right] \cos[e + f x] \\
 & \quad \left. (d \cos[e + f x])^m (a \cos[e + f x] + b \sin[e + f x]) (a + b \tan[e + f x])^n \right) / (b f (1 + n) \\
 & \quad \left( 2 (a^2 + b^2) (2 + n) \text{AppellF1} \left[ 1 + n, 1 + \frac{m}{2}, 1 + \frac{m}{2}, 2 + n, \frac{a + b \tan[e + f x]}{a - i b}, \frac{a + b \tan[e + f x]}{a + i b} \right] + \right. \\
 & \quad (2 + m) \left( (a - i b) \text{AppellF1} \left[ 2 + n, 1 + \frac{m}{2}, 2 + \frac{m}{2}, 3 + n, \frac{a + b \tan[e + f x]}{a - i b}, \frac{a + b \tan[e + f x]}{a + i b} \right] + \right. \\
 & \quad \left. (a + i b) \text{AppellF1} \left[ 2 + n, 2 + \frac{m}{2}, 1 + \frac{m}{2}, 3 + n, \frac{a + b \tan[e + f x]}{a - i b}, \frac{a + b \tan[e + f x]}{a + i b} \right] \right) (a + \\
 & \quad \left. \left. \left. b \tan[e + f x] \right) \right) \right)
 \end{aligned}$$

## Summary of Integration Test Results

700 integration problems



A - 479 optimal antiderivatives

B - 105 more than twice size of optimal antiderivatives

C - 104 unnecessarily complex antiderivatives

D - 12 unable to integrate problems

E - 0 integration timeouts